



REFERENCES

- Aubry, D., and Postel, M. 1985. Dynamic response of a large number of piles by homogeneization. In C.A. Brebbia et al. (eds.), Soil dynamics and earthquake engineering. Vol. 4, pp. 105-114. Southampton : Springer-Verlag.
- Berger, E., Lysmer, J. and Seed, H.B. 1975. Comparison of plane strain and axisymmetric soil-structure analyses. Proceedings of the Second ASCE Specialty Conference on Structure Design of Nuclear Plant Facilities. Vol. I-A. pp. 809-825. New Orleans.
- Blaney, G.W., Kausel, E., and Roesset, J.M. 1976. Dynamic stiffness of piles. Proceedings of the International Conference on Numerical Methods in Geomechanics. Vol. 2. pp. 1001-1012. Virginia.
- Clough, R.W., and Penzien, J. 1975. Dynamics of Structures. New York : McGraw-Hill.
- Hwang, R.N., Lysmer, J. and Berger, E. 1975. A simplified three-dimensional soil-structure interaction study. Proceedings of the Second ASCE special Conference on Structure Design of Nuclear Plant Facilities. Vol. I-A, pp. 786-808. New Orleans.
- Karasudhi, P., Keer, L.M., and Lee, S.L. 1968. Vibratory motion of a body on an elastic half plane. J. of Applied Mechanics 35 : 697-705.
- Kausel, E., and Roesset, J.M. 1975. Dynamic stiffness of circular foundations. J. of the Engineering Mechanics Division, ASCE 101 : 771-785.
- Kausel, E., Roesset, J.M. and Waas, G. 1975. Dynamic analysis of footings on layered media. J. of the Engineering Mechanics Division, ASCE 101 : 679-693.

- Luco, J.E., and Hadjian, A.H. 1974. Two-dimensional approximations to the three-dimensional soil-structure interaction problem. Nuclear Engineering and Design 31 : 195-203.
- Luco, J.E., and Westmann, R.A. 1971. Dynamic response (of circular footings). J. of the Engineering Mechanics Division, ASCE 97 : 1381-1395.
- Luco, J.E., and Westmann, R.A. 1972. Dynamic response of a rigid footing bounded to an elastic half space. J. of Applied Mechanics, ASCE 32 : 527-534.
- Lysmer, J., and Kuhlemeyer, A.M. 1969. Finite dynamics model for infinite media. J. of the Engineering Mechanics Division, ASCE 95 : 859-877.
- Lysmer, J. and Richart, F.E. 1966. Dynamic response of footings to vertical loading. J. of the Soil Mechanics and Foundations Division, ASCE 92 : 65-91.
- Lysmer, J., Udaka, T., Seed, H.B., and Hwang, R. 1974. LUSH – A computer program for complex response analysis of soil-structure system [Computer program], Berkeley : University of California. (Earthquake Engineering Research Center Report No. EERC 74-4).
- Lysmer, J., Udaka, T., Tsai, C.F. and Seed, H.B. 1975. FLUSH – A computer program for approximate 3-D analysis of soil-structure interaction problems [Computer program], Berkeley : University of California. (Earthquake Engineering Research Center Report No. EERC 75-30).
- Nogami, T., and Novak, M. 1976. Soil-pile interaction in vertical vibration. Earthquake Engineering and Structural Dynamics 4 : 277-293.
- Novak, M. 1974. Dynamic stiffness and damping of piles. Canadian Geotechnical Journal 11 : 574-598.
- Novak, M., and Nogami, T. 1977. Soil-pile interaction in horizontal vibration. Earthquake Engineering and Structural Dynamics 5 : 263-281.

- Penzien, J. 1970. Soil-pile foundation interaction. In R.L. Wiegel (ed.), Earthquake engineering, ch. 14. New Jersey : Prentice-Hall.
- Phillips, D.V., and Zienkiewicz, O.C. 1976. Finite element non-linear analysis of concrete structures. ICE proceedings 61 : 59-88.
- Roesset, J.M., and Ettouney, M.M. 1977. Transmitting boundaries : A comparison. International Journal for Numerical and Analitical Methods in Geomechanics 1 : 151-176.
- Seed, H.B., and Idriss, I.M. 1969. The influence of soil conditions on ground motions during earthquakes. J. of the Soil Mechanics and Foundations Division, ASCE 94 : 99-137.
- Tantiprabha, P. 1981. A prestressing tendon element and its application to segmental prestressed concrete box girders. Master's Thesis, Asian Institute of Technology.
- Veletsos, A.S., and Wei, T.Y. 1971. Lateral and rocking vibration of footings. J. of the Soil Mechanics and Foundation Division, ASCE 97 : 1227-1248.
- Washizu, K. 1968. Variational methods in elasticity and plasticity. Oxford : Pergamon Press.
- Waas, G. 1972. Analysis method for footing vibrations through layered media. Ph.D. Dissertation, University of California, Berkeley.
- Wolf, J.P. 1985. Dynamic soil-structure interaction. New Jersey : Prentice-Hall.
- Wolf, J.P., and von Arx, G.A. 1978. Impedance function of a group of vertical piles. Proceedings of the ASCE Specialty Conference on Earthquake Engineering and Soil Dynamics 2 : 1024-1041. Pasadena, CA.
- Zienkiewicz, O.C. 1977. The finite element method. 2nd ed. New York : McGraw-Hill Book Co.

