

REFERENCES

- Newton, C. and Chen, C. (1980). Second law analysis in cryogenic process. Energy Volume: 5, pp. 899-904.
- Kanoğlu, M. (2002). Exergy analysis of multistage cascade refrigeration cycle used for natural gas liquefaction. International Journal of Energy Research, 26, 763-774
- Remeljej, C.W. and Hoadley, A.F.A. (2004). An exergy analysis of small-scale liquefied natural gas liquefaction processes. Energy, 31, 2005-2019.
- Gundersen, T., Aspelund, A. and Barton, P. (2009). An Overall of New Methodologies for the Design of Cryogenic process with an emphasis on LNG. Proceedings of the 1st Annual Gas Processing Symposium, 104-112.
- Dhole, V.R. and Linnhoff, B. (1994). Overall Design of Low Temperature Processes. Computers Chemical Engineering, 18, S105-S111.
- Marmolejo-Correa, D. and Gundersen, T. (2012). A comparison of exergy efficiency definitions with focus on low temperature processes. Energy, 44, 477-489.
- Aspelund, A., Gundersen, T., Myklebust, J., Nowak, M.P. and Tomaszard, A. (2009). An optimization-simulation model for a simple LNG process. Computers and Chemical Engineering, 34, 1606-1617.
- Alabdulkarem, A., Mortazavi, A., Hwang, Y., Radermacher, R. and Rogers, P. (2011). Optimization of propane pre-cooled mixed refrigerant LNG plant. Applied Thermal Engineering, 31, 091-1098.
- Aspelund, A. and Gundersen, T. (2007). A new Process Synthesis Methodology utilizing Pressure Exergy in Subambient Processes. Procedding of the 17th European Symposium on Computer Aided Process Engineering, 24, 1133-1138.
- Mahabadipour, H. and Gharbi, H. (2013). Development and comparison of two expander cycles used in refrigeration system of olefin plant based on exergy analysis. Applied Thermal Engineering, 50, 771-780.

- Vidal, A., Best, R., Rivero, R. and Cervantes, J. (2006). Analysis of a combined power and refrigeration cycle by the exergy method. Energy, 31, 3401-3414.
- Marmolejo-Correa, D. and Gundersen, T. (2013). New Graphical Representation of Exergy Applied to Low Temperature Process Design. Industrial and Engineering Chemistry Research, 52, 7145-7156.
- Marmolejo-Correa, D. and Gundersen, T. (2012). A new procedure for the design of LNG processes by combining Exergy and Pinch Analyses. Proceeding of the 25TH International Conference on Efficiency, Cost, Optimization, Simulation and Environmental Impact of Energy Systems, Perugia, Italy.
- Marmolejo-Correa, D. and Gundersen, T. (2012). A new graphical representation of exergy applied to low temperature process design. Proceeding of the 11TH International Symposium on Process Systems Engineering, 2, 1180-1184, DOI: 10.1016/B978-0-444-59506-5.50067-5.
- Marmolejo-Correa, D. and Gundersen, T. (2012). A new graphical exergy targeting representation for processes operating above and below ambient temperature. Proceeding of the 22nd European Symposium on Computer Aided Process Engineering, London, UK, 557-561.
- Marmolejo-Correa, D. and Gundersen, T. (2011). Low Temperature Process Design: Challenges and Approaches for using Exergy Efficiencies. Proceeding of the 21st European Symposium on Computer Aided Process Engineering, 2, 1909-1913, DOI: 10.1016/B978-0-444-54298-4.50160-4.
- Aspelund, A., Berstad, D.O., Gundersen, T. (2007). An Extended Pinch Analysis and Design procedure utilizing pressure based exergy for subambient cooling. Applied Thermal Engineering, 27(16), 2633-2649.
- Linnhoff, B. and Dhole, V.R. (1992). Shaftwork targets for low-temperature process design. Chemical Engineering Science, 47(8), 2081-2091.
- Yee, T.F., and Grossmann, I.E. (1990). Simultaneous optimization models for heat integration. II. Heat exchanger network synthesis. Computers and Chemical Engineering, 14(10), 1165-1184.

- Linnhoff, B., Townsend, D.W., Boland, D., Hewitt, G.F., Thomas, B.E.A., Guy, A.R. and Marsland, R.H. (1982). A User Guide on Process Integration for the Efficient Use of Energy. The Institution of Chemical Engineers, Rugby.
- Hackl, R. and Harvey, S. (2012). Total Site Analysis (TSA) and Exergy Analysis for Shaft Work and Associated Steam and Electricity Savings in Low Temperature Processes in Industrial Clusters. Chemical Engineering Transactions, 29, 73-78, DOI: 10.3303/CET1229013.
- Pereira, C. and Lequisiga, D. (2014). Technical Evaluation of C₃-MR and Cascade Cycle on Natural Gas Liquefaction Process. International Journal of Chemical Engineering and Applications, 5, 451-456, DOI: 10.7763/IJCEA.2014.V5.427.

APPENDICES

Appendix A HEN Synthesis

SETS

I hot streams

/H1,H2,H3,H4,H5,H6,H7,H8,H9,H10,H11,H12,H13,H14,H15,H16,H17,H18/

J cold streams / C1,C2,C3,C4,C5,C6,C7,C8,C9 /

K location / firstlocation,location2*location26,lastlocation /

CU cold utility / CU1,CU2,CU3,CU4,CU5,CU6,CU7,CU8,CU9,CU10/

;

SCALARS

OMEGA upper bound for heat exchange /999999/

GAMMA upper bound for temperature difference /999999/

EMAT exchanger minimum approach temperature /3/

CHU unit cost for hot utility /1000/

CF fixed charge for exchangers /99000/

CW unit cost for power consumption /200000/

PARAMETERS

TOUTH(I) outlet temperature of cold stream

/ H1 271.634

 H2 249.582

 H3 236.977

 H4 207.45

 H5 186.17

 H6 183.036

 H7 148.15

 H8 129.446

 H9 118.15

H10 298.58

H11 271.79

H12 249.58

H13 237.15

H14 207.416

H15 186.214

H16 182.579

H17 147.941

H18 129.501 /

TINC(J) inlet temperature of cold stream

/ C1 268.793

C2 246.57

C3 234.198

C4 204.446

C5 183.188

C6 179.915

C7 144.942

C8 126.521

C9 111.587 /

TOUTC(J) outlet temperature of cold stream

/ C1 269.293

C2 247.07

C3 234.698

C4 204.946

C5 183.688

C6 180.415

C7 145.442

C8 127.021

C9 112.087 /

FH(I) heat capacity of hot stream

/ H1 263.3583

H2 272.9911

H3	286.2356
H4	351.4749
H5	1480.733
H6	1276.324
H7	461.5032
H8	374.2515
H9	354.1076
H10	22399
H11	13446.61
H12	12558.84
H13	3152.466
H14	2504.468
H15	2901.974
H16	1036.471
H17	410.6263
H18	149.4232

