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ของก๊าซซัลเฟอร์ไดออกไซด์ในพูนโดยใช้วิธีมอนทิการ์โล



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**Modeling of Sulfur Dioxide Oxidation in Plume
Using the Monte Carlo Method**

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A Thesis Submitted in Partial Fulfillment of the Requirements

for the Degree of Master of Engineering

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พิมพ์ด้วยบันทึกด้วยวิทยานิพนธ์ถ่ายในกรอบสีเขียวที่พิมพ์ผ่านโดย

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ให้วิธีมอนติคาร์โล (MODELING OF SULFUR DIOXIDE OXIDATION IN PLUME USING THE MONTE CARLO METHOD)

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การวิจัยนี้ประกอบด้วยการสร้างแบบจำลองทางคณิตศาสตร์ของปฏิกิริยาออกซิเดชั่นของก๊าซซัลเฟอร์โดยใช้ไอน้ำในพิมพ์โดยให้วิธีมอนติคาร์โลสำหรับแหล่งกำเนิดแบบบุดและลักษณะภูมิประเทศเป็นที่ราบ แบบจำลองทางคณิตศาสตร์แบบภายในภูมิภาคเมืองที่สามารถประมวลผลการเพร่กระจายแบบ gauss เสียนและการเปลี่ยนแปลงทางปฏิกิริยาเคมีของก๊าซซัลเฟอร์โดยใช้ไอด์ ปฏิกิริยาเคมีของ Brimblecombe และ Spedding (1974) ปฏิกิริยาเคมีของ Freiberg (1974) ในสภาพแวดล้อมที่มีไอน้ำเนียมาก และ แอมโมเนียนีจำกัด และ ปฏิกิริยาเคมีของ Ibusuki, Ohsawa และ Takeuchi (1990) ในสภาพแวดล้อมที่มีไอน้ำเนียมาก ทั้ง 3 ปฏิกิริยานี้เป็นปฏิกิริยาที่ใช้ในการศึกษาไวเคราะห์ความไวทางปฏิกิริยาเคมีด้วยแบบจำลองทางคณิตศาสตร์ โดยทำการเปลี่ยนตัวแปรต่าง ๆ ดังนี้ คือ ความสูงของบรรยายกาศ ความชื้นสัมพัทธ์ อุณหภูมิ ความเข้มข้นของเหล็ก และ แอมโมเนีย ในการศึกษานี้ความเข้มข้นของซัลเฟตที่วัดได้ในอากาศบริเวณบ้านๆ ถูกเปรียบเทียบกับความเข้มข้นของซัลเฟตที่ประมวลผลได้จากปฏิกิริยาเคมีของ Freiberg (1974) และ Alkezweeny และ Powell (1977) ด้วย

ผลการศึกษาของการเกิดซัลเฟตของปฏิกิริยาเคมีทั้ง 3 แบบ พบว่า ปฏิกิริยาเคมีของ Freiberg (1974) ทั้งในสภาพแวดล้อมที่มีไอน้ำเนียมาก และ แอมโมเนียนีจำกัด มีซัลเฟตเกิดขึ้นที่ความชื้นสัมพัทธ์สูง แต่ปฏิกิริยาเคมีของ Brimblecombe และ Spedding (1974) และ ปฏิกิริยาเคมีของ Ibusuki et al. (1990) ในสภาพแวดล้อมที่มีไอน้ำเนียมาก กลับพบว่า มีการเกิดซัลเฟตได้น้อยมาก ในทุกสถานการณ์

ผลการวิเคราะห์ความไวทางปฏิกิริยาเคมีของปฏิกิริยาเคมีแบบ Freiberg (1974) ในสภาพแวดล้อมที่มีไอน้ำเนียมาก และ แอมโมเนียนีจำกัด พบว่า อัตราการเกิดซัลเฟตจะเพิ่มขึ้น เมื่อความชื้นสัมพัทธ์ ความเข้มข้นของเหล็ก และ แอมโมเนียนีเพิ่มขึ้น และ เมื่ออุณหภูมิลดลง ในสภาพแวดล้อมที่มีไอน้ำเนียมาก และ แอมโมเนียนีจำกัด จะพบว่า ปริมาณซัลเฟตจะเกิดขึ้นในกรณีแรกมากกว่าในกรณีที่สองสำหรับที่เงื่อนไขเดียวกัน ในการทดลองเปลี่ยนความสูงของบรรยายกาศ พบว่า ปริมาณซัลเฟตที่เกิดขึ้นมีค่าต่ำมากในความสูงของบรรยายกาศแบบไม่สูง และ แบบสูงเทิน ในทางกลับกัน ปริมาณซัลเฟตที่เกิดขึ้นมีค่าสูงมากในความสูงของบรรยายกาศแบบสูงเทินจากเป็นปฏิกิริยาเคมีแบบขันดับที่สอง

ปริมาณซัลเฟตต่อซัลเฟอร์โดยใช้ไอด์ที่วัดได้ที่จุดตรวจบ้านๆ และ ที่ความเร็วลมเท่ากับ 2 เมตร ต่อ วินาที เปรียบเทียบกับปริมาณซัลเฟตต่อซัลเฟอร์โดยใช้ไอด์ที่ได้จากปฏิกิริยาเคมีของ Freiberg (1974) ให้ข้อสรุปว่า ปฏิกิริยาเคมีของ Freiberg (1974) อาจมีความสำคัญในการออกซิเดชั่นซัลเฟอร์โดยใช้ไอด์ให้กับลายเป็นซัลเฟต หากในสภาพแวดล้อมมีปัจจัย เช่น ความชื้นสัมพัทธ์ ความเข้มข้นของแอมโมเนีย และ เหล็กที่สูง และ อุณหภูมิที่ต่ำ



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MUTITA TRIWITTAYAPOOM : MODELING OF SULFUR DIOXIDE OXIDATION IN PLUME USING THE MONTE CARLO METHOD.