FIGURES

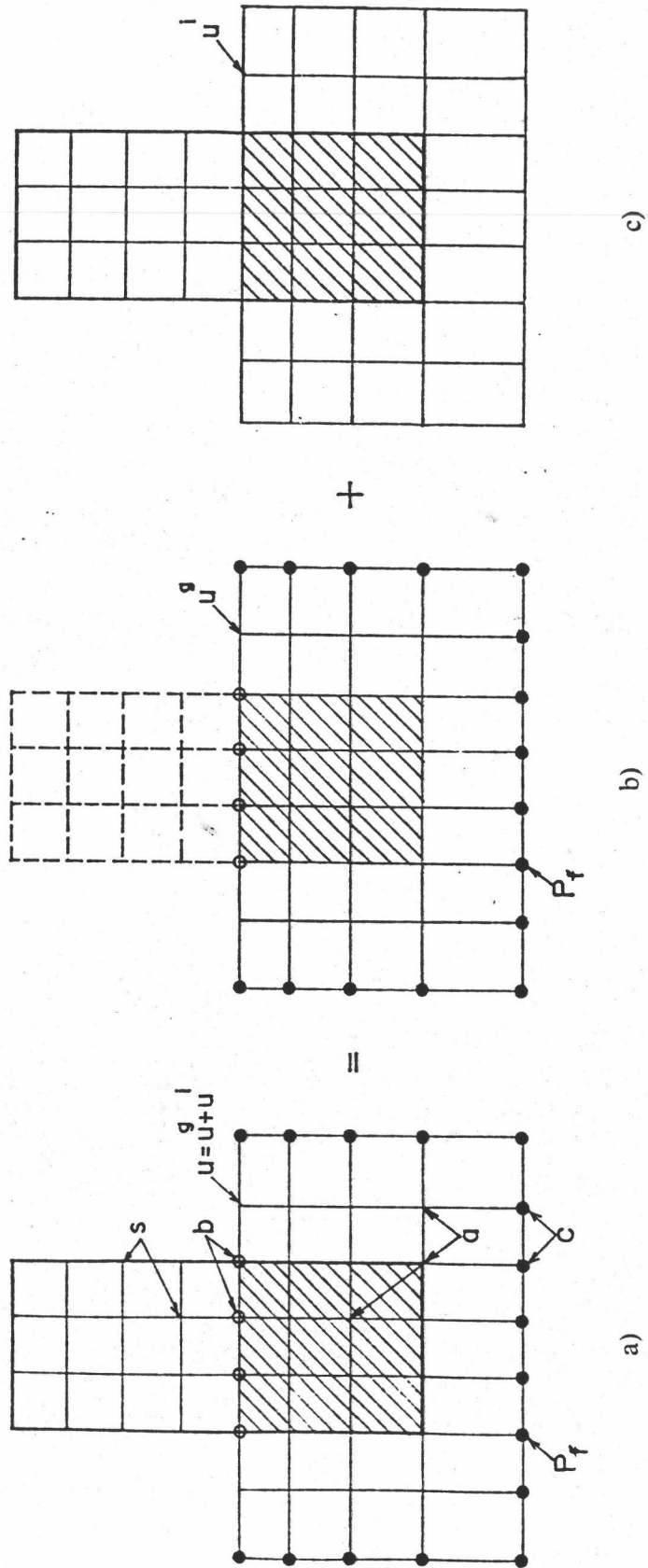


FIGURE 2.1 Displacement superposition schematic representation of soil-structure interaction substructuring a) complete model b) model of foundation without super-structure c) interaction model

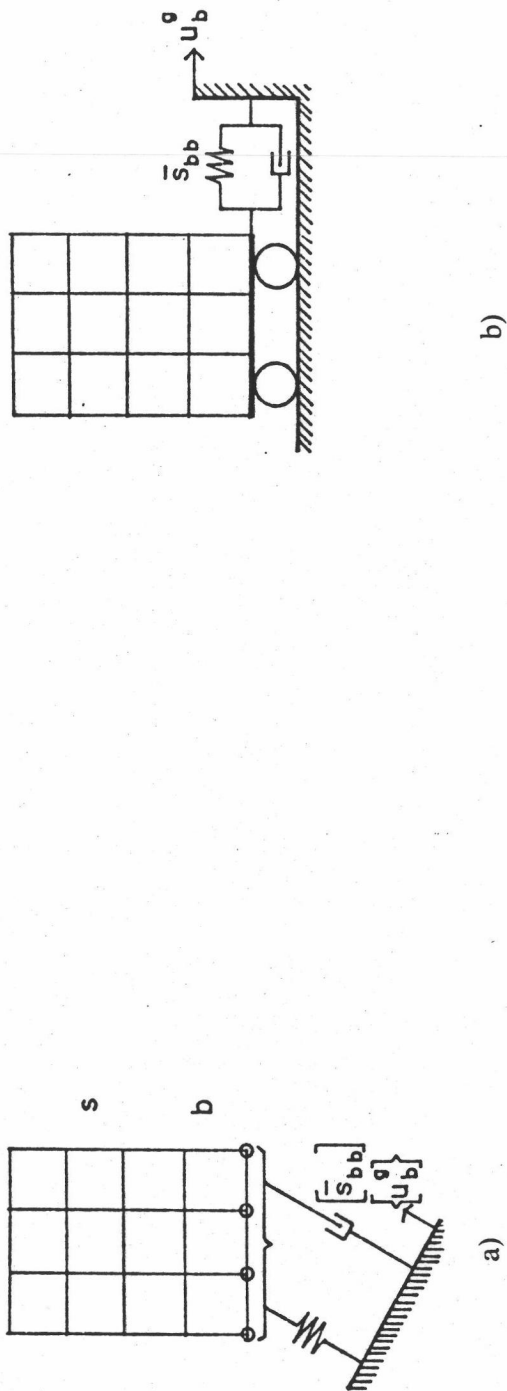


FIGURE 2.2 Physical interpretation of soil-structure interaction analysis using substructure

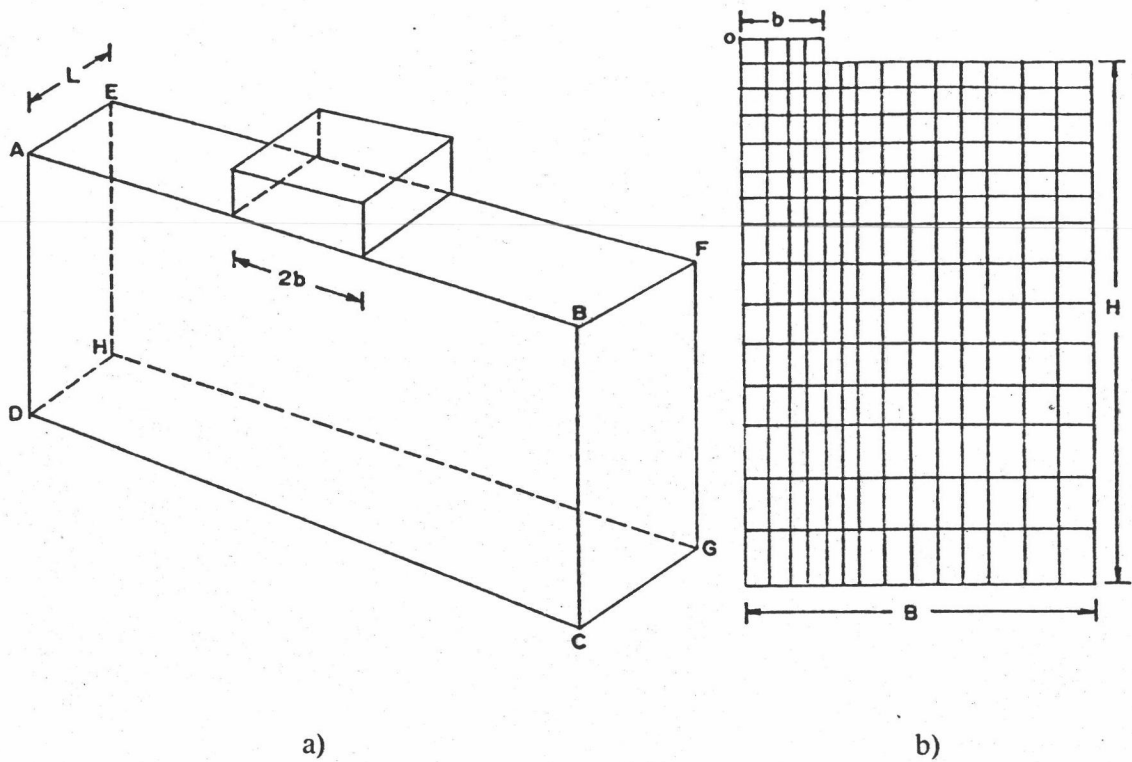


FIGURE 3.1 a) Soil-structure model
 b) Finite element discretization $B/b = 4.3$, $H/B = 1.5$,
 $\nu = 0.25$