FC(J) heat capacity of cold stream

/	C1	396200
	C2	320063
	C3	258800
	C4	221200
	C5	172800
	C6	65600
	C7	62400
	C8	23300
	C9	7830

FW(I,J) heat capacity of work

TCUIN(CU) inlet temperature of cold utility

/	CU1	295
	CU2	268
	CU3	246

CU4 234

CU5 204

CU6 183

CU7 180

CU8 145

CU9 127

CU10 111 /

TCUOUT(CU) outlet temperature of cold utility

/ CU1 300

CU2 269

CU3 247

CU4 235

CU5 205

CU6 184

CU7 181

CU8 146

CU9 128

CU10 112 /

CCU(CU) unit cost for cold utility

/ CU1 22

CU2 140

CU3 160

CU4 180

CU5 300

CU6 400

CU7 450

CU8 500

CU9 600

CU10 700 /

;

FW(I,J)=0;

FW('H10','C1') = 851.636;

$FW('H11','C2') = 621.772;$
 $FW('H12','C3') = 450.434;$
 $FW('H13','C4') = 388.078;$
 $FW('H14','C5') = 263.583;$
 $FW('H15','C6') = 88.14;$
 $FW('H16','C7') = 230.15;$
 $FW('H17','C8') = 55.29;$
 $FW('H18','C9') = 21.027;$

VARIABLES

TINH(I)	inlet temperature of hot stream
O	objective function
W	Shaft Work Requirement
;	

POSITIVE VARIABLES

dt(I,J,K)	temperature approach for match ij at the left of stage k
dtcu(I,CU)	temperature approach for match hot stream i and cold utility
dthu(J)	temperature approach for match cold stream j and hot utility
q(I,J,K)	heat exchanged between hot stream i and cold stream j at stage k
qcu(I,CU)	heat exchanged between hot stream i and cold utility
qhu(J)	heat exchanged between cold stream j and hot utility
tH(I,K)	temperature of hot stream i at location k
tC(J,K)	temperature of cold stream j at location k
;	

BINARY VARIABLE

z(I,J,K)	Binary variable of HEX Process to Process
zcu(I,CU)	Binary variable of cold utility
zhu(J)	Binary variable of hot utility
;	

TINH.fx('H1') = 303.15;
TINH.fx('H2') = 271.634;
TINH.fx('H3') = 249.582;
TINH.fx('H4') = 236.977;
TINH.fx('H5') = 207.45;
TINH.fx('H6') = 186.17;
TINH.fx('H7') = 183.036;
TINH.fx('H8') = 148.15;
TINH.fx('H9') = 129.446;

TINH.lo('H10') = 299;
TINH.lo('H11') = 272;
TINH.lo('H12') = 250;
TINH.lo('H13') = 240;
TINH.lo('H14') = 208;
TINH.lo('H15') = 187;
TINH.lo('H16') = 183;
TINH.lo('H17') = 148;
TINH.lo('H18') = 130;

TINH.up('H10') = 308.951;
TINH.up('H11') = 285.491;
TINH.up('H12') = 260.839;
TINH.up('H13') = 281.75;
TINH.up('H14') = 248.822;
TINH.up('H15') = 198.068;
TINH.up('H16') = 232.016;
TINH.up('H17') = 184.059;
TINH.up('H18') = 162.963;

EQUATIONS

OHB_H(I)	overall heat balance for each hot stream
OHB_C(J)	overall heat balance for each cold stream
SHB_H(I,K)	heat balance at each stage for hot stream
SHB_C(J,K)	heat balance at each stage for cold stream
TINHASSGN(I)	assignment of inlet temperature of hot stream i
TINCASSGN(J)	assignment of inlet temperature of cold stream j
FH1(I,K)	feasibility of temperature at each stage for hot stream
FH2(I)	feasibility of temperature at last stage for hot stream
FC1(J,K)	feasibility of temperature at each stage for cold stream
FC2(J)	feasibility of temperature at first stage for cold stream
HULOAD(I)	hot utility load
CULOAD(J)	cold utility load
HECOUNT1(I,J,K)	count heat exchanger
HECOUNT2(I,CU)	count hot utility
HECOUNT3(J)	count cold utility
APPTEMPL(I,J,K)	approach temperature at the left of stage k
APPTEMPR(I,J,K)	approach temperature at the right of stage k
APPTEMPCU(I,CU)	approach temperature at cold utility of hot stream i
APPTEMPHU(J)	approach temperature at hot utility of cold stream j
APPTEMPLIMIT(I,J,K)	limiting temperature approach
APPTEMPCUMIN (I,CU)	approach temperature at cold utility
CONSTMATCH	define match of cold utility
CONSTMATCHC	define match of hot utility
OBJFN	objective function
SHAFTWORK	shaft work requirement

* Overall Energy balance.....

OHB_H(I) .. (TINH(I)-TOUTH(I))*FH(I) =e=

SUM((J,K),q(I,J,K))+SUM(CU,qcu(I,CU));

OHB_C(J) .. (TOUTC(J)-TINC(J))*FC(J) =e= SUM((I,K),q(I,J,K))+qhu(J);

* Heat balance at each stage.....

```
SHB_H(I,K)$(ORD(K) NE CARD(K)) .. (tH(I,K)-tH(I,K+1))*FH(I) =e=
SUM(J,q(I,J,K));
SHB_C(J,K)$(ORD(K) NE CARD(K)) .. (tC(J,K)-tC(J,K+1))*FC(J) =e=
SUM(I,q(I,J,K));
```

* Assignment Temperature.....

```
TINHASSGN(I) .. TINH(I) =e= tH(I,'firstlocation');
TINCASSGN(J) .. TINC(J) =e= tC(J,'lastlocation');
```

* Feasible Temperature.....

```
FH1(I,K)$(ORD(K) NE CARD(K)) .. tH(I,K) =g= tH(I,K+1);
FH2(I) .. TOUTH(I) =l= tH(I,'lastlocation');
FC1(J,K)$(ORD(K) NE CARD(K)) .. tC(J,K) =g= tC(J,K+1);
FC2(J) .. TOUTC(J) =g= tC(J,'firstlocation');
```

* Heat&Cold utility.....

```
HULOAD(I) .. (tH(I,'lastlocation')-TOUTH(I))*FH(I) =e= SUM(CU,qcu(I,CU));
CULQAD(J) .. (TOUTC(J)-tC(J,'firstlocation'))*FC(J) =e= qhu(J);
```