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This research succeeds in modeling of sulfur dioxide oxidation in plume using the Monte Carlo method for a single point source and flat terrain. The physico-chemical mathematical model is capable of simulating the Gaussian dispersions and chemical transformations of sulfur dioxide. The mathematical model was also used to assess sensitivity analysis of Brimblecombe and Spedding (1974)'s reaction rate, Freiberg (1974)'s reaction rate in ammonia-rich environment and in ammonia-deficient environment and Ibusuki, Ohsawa and Takeuchi (1990)'s reaction rate in ammonia-rich environment, which effects sulfate formation by varying parameters such as atmospheric stability class, relative humidity, temperature, iron and ammonia concentrations. In this study, the measured sulfate concentration in Bang Na was compared with the simulated sulfate concentrations calculated from Freiberg (1974)'s reaction rate and Alkezweeny and Powell (1977)'s first order reaction rate.

In comparison with yields of three chemical reactions, it is found that no yield occurs for Brimblecombe and Spedding (1974)'s reaction rate. Only at relative humidity of 99%, Freiberg (1974)'s reaction rate in both of ammonia-rich environment and ammonia-deficient environment plays a significant role in sulfate formation for every atmospheric stability class, temperature, iron concentration or ammonia concentration variations. Ibusuki et al. (1990)'s reaction rate in ammonia-rich environment does not cause significant yield for each atmospheric stability class, nor as a result of the temperature decrease or the relative humidity increase or the ammonia concentration increase or iron concentration increase.

The results of sensitivity analysis of Freiberg (1974)'s reaction rate in ammonia-rich environment and in ammonia-deficient environment indicate that the sulfate formation increases with increasing relative humidity, iron and ammonia concentrations and with decreasing temperature. Between ammonia-rich environment and ammonia-deficient environment, the yield in the first condition is much more than that in the latter condition for the same given condition. In the cases of varying atmospheric stability class, the sulfate production is very low in the unstable and neutral atmospheric stabilities, vice versa, the conversion of sulfur dioxide to sulfate is very high in the stable atmosphere due to the nature of second order reaction rate.

The measured yield during the dry season at the location of Bang Na with wind velocity of 2 m/s and Freiberg (1974)'s yields in some cases provide the comparable yields, which indicate that Freiberg (1974)'s reaction rate may become important if relative humidity, ammonia and iron concentrations are high with low temperature in the environment.

ภาควิชา วิศวกรรมดิ่งและกล้อง

ลายมือชื่อนิสิต พัฒน์ พร้อมกุล

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ลายมือชื่ออาจารย์ที่ปรึกษา

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ลายมือชื่ออาจารย์ที่ปรึกษาร่วม



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Nomenclature

C	concentration of the non-gaseous pollutant	(g/m ³)
d	stack diameter	(m)
g	gravitational acceleration	(m/s ²)
Δh	plume rise	(m)
H	effective height	(m)
K_d	diffusion coefficient	(m ² /s)
K_n	dissociation constant of ammonia	(mole/m ³)
K_o	rate constant of the reaction	(m ³ /mole-min)
K_s	first dissociation constant of sulfurous acid	(mole/m ³)
K_w	dissociation constant of water	(mole/m ³) ²
K_x	diffusion coefficient in x direction	(m ² /s)
K_y	diffusion coefficient in y direction	(m ² /s)
K_z	diffusion coefficient in z direction	(m ² /s)
m	m^{th} order with respect to oxidizing agent or inert substance or catalyst concentration	(-)
n	n^{th} order with respect to sulfur dioxide concentration	(-)
P	probability of sulfur dioxide to sulfate transformation of each sulfur dioxide quantum	(-)
P1	probability of sulfur dioxide to sulfate transformation of the first sulfur dioxide quantum	(-)
P2	probability of sulfur dioxide to sulfate transformation of the second sulfur dioxide quantum	(-)

Nomenclature (Continued)

P_{total}	probability of sulfur dioxide to sulfate	
	transformation of the both sulfur dioxide quanta	(-)
Q	sulfur dioxide emission rate	(g/s)
RH	relative humidity	(-)
t	time	(s or min)
T	temperature	(°C)
T_a	absolute temperature of ambient atmosphere	(K)
T_s	absolute flue gas exit temperature	(K)
\bar{u}	average wind velocity	(m/s)
V_s	stack gas exit velocity	(m/s)
x	distance downwind from the source	(m)
y	distance horizontally from the plume center line	(m)
z	distance vertically from the plume center line	(m)
β_n	Ostwald's constant for ammonia	(-)
β_s	Ostwald's constant for sulfur dioxide	(-)
λ_z	pressure-lowering coefficient for ammonium sulfate	(m ³ /mole)
σ_y	horizontal dispersion coefficient	(m)
σ_z	vertical dispersion coefficient	(m)
[]	molar concentration of the component	(mole/m ³)
subscript [] _o	initial condition	(-)
subscript [] _{react}	reacting condition	(-)
subscript [] _{remaining}	remaining condition	(-)
subscript () _{acc}	accumulation condition	(-)

Nomenclature (Continued)

subscript () _{in}	input condition	(-)
subscript () _{out}	output condition	(-)