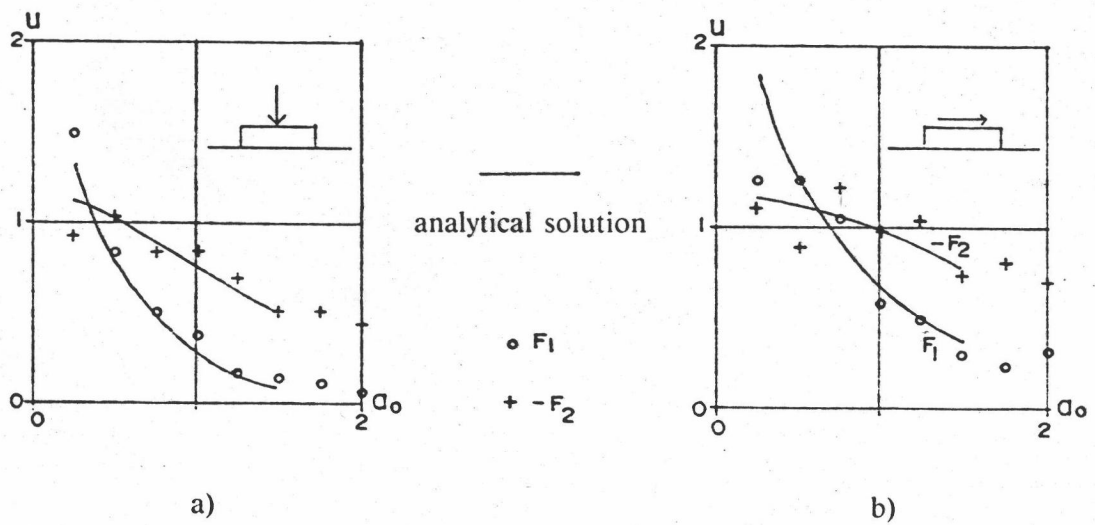


FIGURE 3.2 Non-dimensional displacement functions comparing the plane strain finite element and analytical solutions

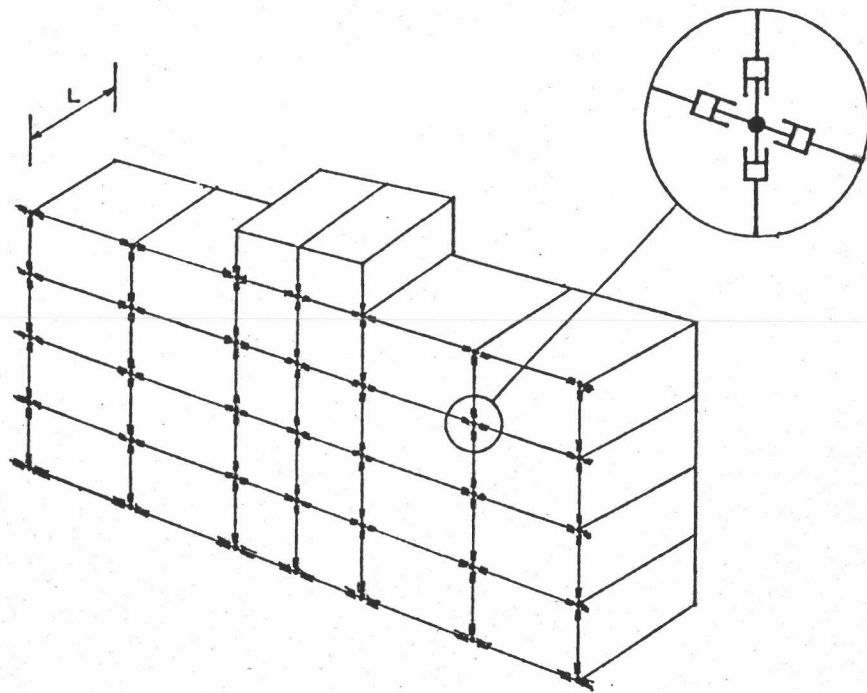


FIGURE 3.3 Simplified three-dimensional model using dashpots

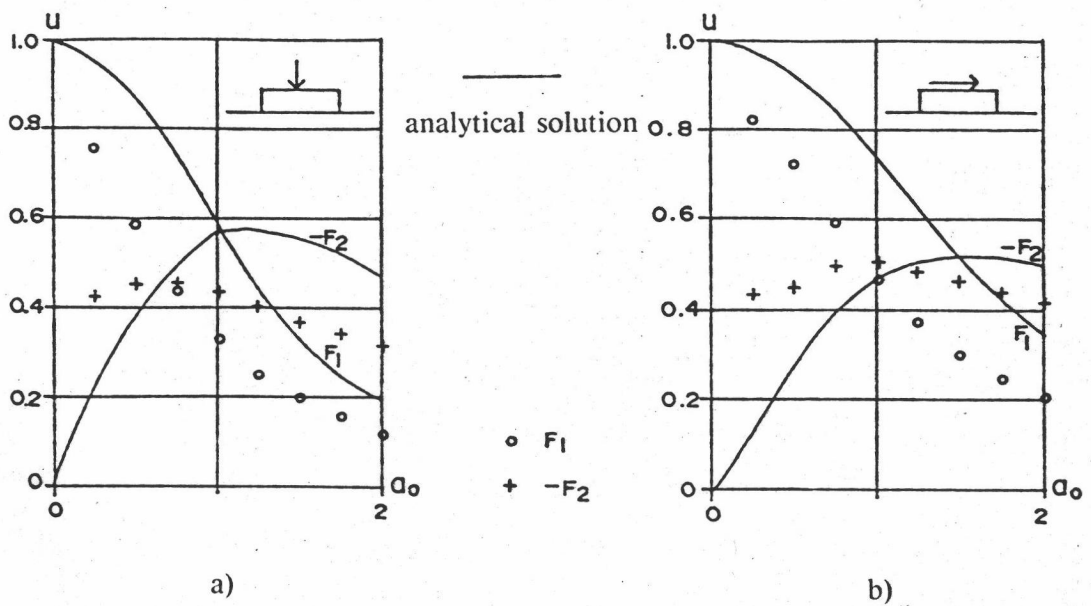


FIGURE 3.4 Non-dimensional displacement functions of circular footing on elastic half space comparing the Hwang's simplified three-dimensional model and analytical solutions

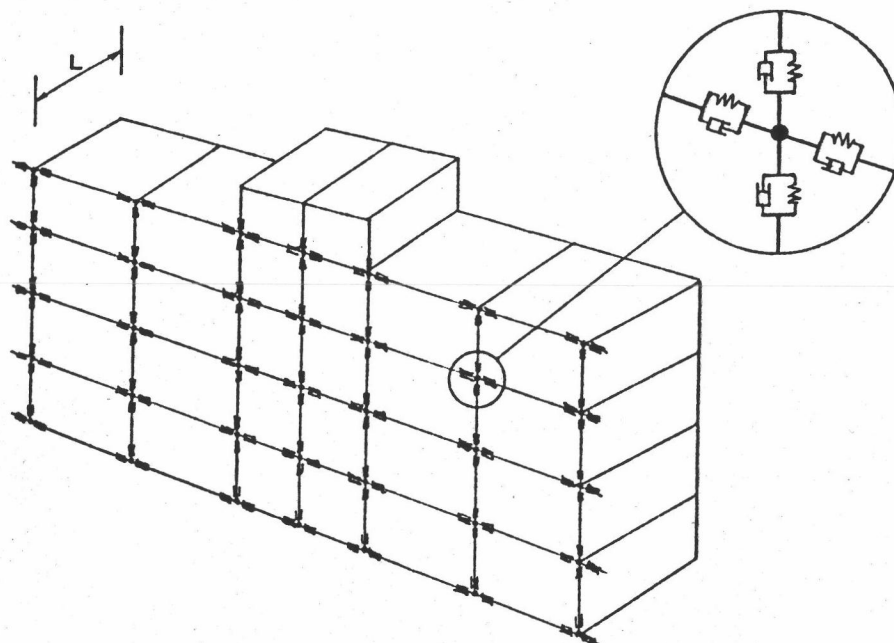


FIGURE 3.5 Equivalent plane strain model using dashpots together with side springs