* Counting existing heat exchanger at each stage.....

```
HECOUNT1(I,J,K)$(ORD(K) NE CARD(K)) .. q(I,J,K)-OMEGA*z(I,J,K) =l= 0;
HECOUNT2(I,CU).. qcu(I,CU)-OMEGA*zcu(I,CU) =l= 0;
HECOUNT3(J) .. qhu(J)-OMEGA*zhu(J) =l= 0;
```

* Calculation of approach temperature.....

```
APPTEMPL(I,J,K)$(ORD(K) NE CARD(K)) .. dt(I,J,K) =l= tH(I,K)-
tC(J,K)+GAMMA*(1-z(I,J,K));
APPTEMPR(I,J,K)$(ORD(K) NE CARD(K)) .. dt(I,J,K+1) =l= tH(I,K+1)-
tC(J,K+1)+GAMMA*(1-z(I,J,K));
```

```

APPTEMPCU(I,CU)..          dtcu(I,CU)      =l=      tH(I,'lastlocation')-
TCUOUT(CU)+GAMMA*(1-zcu(I,CU));
APPTEMPHU(J) .. dthu(J) =l= TOUTC(J)- tC(J,'firstlocation')+GAMMA*(1-
zhu(J));
APPTEMLIMIT(I,J,K$(ORD(K) NE CARD(K)) .. dt(I,J,K)=g= EMAT;
APPTEMPCUMIN (I,CU) .. dtcu(I,CU) =g= EMAT;
CONSTMATCH.. SUM((I,CU),zcu(I,CU)) =l= 2;
CONSTMATCHC.. SUM((J),zhu(J)) =l= 0;

```

* Objective Function.....

```

OBJFN .. O =e=
SUM((I,CU),CCU(CU)*qcu(I,CU))+CHU*SUM(J,qhu(J))+CF*SUM((I,J,K),z(I,J,K
))+SUM((I,CU),CF*zcu(I,CU))+CF*SUM(J,zhu(J))+
CW*SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J)));
SHAFTWORK .. W =e= SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J))) ;
;
MODEL STAGEMODEL SYNHEAT model /ALL/ ;
SOLVE STAGEMODEL USING MIP MINIMISING O;
DISPLAY z.l,zcu.l,zhu.l,tH.l,tC.l,q.l,qcu.l,qhu.l,O.l,W.l,FW;
```

**Appendix B The Multistage Cascade Refrigeration of LNG Process
Flowsheet and Stream Condition in PROII**

Table B1 The base case condition of multistage cascade refrigeration of LNG process

	T_s (°C)	T_t (°C)	P_s (atm)	P_t (atm)	F (kg/s)
H11	12.34	-1.36	4.48	4.48	458.692
H12	8.6	-1.36	16.5	16.5	332.718
H13	30	-1.52	39.47	39.47	108.733
H14	35.8	25.43	9.5	9.5	652.143
H21	-12.31	-23.57	2.12	2.12	334.604
H22	-1.36	-23.63	16.5	16.5	332.718
H23	-1.52	-23.57	39.47	39.47	108.733
H31	-23.63	-36	16.5	16.5	332.718
H32	-24.33	-35.57	6.02	6.02	216.771
H33	-23.57	-36.17	39.47	39.47	108.733
H41	-35.57	-65.73	6.02	6.02	216.771
H42	-36.17	-65.7	39.47	39.47	108.733
H51	-75.08	-86.94	2.454	2.454	73.108
H52	-41.13	-86.9	35.5	35.5	136.283
H53	-65.7	-86.98	39.47	39.47	108.733
H61	-86.9	-90.57	35.5	35.5	136.283
H62	-86.98	-90.11	39.47	39.47	108.733
H71	-89.09	-125.21	9.402	9.402	29.39
H72	-110.19	-125	3.536	3.536	9.16
H73	-90.11	-125	39.47	39.47	108.733
H81	-125	-143.65	3.536	3.536	9.16
H82	-125	-143.7	39.47	39.47	108.733
H91	-143.7	-155	39.47	39.47	108.733
C1	-4.36	-4.36	4.08	4.08	652.143
C2	-26.58	-26.58	1.89	1.89	458.692
C3	-38.95	-38.95	1.15	1.15	334.604
C4	-68.7	-68.7	5.37	5.37	332.718
C5	-89.96	-89.9	2.12	2.12	216.771
C6	-93.24	-93.24	1.8	1.8	73.108
C7	-128.21	-128.21	8.15	8.15	136.283
C8	-146.63	-146.6	2.94	2.94	29.39
C9	-161.56	-161.56	1	1	9.16

Table B2 The condition of multistage cascade refrigeration of LNG process from result of Shaft work targeting technique

	T_s (°C)	T_t (°C)	P_s (atm)	P_t (atm)	F (kg/s)
H11	12.351	-1.373	4.48	4.48	425.756
H12	9.858	-1.36	16.5	16.5	307.808
H13	30	-1.36	39.47	39.47	108.733
H14	36.204	25.43	9.5	9.5	607.524
H21	-12.301	-23.563	2.12	2.12	309.773
H22	-1.36	-23.56	16.5	16.5	307.808
H23	-1.36	-23.55	39.47	39.47	108.733
H31	-23.56	-35.269	16.5	16.5	307.808
H32	-22.799	-36	6.02	6.02	198.524
H33	-23.55	-36	39.47	39.47	108.733
H41	-36	-65.734	6.02	6.02	198.524
H42	-36	-65.7	39.47	39.47	108.733
H51	-50.197	-86.936	2.454	2.454	84.691
H52	-64.411	-86.9	25	25	84.346
H53	-65.7	-86.93	39.47	39.47	108.733
H61	-86.9	-101.024	25	25	84.346
H62	-86.93	-101	39.47	39.47	108.733
H71	-89.117	-125.21	9.402	9.402	29.393
H72	-115.271	-125	3.536	3.536	9.043
H73	-101	-125	39.47	39.47	108.733
H81	-125	-143.66	3.536	3.536	9.043
H82	-125	-143.6	39.47	39.47	108.733
H91	-143.6	-155	39.47	39.47	108.733
C1	-4.36	-4.35	4.08	4.08	607.524
C2	-26.58	-26.57	1.89	1.89	425.756
C3	-38.95	-38.94	1.15	1.15	309.773
C4	-68.7	-68.7	5.37	5.37	307.808
C5	-89.96	-89.95	2.12	2.12	198.524
C6	-104.028	-104.018	1	1	84.691
C7	-128.208	-128.198	8.15	8.15	84.346
C8	-146.63	-146.62	2.94	2.94	29.393
C9	-157.981	-157.98	1.33	1.33	9.043

Table B3 The condition of multistage cascade refrigeration of LNG process from result of the Extended Pinch Analysis and Design Methodology and novel exergy diagram

	T _s	T _t	P _s	P _t	F
	(°C)	(°C)	(atm)	(atm)	(kg/s)
H11	12.351	-1.363	4.48	4.48	407.099
H12	0.674	-1.36	14.78	14.78	275.825
H13	30	-1.516	39.47	39.47	108.733
H14	35.932	25.43	9.5	9.5	561.128
H21	-9.612	-23.563	2.12	2.12	297.343
H22	-1.36	-23.681	14.78	14.78	275.825
H23	-1.516	-23.568	39.47	39.47	108.733
H31	-23.681	-39.011	14.78	14.78	275.825
H32	-23.906	-40.219	6.02	6.02	189.251
H33	-23.568	-38.882	39.47	39.47	108.733
H41	-40.219	-65.724	6.02	6.02	189.251
H42	-38.882	-65.7	39.47	39.47	108.733
H51	-50.286	-86.936	2.45	2.45	79.392
H52	-65.443	-86.9	25	25	77.968
H53	-65.7	-86.988	39.47	39.47	108.733
H61	-86.9	-101.024	25	25	77.968
H62	-86.988	-101.181	39.47	39.47	108.733
H71	-89.122	-125.21	9.402	9.402	27.722
H72	-121.905	-125	3.536	3.536	8.086
H73	-101.181	-125	39.47	39.47	108.733
H81	-125	-144.515	3.536	3.536	8.086
H82	-125	-143.704	39.47	39.47	108.733
H91	-143.704	-155.325	39.47	2.2	108.733
C1	-4.36	-4.36	4.08	4.08	561.128
C2	-26.58	-26.58	1.89	1.89	407.099
C3	-42.19	-42.19	1	1	297.343
C4	-68.7	-68.7	5.37	5.37	275.825
C5	-89.96	-89.96	2.12	2.12	189.251
C6	-104.028	-104.028	1	1	79.392
C7	-128.208	-128.208	8.15	8.15	77.968
C8	-146.63	-146.63	2.94	2.94	27.722
C9	-157.032	-157.032	1.43	1.43	8.086

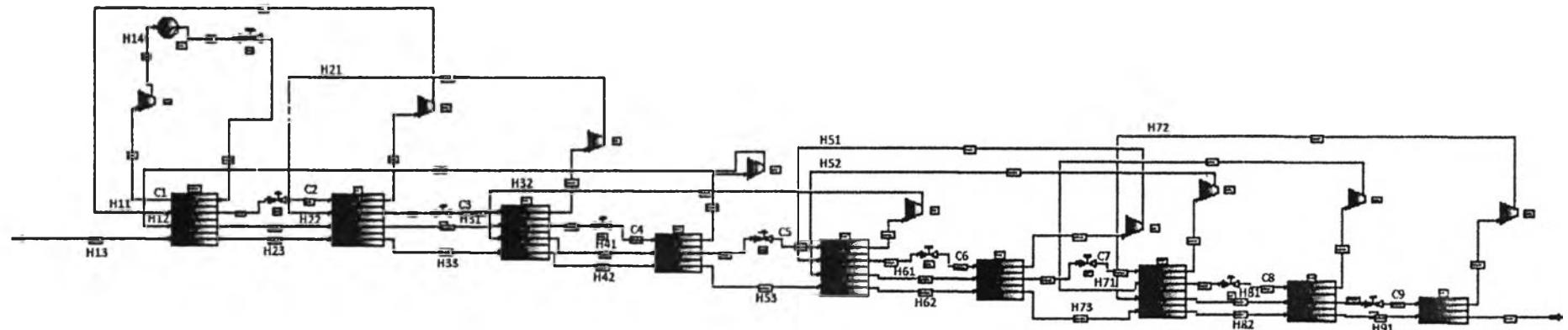


Figure B1 The multistage cascade refrigeration of LNG process in PROII.

Appendix C HEN Retrofit

Model of HEN Retrofit for Case 1 (new exchangers ≥ 20)

SETS

```

I      hot streams /H1,H2,H3,H4,H5,H6,H7,H8,H9,H10,H11,H12,H13,H14,H15,H16,H17,H18/
J      cold streams / C1,C2,C3,C4,C5,C6,C7,C8,C9 /
K      location / firstlocation,location2*location26,lastlocation /
CU     cold utility / CU1,CU2,CU3,CU4,CU5,CU6,CU7,CU8,CU9,CU10/
;
```

SCALARS

OMEGA	upper bound for heat exchange /999999/
GAMMA	upper bound for temperature difference /999999/
EMAT	exchanger minimum approach temperature /3/
CHU	unit cost for hot utility /1000/
CF	fixed charge for exchangers /99000000/
CW	unit cost for power consumption /200000/

PARAMETERS

TOUTH(I) outlet temperature of cold stream

/	H1 271.634
	H2 249.582
	H3 236.977
	H4 207.45
	H5 186.17
	H6 183.036
	H7 148.15
	H8 129.446
	H9 118.15

H10 298.58

H11 271.79

H12 249.58

H13 237.15

H14 207.416

H15 186.214

H16 182.579

H17 147.941

H18 129.501 /

TINC(J) inlet temperature of cold stream

/ C1 268.793

C2 246.57

C3 234.198

C4 204.446

C5 183.188

C6 179.915

C7 144.942

C8 126.521

C9 111.587 /

TOUTC(J) outlet temperature of cold stream

/ C1 269.293

C2 247.07

C3 234.698

C4 204.946

C5 183.688

C6 180.415

C7 145.442

C8 127.021

C9 112.087 /

FH(I) heat capacity of hot stream

/ H1 263.3583

H2 272.9911

H3 286.2356

H4 351.4749

H5 1480.733

H6 1276.324

H7 461.5032

H8 374.2515

H9 354.1076

H10 22399

H11 13446.61

H12 12558.84

H13 3152.466

H14 2504.468

H15 2901.974

H16 1036.471

H17 410.6263

H18 149.4232 /

FC(J) heat capacity of cold stream

/ C1 396200

C2 320063

C3 258800

C4 221200

C5 172800

C6 65600

C7 62400

C8 23300

C9 7830 /

FW(I,J) heat capacity of work

TCUIN(CU) inlet temperature of cold utility

/ CU1 295

CU2 268

CU3 246

CU4 234

CU5 204

CU6 183

CU7 180

CU8 145

CU9 127

CU10 111 /

TCUOUT(CU) outlet temperature of cold utility

/ CU1 300

CU2 269

CU3 247

CU4 235

CU5 205

CU6 184

CU7 181

CU8 146

CU9 128

CU10 112 /

CCU(CU) unit cost for cold utility

/ CU1 22

CU2 140

CU3 160

CU4 180

CU5 300

CU6 400

CU7 450

CU8 500

CU9 600

CU10 700 /

; FW(I,J)=0;