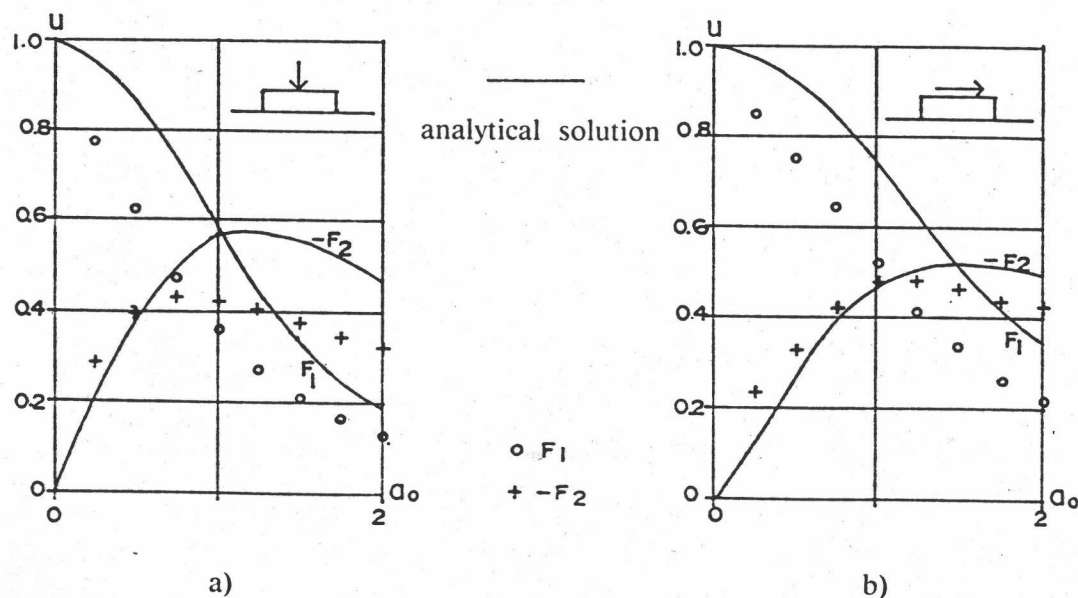


FIGURE 3.6 Non-dimensional displacement functions of circular footing on elastic half space comparing the proposed model using Hwang's parameters and analytical solutions

a) $C_m = 1.0$, $C_d = 1.0$ and $C_s = 0.0259$

b) $C_m = 1.0$, $C_d = 1.0$ and $C_s = 0.0449$

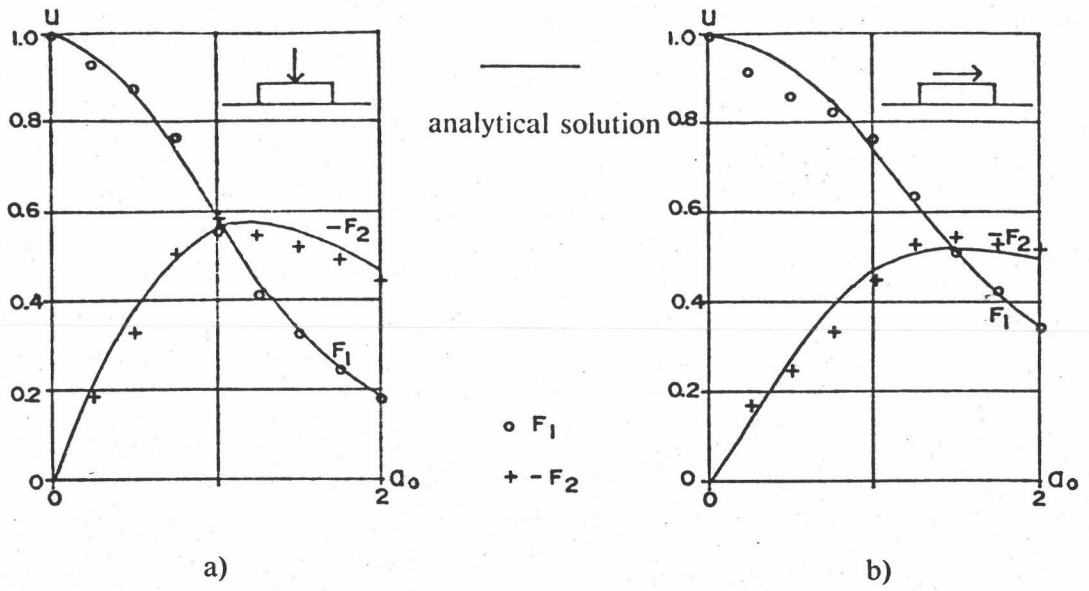


FIGURE 3.7 Non-dimensional displacement functions of circular footing on elastic half space comparing the proposed model after adjustment of parameters C_m and C_d and analytical solutions

a) $C_m = 0.55$, $C_d = 0.35$ and $C_s = 0.0259$

b) $C_m = 0.50$, $C_d = 0.50$ and $C_s = 0.0449$

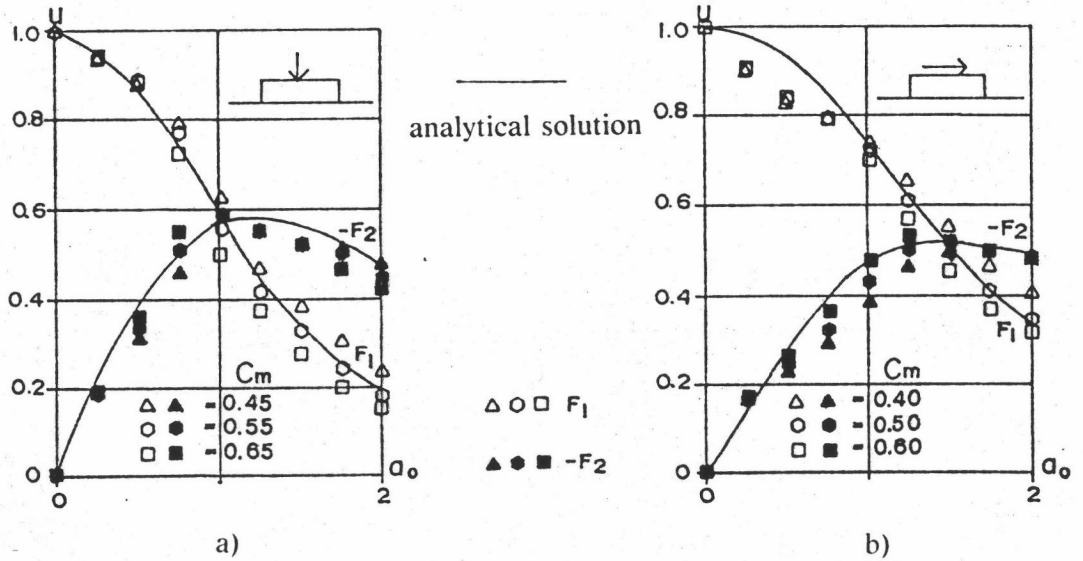


FIGURE 3.8 Parametric study on the variations of C_m while keeping C_d and C_s constant

a) $C_d = 0.35$, $C_s = 0.026$

b) $C_d = 0.50$, $C_s = 0.042$

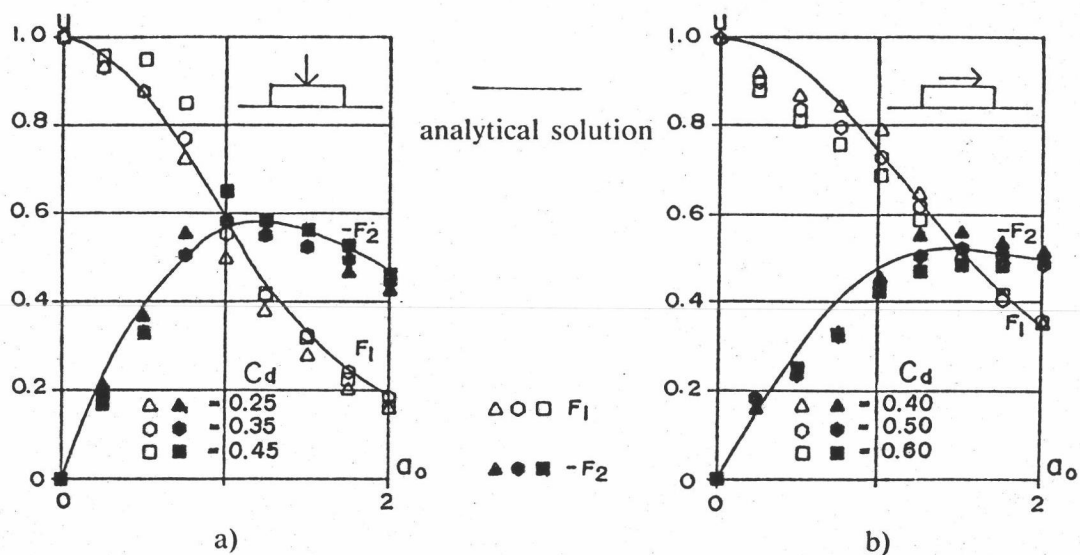


FIGURE 3.9 Parametric study on the variations of C_d while keeping C_m and C_s constant

a) $C_m = 0.55, C_s = 0.026$

b) $C_m = 0.50, C_s = 0.042$

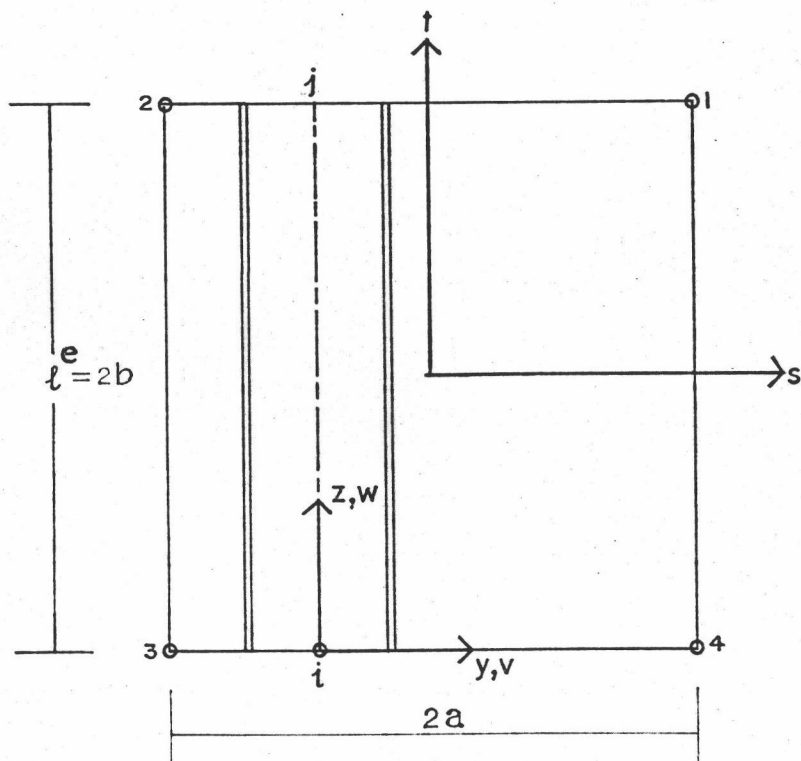


FIGURE 4.1 Typical soil-pile element

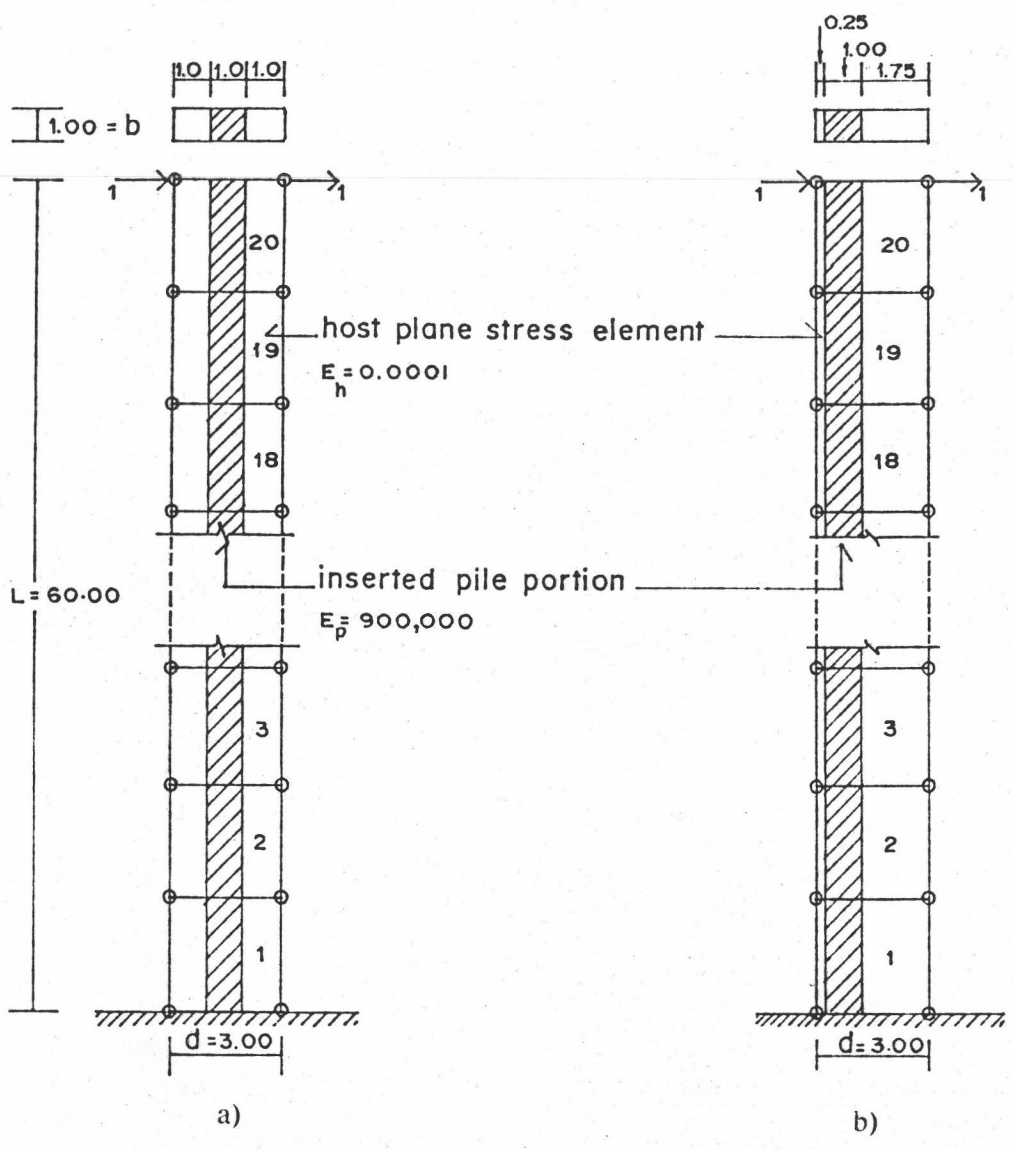


FIGURE 4.2 Cantilever beams using plane stress finite element model with inserted piles.