FW('H10','C1') = 851.636;

$FW('H11','C2') = 621.772;$
 $FW('H12','C3') = 450.434;$
 $FW('H13','C4') = 388.078;$
 $FW('H14','C5') = 263.583;$
 $FW('H15','C6') = 88.14;$
 $FW('H16','C7') = 230.15;$
 $FW('H17','C8') = 55.29;$
 $FW('H18','C9') = 21.027;$

`ex_z(I,J,K);`
`ex_z(I,J,K) = 0;`
`ex_z('H11','C1','firstlocation')= 1;`
`ex_z('H15','C1','firstlocation')= 1;`
`ex_z('H1','C1','firstlocation')= 1;`
`ex_z('H2','C2','location2')= 1;`
`ex_z('H12','C2','location2')= 1;`
`ex_z('H15','C2','location2')= 1;`
`ex_z('H17','C3','location3')= 1;`
`ex_z('H15','C3','location3')= 1;`
`ex_z('H3','C3','location3')= 1;`
`ex_z('H4','C4','location4')= 1;`
`ex_z('H17','C4','location4')= 1;`
`ex_z('H20','C5','location5')= 1;`
`ex_z('H18','C5','location5')= 1;`
`ex_z('H5','C5','location5')= 1;`
`ex_z('H6','C6','location6')= 1;`
`ex_z('H20','C6','location6')= 1;`
`ex_z('H7','C7','location7')= 1;`
`ex_z('H23','C7','location7')= 1;`
`ex_z('H21','C7','location7')= 1;`
`ex_z('H23','C8','location8')= 1;`
`ex_z('H8','C8','location8')= 1;`

`ex_z('H9','C9','location9')= 1;`

VARIABLES

TINH(I)	inlet temperature of hot stream
O	objective function
W	Shaft Work Requirement

;

POSITIVE VARIABLES

dt(I,J,K)	temperature approach for match ij at the left of stage k
dtcu(I,CU)	temperature approach for match hot stream i and cold utility
dthu(J)	temperature approach for match cold stream j and hot utility
q(I,J,K)	heat exchanged between hot stream i and cold stream j at stage k
qcu(I,CU)	heat exchanged between hot stream i and cold utility
qhu(J)	heat exchanged between cold stream j and hot utility
tH(I,K)	temperature of hot stream i at location k
tC(J,K)	temperature of cold stream j at location k

;

BINARY VARIABLE

z(I,J,K)	Binary variable of HEX Process to Process
zcu(I,CU)	Binary variable of cold utility
zhu(J)	Binary variable of hot utility
;	

`TINH.fx('H1') = 303.15;`

`TINH.fx('H2') = 271.634;`

`TINH.fx('H3') = 249.582;`

`TINH.fx('H4') = 236.977;`

`TINH.fx('H5') = 207.45;`

`TINH.fx('H6') = 186.17;`

TINH.fx('H7') = 183.036;

TINH.fx('H8') = 148.15;

TINH.fx('H9') = 129.446;

TINH.lo('H10') = 299;

TINH.lo('H11') = 272;

TINH.lo('H12') = 250;

TINH.lo('H13') = 240;

TINH.lo('H14') = 208;

TINH.lo('H15') = 187;

TINH.lo('H16') = 183;

TINH.lo('H17') = 148;

TINH.lo('H18') = 130;

TINH.up('H10') = 308.951;

TINH.up('H11') = 285.491;

TINH.up('H12') = 260.839;

TINH.up('H13') = 281.75;

TINH.up('H14') = 248.822;

TINH.up('H15') = 198.068;

TINH.up('H16') = 232.016;

TINH.up('H17') = 184.059;

TINH.up('H18') = 162.963;

EQUATIONS

OHB_H(I) overall heat balance for each hot stream

OHB_C(J) overall heat balance for each cold stream

SHB_H(I,K) heat balance at each stage for hot stream

SHB_C(J,K) heat balance at each stage for cold stream

TINHASSGN(I) assignment of inlet temperature of hot stream i

TINCASSGN(J) assignment of inlet temperature of cold stream j

FH1(I,K) feasibility of temperature at each stage for hot stream
 FH2(I) feasibility of temperature at last stage for hot stream
 FC1(J,K) feasibility of temperature at each stage for cold stream
 FC2(J) feasibility of temperature at first stage for cold stream
 HULOAD(I) hot utility load
 CULOAD(J) cold utility load
 HECOUNT1(I,J,K) count heat exchanger
 HECOUNT2(I,CU) count hot utility
 HECOUNT3(J) count cold utility
 APPTEMPL(I,J,K) approach temperature at the left of stage k
 APPTEMPR(I,J,K) approach temperature at the right of stage k
 APPTEMPCU(I,CU) approach temperature at cold utility of hot stream i
 APPTEMPHU(J) approach temperature at hot utility of cold stream j
 APPTEMPLIMIT(I,J,K) limiting temperature approach
 APPTEMPCUMIN (I,CU) approach temperature at cold utility
 CONSTMATCH define match of cold utility
 CONSTMATCHC define match of hot utility
 newmatchz(I,J,K)
 OBJFN objective function
 SHAFTWORK shaft work requirement

* Overall Energy balance.....

$OHB_H(I) \dots (TINH(I)-TOUTH(I))*FH(I) =e=$
 $SUM((J,K),q(I,J,K))+SUM(CU,qcu(I,CU));$
 $OHB_C(J) \dots (TOUTC(J)-TINC(J))*FC(J) =e= SUM((I,K),q(I,J,K))+qhu(J);$

* Heat balance at each stage.....

$SHB_H(I,K)$(ORD(K) NE CARD(K)) .. (tH(I,K)-tH(I,K+1))*FH(I) =e=$
 $SUM(J,q(I,J,K));$
 $SHB_C(J,K)$(ORD(K) NE CARD(K)) .. (tC(J,K)-tC(J,K+1))*FC(J) =e=$
 $SUM(I,q(I,J,K));$

* Assignment Temperature.....

```
TINHASSGN(I) .. TINH(I) =e= tH(I,'firstlocation');
TINCASSGN(J) .. TINC(J) =e= tC(J,'lastlocation');
```

* Feasible Temperature.....

```
FH1(I,K)$($ORD(K) NE CARD(K)) .. tH(I,K) =g= tH(I,K+1);
FH2(I) .. TOUTH(I) =l= tH(I,'lastlocation');
FC1(J,K)$($ORD(K) NE CARD(K)) .. tC(J,K) =g= tC(J,K+1);
FC2(J) .. TOUTC(J) =g= tC(J,'firstlocation');
```

* Heat&Cold utility.....

```
HULOAD(I) .. (tH(I,'lastlocation')-TOUTH(I))*FH(I) =e= SUM(CU,qcu(I,CU));
CULOAD(J) .. (TOUTC(J)-tC(J,'firstlocation'))*FC(J) =e= qhu(J);
```