- a) concentric pile
- b) eccentric pile

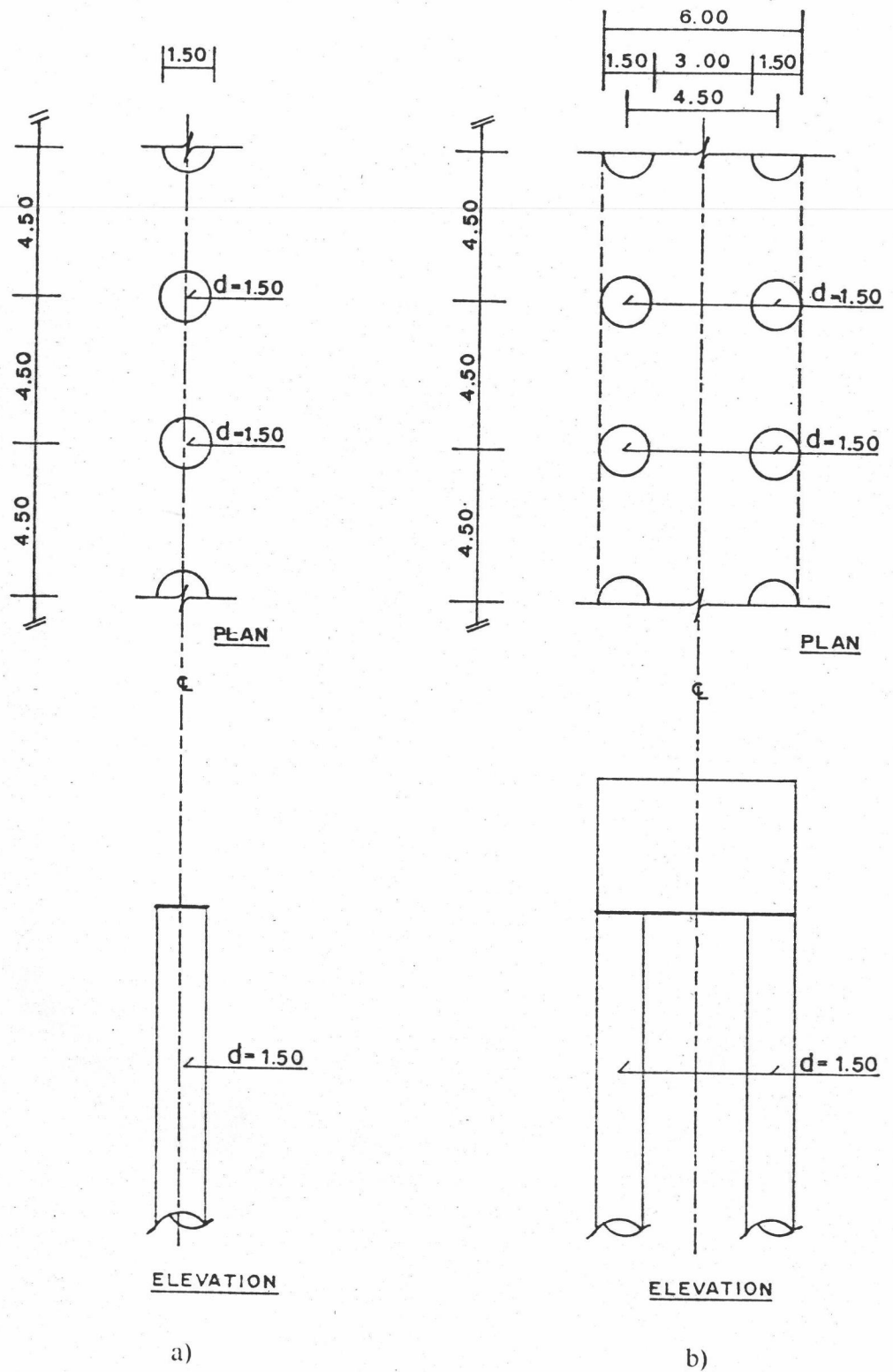


FIGURE 5.1 Pile configurations in the plane strain model
 a) single-line piles b) two-line piles

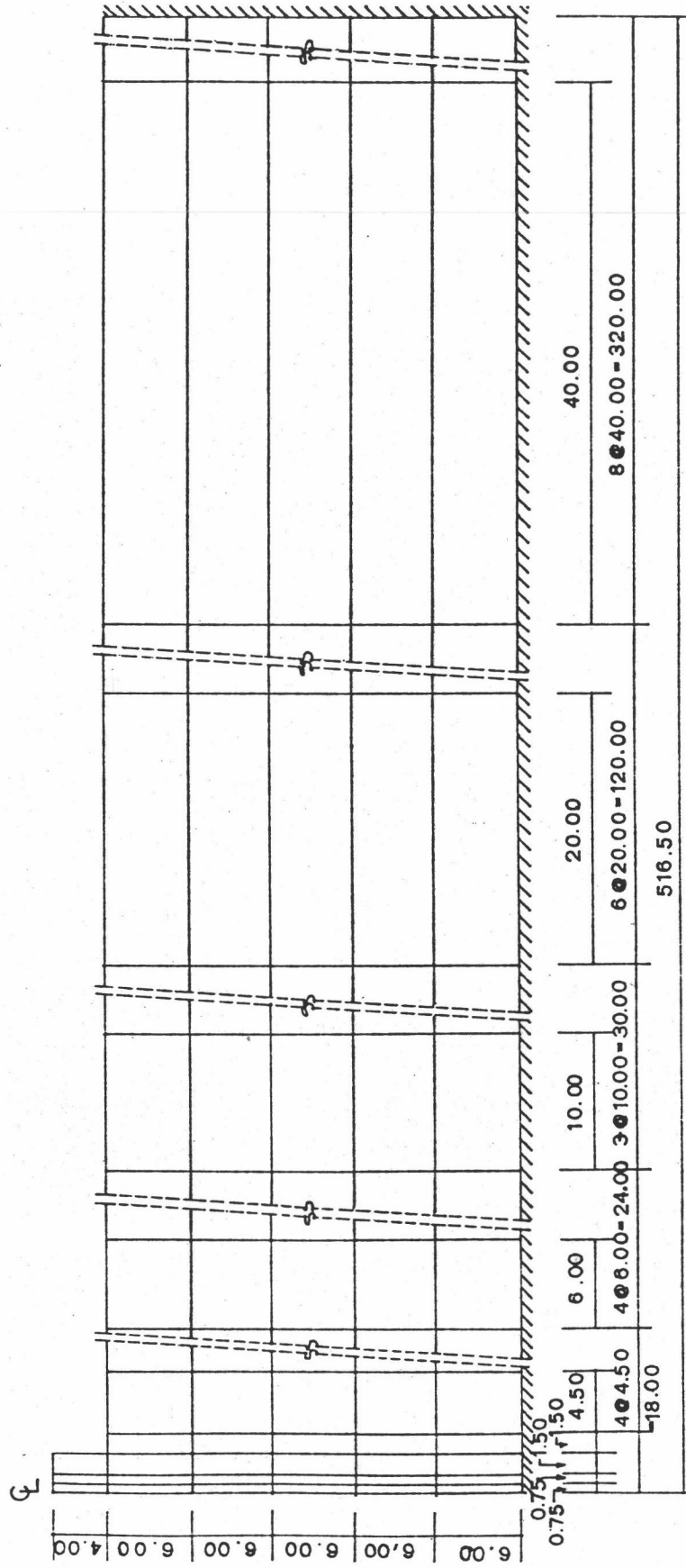


FIGURE 5.2 Finer model of finite element mesh

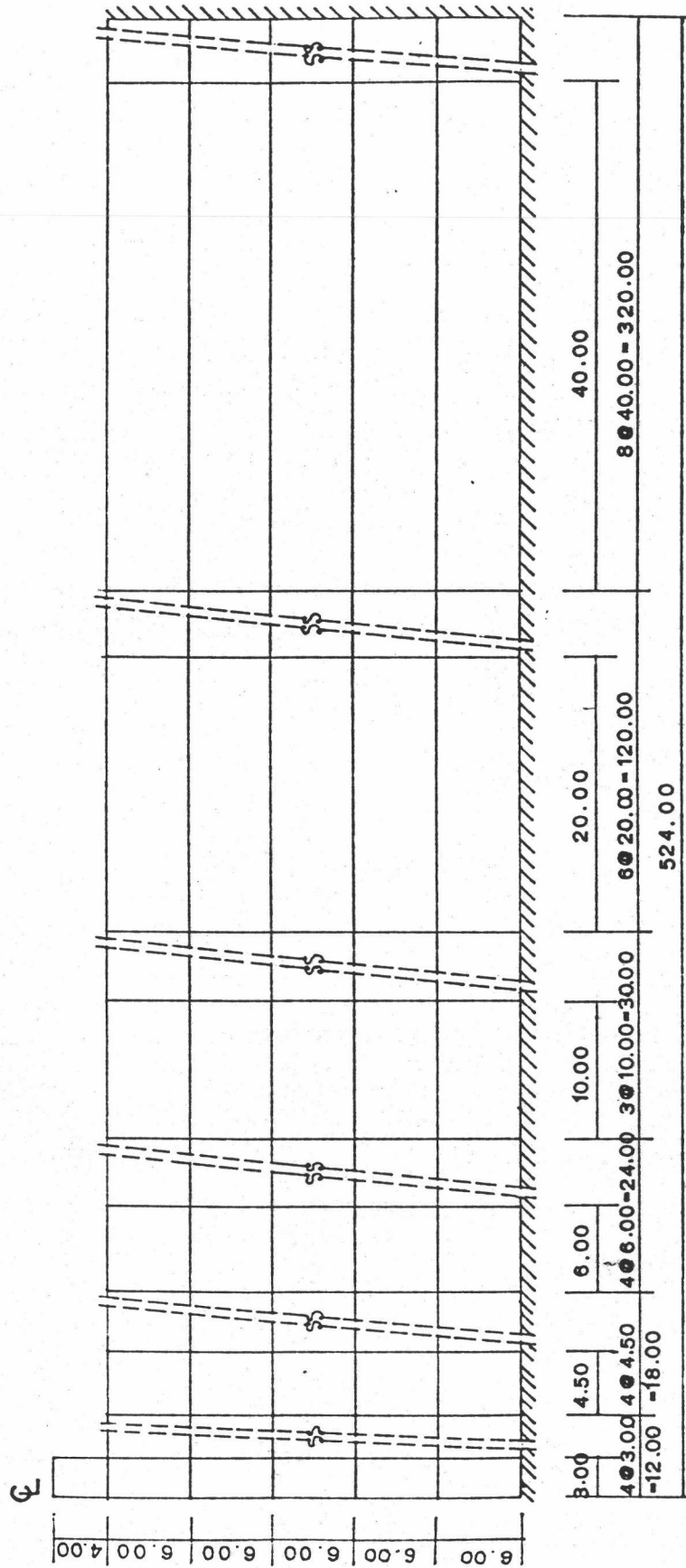
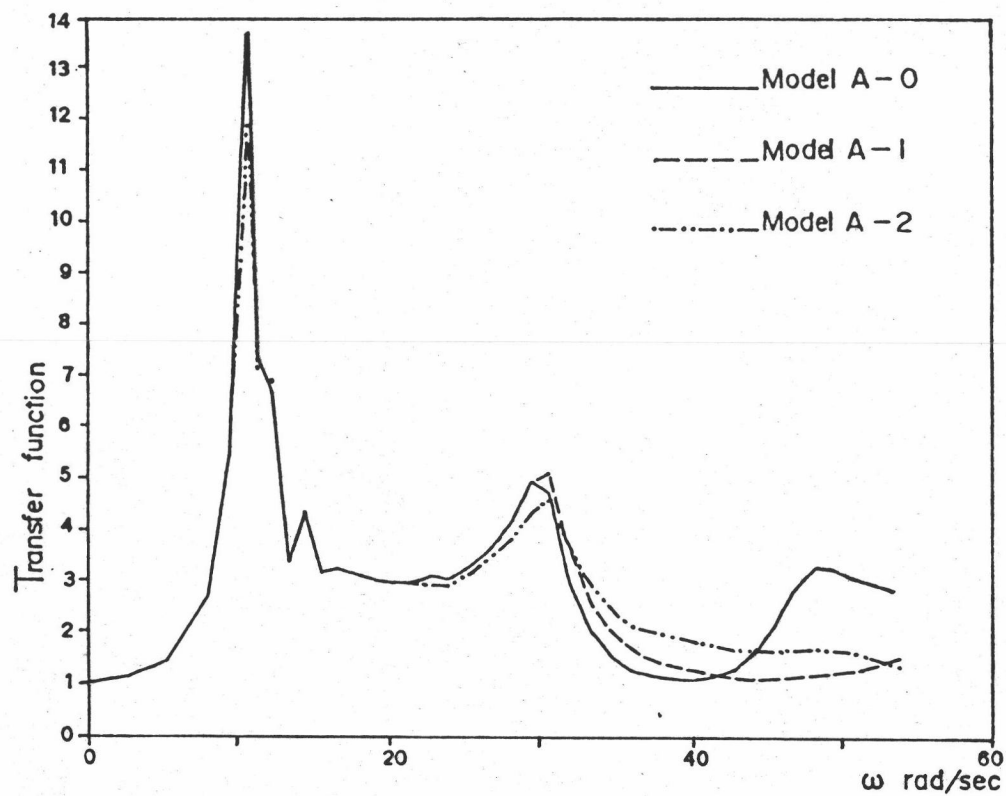
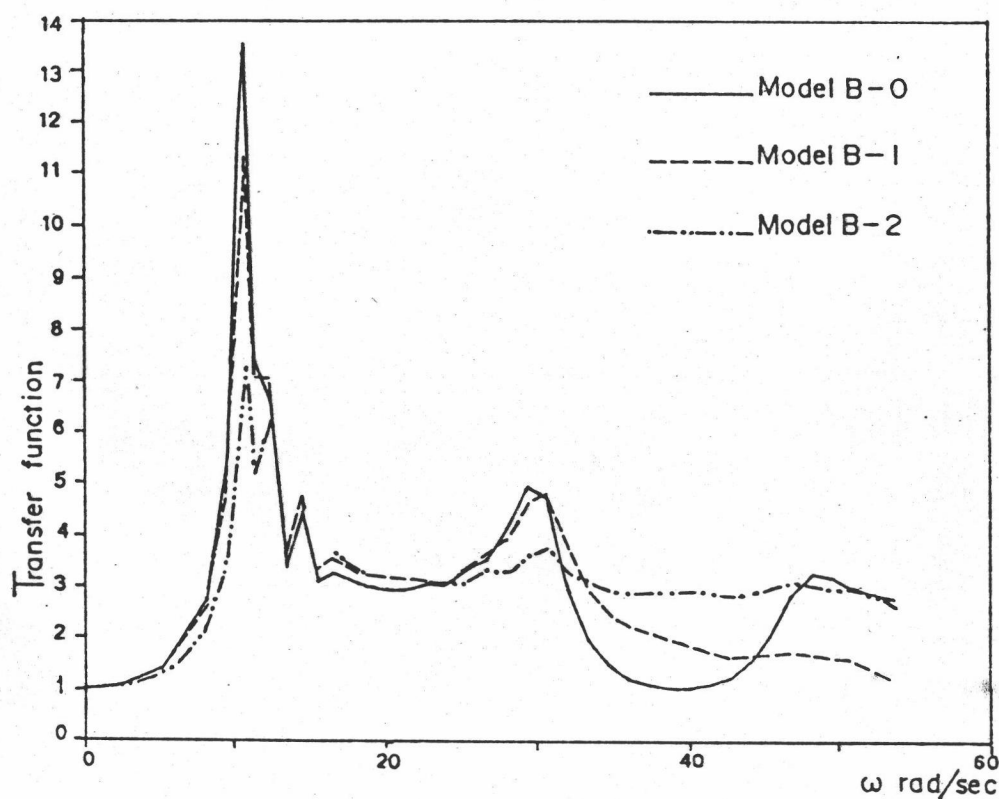