* Counting existing heat exchanger at each stage.....

```
HECOUNT1(I,J,K)$($ORD(K) NE CARD(K)) .. q(I,J,K)-OMEGA*z(I,J,K) =l= 0;
HECOUNT2(I,CU).. qcu(I,CU)-OMEGA*zcu(I,CU) =l= 0;
HECOUNT3(J) .. qhu(J)-OMEGA*zhu(J) =l= 0;
```

* Calculation of approach temperature.....

```
APPTEML(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K) =l= tH(I,K)-
tC(J,K)+GAMMA*(1-z(I,J,K));
APPTEMPR(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K+1) =l= tH(I,K+1)-
tC(J,K+1)+GAMMA*(1-z(I,J,K));
APPTEMPCU(I,CU).. dtcu(I,CU) =l= tH(I,'lastlocation')-
TCUOUT(CU)+GAMMA*(1-zcu(I,CU));
APPTEMPHU(J) .. dthu(J) =l= TOUTC(J)- tC(J,'firstlocation')+GAMMA*(1-
zhu(J));
APPTEMLIMIT(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K) =g= EMAT;
APPTEMPCUMIN (I,CU) .. dtcu(I,CU) =g= EMAT;
CONSTMATCH.. SUM((I,CU),zcu(I,CU)) =l= 2;
```

```

CONSTMATCHC.. SUM((J),zhu(J)) =l= 0;
CONSTMATCHHX.. SUM((I,J,K),newz(I,J,K)) =l= 20;
newmatchz(I,J,K)$ORD(K) NE CARD(K) .. newz(I,J,K) =E= z(I,J,K)-ex_z(I,J,K);

```

```

* Objective Function.....  

OBJFN .. O =e=
SUM((I,CU),CCU(CU)*qcu(I,CU))+CHU*SUM(J,qhu(J))+CF*SUM((I,J,K),newz(I
,J,K))+SUM((I,CU),CF*zcu(I,CU))+CF*SUM(J,zhu(J))+  

CW*SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J)));
SHAFTWORK .. W =e= SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J))) ;
;  

MODEL STAGEMODEL SYNHEAT model /ALL/ ;  

SOLVE STAGEMODEL USING MIP MINIMISING O;  

DISPLAY z.l,ex_z,newz.l,zcu.l,zhu.l,tH.l,tC.l,q.l,qcu.l,qhu.l,O.l,W.l,FW;

```

Model of HEN Retrofit for Case 2 (new exchangers ≥ 10)

SETS

```

I      hot streams  

/H1,H2,H3,H4,H5,H6,H7,H8,H9,H10,H11,H12,H13,H14,H15,H16,H17,H18/  

J      cold streams / C1,C2,C3,C4,C5,C6,C7,C8,C9 /  

K      location   / firstlocation,location2*location26,lastlocation /  

CU     cold utility / CU1,CU2,CU3,CU4,CU5,CU6,CU7,CU8,CU9,CU10/  

;
```

SCALARS

OMEGA	upper bound for heat exchange /999999/
GAMMA	upper bound for temperature difference /999999/
EMAT	exchanger minimum approach temperature /3/
CHU	unit cost for hot utility /1000/
CF	fixed charge for exchangers /99000000/
CW	unit cost for power consumption /200000/

PARAMETERS

TOUTH(I) outlet temperature of cold stream

/	H1	271.634
	H2	249.582
	H3	236.977
	H4	207.45
	H5	186.17
	H6	183.036
	H7	148.15
	H8	129.446
	H9	118.15
	H10	298.58
	H11	271.79
	H12	249.58
	H13	237.15
	H14	207.416
	H15	186.214
	H16	182.579
	H17	147.941
	H18	129.501 /

TINC(J) inlet temperature of cold stream

/	C1	268.793
	C2	246.57
	C3	234.198
	C4	204.446
	C5	183.188
	C6	179.915
	C7	144.942
	C8	126.521
	C9	111.587 /

TOUTC(J) outlet temperature of cold stream

/ C1 269.293
C2 247.07
C3 234.698
C4 204.946
C5 183.688
C6 180.415
C7 145.442
C8 127.021
C9 112.087 /

FH(I) heat capacity of hot stream

/ H1 263.3583
H2 272.9911
H3 286.2356
H4 351.4749
H5 1480.733
H6 1276.324
H7 461.5032
H8 374.2515
H9 354.1076
H10 22399
H11 13446.61
H12 12558.84
H13 3152.466
H14 2504.468
H15 2901.974
H16 1036.471
H17 410.6263
H18 149.4232 /

FC(J) heat capacity of cold stream

/ C1 396200
C2 320063

C3	258800
C4	221200
C5	172800
C6	65600
C7	62400
C8	23300
C9	7830 /

FW(I,J) heat capacity of work

TCUIN(CU) inlet temperature of cold utility

/	CU1	295
	CU2	268
	CU3	246
	CU4	234
	CU5	204
	CU6	183
	CU7	180
	CU8	145
	CU9	127
	CU10	111 /

TCUOUT(CU) outlet temperature of cold utility

/	CU1	300
	CU2	269
	CU3	247
	CU4	235
	CU5	205
	CU6	184
	CU7	181
	CU8	146
	CU9	128
	CU10	112 /

CCU(CU) unit cost for cold utility

```

/ CU1 22
  CU2 140
  CU3 160
  CU4 180
  CU5 300
  CU6 400
  CU7 450
  CU8 500
  CU9 600
CU10 700    /
;
```

```

FW(I,J)=0;
FW('H10','C1') = 851.636;
FW('H11','C2') = 621.772;
FW('H12','C3') = 450.434;
FW('H13','C4') = 388.078;
FW('H14','C5') = 263.583;
FW('H15','C6') = 88.14;
FW('H16','C7') = 230.15;
FW('H17','C8') = 55.29;
FW('H18','C9') = 21.027;
```

```

ex_z(I,J,K),
ex_z(I,J,K) = 0;
ex_z('H11','C1','firstlocation')= 1;
ex_z('H15','C1','firstlocation')= 1;
ex_z('H1','C1','firstlocation')= 1;
ex_z('H2','C2','location2')= 1;
ex_z('H12','C2','location2')= 1;
ex_z('H15','C2','location2')= 1;
ex_z('H17','C3','location3')= 1;
ex_z('H15','C3','location3')= 1;
```

```

ex_z('H3','C3','location3')= 1;
ex_z('H4','C4','location4')= 1;
ex_z('H17','C4','location4')= 1;
ex_z('H20','C5','location5')= 1;
ex_z('H18','C5','location5')= 1;
ex_z('H5','C5','location5')= 1;
ex_z('H6','C6','location6')= 1;
ex_z('H20','C6','location6')= 1;
ex_z('H7','C7','location7')= 1;
ex_z('H23','C7','location7')= 1;
ex_z('H21','C7','location7')= 1;
ex_z('H23','C8','location8')= 1;
ex_z('H8','C8','location8')= 1;
ex_z('H9','C9','location9')= 1;