FIGURE 5.3 Coarser model of finite element mesh



a)



b)

FIGURE 5.4 Acceleration transfer functions a) finer models b) coarser models

APPENDIX

APPENDIX

Element Stiffness of Two-dimensional Plane Strain Element

As described in the introductory chapter, the two-dimensional plane strain model is used as the host soil element for the soil-pile element. Derivation of the plane strain element stiffness is simple and normally appears as an example in most finite element text books. The following presentation on plane strain element stiffness is to review the basic concept and to use the pertinent quantities as the basis in derivation of the soil-pile element stiffness.

Since the soil mass is a large medium and only the global effect on the super-structure due to soil is required, modeling of the soil element in the shape of simple rectangular with four corner nodes as shown in Fig. 4.1 is adequate and widely adopted.

For isoparametric elements, both the spatial coordinates and the displacement fields of any point within the element can be expressed by the same interpolation functions; thus we have

$$y(s, t) = \sum_{i=1}^4 N_i^e(s, t) \cdot y_i \quad (\text{A.1a})$$

$$z(s, t) = \sum_{i=1}^4 N_i^e(s, t) \cdot z_i \quad (\text{A.1b})$$

and

$$v(s, t) = \sum_{i=1}^4 N_i^e(s, t) \cdot v_i \quad (\text{A.2a})$$

$$w(s, t) = \sum_{i=1}^4 N_i^e(s, t) \cdot w_i \quad (\text{A.2b})$$

The local shape functions of the four-node two-dimensional rectangular element are in the form

$$N_1^e(s, t) = \frac{1}{4} (1+s) (1+t) \quad (\text{A.3a})$$

$$N_2^e(s, t) = \frac{1}{4} (1-s) (1+t) \quad (\text{A.3b})$$

$$N_3^e(s, t) = \frac{1}{4} (1-s) (1-t) \quad (\text{A.3c})$$

$$N_4^e(s, t) = \frac{1}{4} (1+s) (1-t) \quad (\text{A.3d})$$

The strain energy U_s , already derived in Chapter 2 and appears as the first term on the right hand side of Eq.(2.17), is

$$U_s = \sum_e \frac{1}{2} \int_{\Omega^e} \{q\}^T [B^e]^T [D^e] [B^e] \{q\} d\Omega^e \quad (\text{A.4})$$

in which $\{q\}$, the vector of generalized displacement defined by Eq.(2.10), is taken as the nodal point displacements :

$$\begin{Bmatrix} v \\ w \end{Bmatrix} = \sum_{i=1}^4 \begin{bmatrix} N_i^e & 0 \\ 0 & N_i^e \end{bmatrix} \begin{Bmatrix} v_i \\ w_i \end{Bmatrix} = [N^e] \{q\} ; \quad (\text{A.5})$$

$$[B^e] = [B_1^e, B_2^e, B_3^e, B_4^e] \quad (\text{A.6})$$

in which

$$[B_i^e] = \begin{bmatrix} \frac{\partial N_i^e}{\partial y} & 0 \\ 0 & \frac{\partial N_i^e}{\partial z} \\ \frac{\partial N_i^e}{\partial z} & \frac{\partial N_i^e}{\partial y} \end{bmatrix} \quad (\text{A.7})$$

and

$$[D^e] = \frac{E(1-\nu)}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1 & \frac{\nu}{1-\nu} & 0 \\ \frac{\nu}{1-\nu} & 1 & 0 \\ 0 & 0 & \frac{1-2\nu}{2(1-\nu)} \end{bmatrix} \quad (\text{A.8})$$

where E is the modulus of elasticity and ν is the Poisson's ratio.

Formulation of element stiffness matrix follows as described in Chapter 2.

In view of Eq. (2.22), we have

$$[K^e] = \int_{\Omega^e} [B^e]^T [D^e] [B^e] d\Omega^e \quad (\text{A.9})$$

To find the shape function derivatives appearing in Eq.(A.7), we begin with the basic mathematical concepts. Since the transformation from the global x, y to the local s, t is assumed to be one-to-one mapping, any shape function, N_i , can be expressed in terms of both coordinates. We can write, using the chain rule, the shape function derivatives as

$$\begin{pmatrix} \frac{\partial N_i}{\partial s} \\ \frac{\partial N_i}{\partial t} \end{pmatrix} = \begin{bmatrix} \frac{\partial y}{\partial s} & \frac{\partial z}{\partial s} \\ \frac{\partial y}{\partial t} & \frac{\partial z}{\partial t} \end{bmatrix} \begin{pmatrix} \frac{\partial N_i}{\partial y} \\ \frac{\partial N_i}{\partial z} \end{pmatrix} \quad (\text{A.10})$$

where $\begin{bmatrix} \frac{\partial y}{\partial s} & \frac{\partial z}{\partial s} \\ \frac{\partial y}{\partial t} & \frac{\partial z}{\partial t} \end{bmatrix}$ is called the Jacobian matrix $[J]$.

Each term in the Jacobian matrix can be evaluated by differentiating Eqs. (A.1); $\frac{\partial N_i}{\partial s}$ and $\frac{\partial N_i}{\partial t}$ are obtained by differentiation of Eqs. (A.3). Then $\frac{\partial N_i}{\partial y}$ and $\frac{\partial N_i}{\partial z}$ can be solved by matrix inversion of Eq. (A.10). Integration of element stiffness in Eq. (A.9) can be performed on the local coordinate domain by using the relation from elementary calculus :

$$d\Omega^e = \det [J] t ds dt \quad (\text{A.11})$$

where $\det [J]$ is the determinant of the Jacobian matrix; t is the thickness of the two-dimensional element in the direction perpendicular to the $y-z$ plane.

Substituting $d\Omega^e$ from Eq. (A.11) into Eq. (A.9) yields

$$[K^e] = \int_{-1}^1 \int_{-1}^1 [B^e]^T [D^e] [B^e] \det [J] t ds dt \quad (\text{A.12})$$

An appropriate numerical procedure can be adopted in the evaluation of $[K^e]$ in Eq. (A.12).



VITA

Mr. Suriya Thusneeyanont was born on January 17, 1952 in Rajburi. He graduated from Suankularb College in 1970. He entered Chulalongkorn University and received B.Eng. and M.Eng. in Civil Engineering from Chulalongkorn University in 1975 and 1981, respectively. After four years of teaching at Nakhonsawan Technical College, Department of Vocational Education, he enrolled in a D.Eng. program at Chulalongkorn University.