```

VARIABLES

TINH(I)	inlet temperature of hot stream
O	objective function
W	Shaft Work Requirement

POSITIVE VARIABLES

dt(I,J,K)	temperature approach for match ij at the left of stage k
dtcu(I,CU)	temperature approach for match hot stream i and cold utility
dthu(J)	temperature approach for match cold stream j and hot utility
q(I,J,K)	heat exchanged between hot stream i and cold stream j at stage k
qcu(I,CU)	heat exchanged between hot stream i and cold utility
qhu(J)	heat exchanged between cold stream j and hot utility
tH(I,K)	temperature of hot stream i at location k
tC(J,K)	temperature of cold stream j at location k

BINARY VARIABLE

z(I,J,K)	Binary variable of HEX Process to Process
zcu(I,CU)	Binary variable of cold utility
zhu(J)	Binary variable of hot utility

TINH.fx('H1') = 303.15;

TINH.fx('H2') = 271.634;

TINH.fx('H3') = 249.582;

TINH.fx('H4') = 236.977;

TINH.fx('H5') = 207.45;

TINH.fx('H6') = 186.17;

TINH.fx('H7') = 183.036;

TINH.fx('H8') = 148.15;

TINH.fx('H9') = 129.446;

TINH.lo('H10') = 299;

TINH.lo('H11') = 272;

TINH.lo('H12') = 250;

TINH.lo('H13') = 240;

TINH.lo('H14') = 208;

TINH.lo('H15') = 187;

TINH.lo('H16') = 183;

TINH.lo('H17') = 148;

TINH.lo('H18') = 130;

TINH.up('H10') = 308.951;

TINH.up('H11') = 285.491;

TINH.up('H12') = 260.839;

TINH.up('H13') = 281.75;

TINH.up('H14') = 248.822;

TINH.up('H15') = 198.068;
 TINH.up('H16') = 232.016;
 TINH.up('H17') = 184.059;
 TINH.up('H18') = 162.963;

EQUATIONS

OHB_H(I) overall heat balance for each hot stream
 OHB_C(J) overall heat balance for each cold stream
 SHB_H(I,K) heat balance at each stage for hot stream
 SHB_C(J,K) heat balance at each stage for cold stream
 TINHASSGN(I) assignment of inlet temperature of hot stream i
 TINCASSGN(J) assignment of inlet temperature of cold stream j
 FH1(I,K) feasibility of temperature at each stage for hot stream
 FH2(I) feasibility of temperature at last stage for hot stream
 FC1(J,K) feasibility of temperature at each stage for cold stream
 FC2(J) feasibility of temperature at first stage for cold stream
 HULOAD(I) hot utility load
 CULOAD(J) cold utility load
 HECOUNT1(I,J,K) count heat exchanger
 HECOUNT2(I,CU) count hot utility
 HECOUNT3(J) count cold utility
 APPTEML(I,J,K) approach temperature at the left of stage k
 APPTEMPR(I,J,K) approach temperature at the right of stage k
 APPTEMPCU(I,CU) approach temperature at cold utility of hot stream i
 APPTEMPHU(J) approach temperature at hot utility of cold stream j
 APPTEMLIMIT(I,J,K) limiting temperature approach
 APPTEMPCUMIN (I,CU) approach temperature at cold utility
 CONSTMATCH define match of cold utility
 CONSTMATCHC define match of hot utility
 newmatchz(I,J,K)
 OBJFN objective function

SHAFTWORK shaft work requirement

* Overall Energy balance.....

OHB_H(I) .. (TINH(I)-TOUTH(I))*FH(I) =e=

SUM((J,K),q(I,J,K))+SUM(CU,qcu(I,CU));

OHB_C(J) .. (TOUTC(J)-TINC(J))*FC(J) =e= SUM((I,K),q(I,J,K))+qhu(J);

* Heat balance at each stage.....

SHB_H(I,K)\$ORD(K) NE CARD(K) .. (tH(I,K)-tH(I,K+1))*FH(I) =e=

SUM(J,q(I,J,K));

SHB_C(J,K)\$ORD(K) NE CARD(K) .. (tC(J,K)-tC(J,K+1))*FC(J) =e=

SUM(I,q(I,J,K));

* Assignment Temperature.....

TINHASSGN(I) .. TINH(I) =e= tH(I,'firstlocation');

TINCASSGN(J) .. TINC(J) =e= tC(J,'lastlocation');

* Feasible Temperature.....

FH1(I,K)\$ORD(K) NE CARD(K) .. tH(I,K) =g= tH(I,K+1);

FH2(I) .. TOUTH(I) =l= tH(I,'lastlocation');

FC1(J,K)\$ORD(K) NE CARD(K) .. tC(J,K) =g= tC(J,K+1);

FC2(J) .. TOUTC(J) =g= tC(J,'firstlocation');

* Heat&Cold utility.....

HULOAD(I) .. (tH(I,'lastlocation')-TOUTH(I))*FH(I) =e= SUM(CU,qcu(I,CU));

CULOAD(J) .. (TOUTC(J)-tC(J,'firstlocation'))*FC(J) =e= qhu(J);

* Counting existing heat exchanger at each stage.....

HECOUNT1(I,J,K)\$ORD(K) NE CARD(K) .. q(I,J,K)-OMEGA*z(I,J,K) =l= 0;

HECOUNT2(I,CU).. qcu(I,CU)-OMEGA*zcu(I,CU) =l= 0;

HECOUNT3(J) .. qhu(J)-OMEGA*zhu(J) =l= 0;

```

* Calculation of approach temperature.....  

APPTEMPL(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K) =l= tH(I,K)-  

tC(J,K)+GAMMA*(1-z(I,J,K));  

APPTEMPR(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K+1) =l= tH(I,K+1)-  

tC(J,K+1)+GAMMA*(1-z(I,J,K));  

APPTEMPCU(I,CU).. dtcu(I,CU) =l= tH(I,'lastlocation')-  

TCUOUT(CU)+GAMMA*(1-zcu(I,CU));  

APPTEMPHU(J) .. dthu(J) =l= TOUTC(J)- tC(J,'firstlocation')+GAMMA*(1-  

zhu(J));  

APPTEMPLIMIT(I,J,K)$($ORD(K) NE CARD(K)) .. dt(I,J,K) =g= EMAT;  

APPTEMPCUMIN (I,CU) .. dtcu(I,CU) =g= EMAT;  

CONSTMATCH.. SUM((I,CU),zcu(I,CU)) =l= 2;  

CONSTMATCHC.. SUM((J),zhu(J)) =l= 0;  

CONSTMATCHHX.. SUM((I,J,K),newz(I,J,K)) =l= 10;  

newmatchz(I,J,K)$($ORD(K) NE CARD(K)) .. newz(I,J,K) =E= z(I,J,K)-ex_z(I,J,K);  


```

* Objective Function.....

```

OBJFN .. O =e=  

SUM((I,CU),CCU(CU)*qcu(I,CU))+CHU*SUM(J,qhu(J))+CF*SUM((I,J,K),newz(I  

,J,K))+SUM((I,CU),CF*zcu(I,CU))+CF*SUM(J,zhu(J))+  

CW*SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J)));  

SHAFTWORK .. W =e= SUM((I,J),FW(I,J)*(TINH(I)-TOUTC(J))) ;  

;  

MODEL STAGEMODEL SYNHEAT model /ALL/ ;  

SOLVE STAGEMODEL USING MIP MINIMISING O;  

DISPLAY z.l,ex_z,newz.l,zcu.l,zhu.l,tH.l,tC.l,q.l,qcu.l,qhu.l,O.l,W.l,FW;

```

Retrofitted HEN Model Validation by PROII

The result from GAMS for case 1 (new exchangers ≥ 20) is validated with PROII by using the same match of exchanger because this result provides the optimal

solution when compares case 1 (new exchangers ≥ 20) with case 2 (new exchangers ≥ 10). Figure C1 is illustrated the result of validation. Temperature and duty of streams are changed; additionally, three new cooling utilities are added in structure. The result of validation is 229,900 kW of cooling duty and 128,775.69 kW of shaft work requirement. There are errors of temperature, duty and phase change at target temperature of hot stream when compares with base case due to result from GAMS with assumption of heat capacity constant and without consideration of latent heat. In addition, Mathematical Programming does not include equation of thermodynamic. Although there are error of temperature, duty and phase change, the result from GAMS is validated by PROII, resulting in shaft work saving and cooling duty saving are about 10.62 % and 1.16 % from base case.

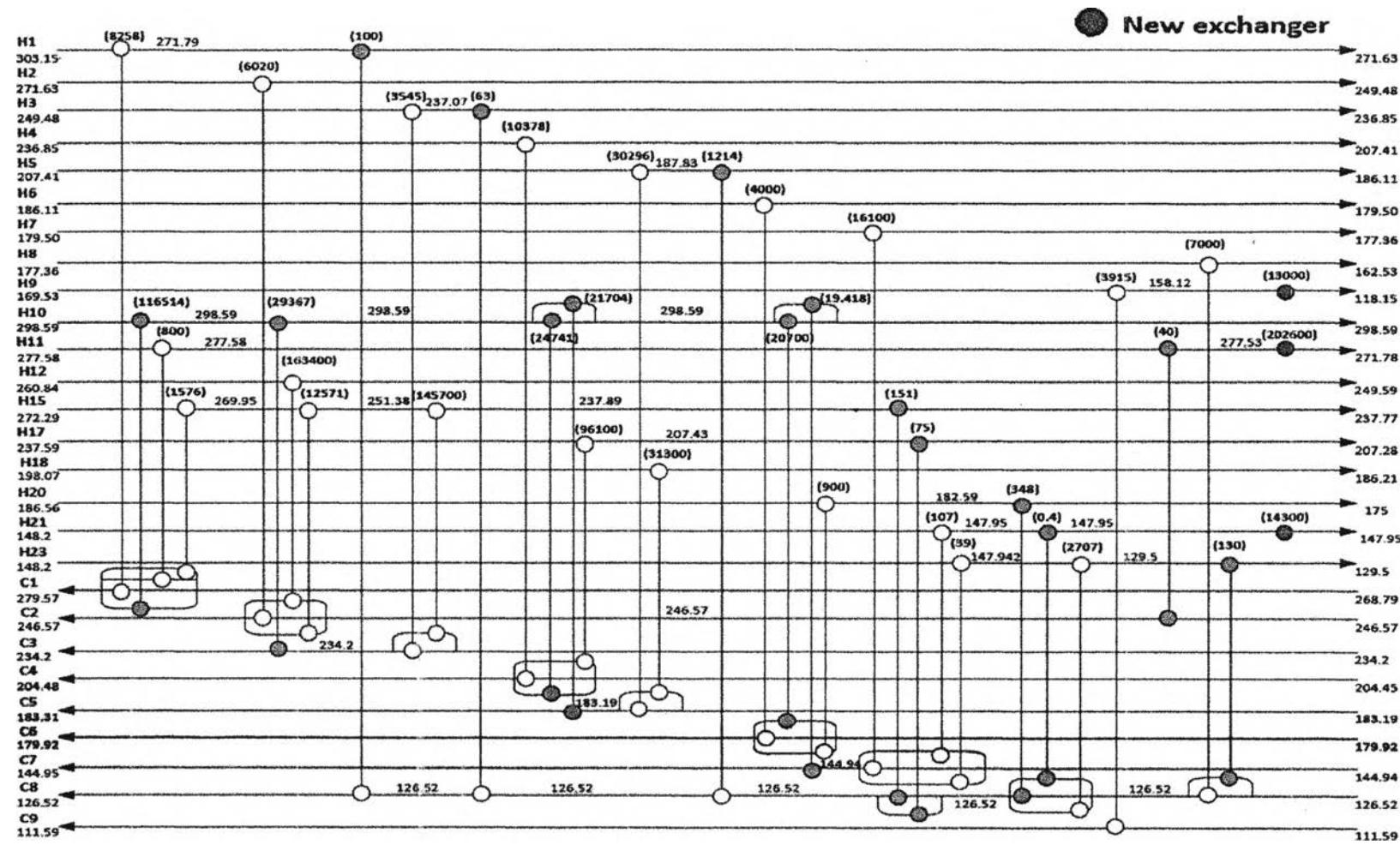


Figure C1 The result of Retrofitted HEN of case 1 (new exchangers ≥ 20) validation from Mathematical programming.

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Proceedings:

1. Thasai, J.; and Siemanond, K. (2015, April 21) Design and Optimization of Cryogenic Process. Proceedings of the 6th Research Symposium on Petrochemical and Materials Technology and the 21th PPC Symposium on Petroleum, Petrochemicals, and Polymers, Bangkok, Thailand.
2. Thasai, J.; and Siemanond, K. (2015, May 19-22) Combined Exergy-Pinch Analysis to Improve Cryogenic Process. Proceedings of the 12th International Conference on Chemical & Process Engineering (ICHEAP 12), Milan, Italy.