# ระบบพื้นรูปรางน้ำคว่ำภายใต้น้ำหนักกระจายสม่ำเสมอ



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วิทยานิพนธ์นี้ เป็นส่วนหนึ่งของการศึกษาตามหลักสูตรปริญญาวิศวกรรมศาสตรมหาบัณฑิต แผนกวิชาวิศวกรรมโยธา บัณฑิตวิทยาลัย จุฬาลงกรณมหาวิทยาลัย พ.ศ. 2520

## INVERTED CHANNEL FLOOR SYSTEM UNDER UNIFORMLY DISTRIBUTED LOAD

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A Thesis Submitted in Partial Fulfillment of the Requirements

for the Degree of Master of Engineering

Department of Civil Engineering

Graduate School

Chulalongkorn University

1977

Thesis Title Inverted Channel Floor System under Uniformly

Distributed Load

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ปีการศึกษา 2520

บทคัดยล



การวิจัยนี้ได้แสดงวิธีการคำนวณหาแรงและระยะโกงตางๆของระบบพื้นรูป รางน้ำควำภายใต้น้ำหนักกระจายสม่ำ เสมอซึ่งไม่ยึดรั้งกับที่รองรับ การแก้ปัญหานี้ใช้ ทฤษฎีของแผนบางโดยมีสมมติฐานวาแผนพื้นในแนวดึงและในแนวราบถูกกระทำโดย แรงรวมระหวางแรงดัดและแรงภายในระนาบของแผนพื้น มีตัวอยางการคำนวณและ ได้แสดงผลที่ได้ในรูปของกราฟ เพื่อให้ เห็นผลของการเปลี่ยนแปลงขนาดตางๆ นอกจาก นั้นยังได้เปรียบ เทียบผลที่ได้กับทฤษฎีแรงดัดธรรมดาและได้ประเมินความละเอียดถูกต้องของการใช้ความกว้างประสิทธิผลด้วย

Thesis Title Inverted Channel Floor System under Uniformly

Distributed Load

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#### ABSTRACT

A complete solution of stress resultants and displacements of inverted channel floor system, simply supported at the ends and subjected to uniformly distributed load, is presented. The problem is solved by the theory of thin plates under the assumption that the vertical and horizontal plates are thin plates subjected to combined bending and in-plane forces.

Numerical examples are given and the results are shown in the form of figures to show the effect of various geometric parameters. Comparisons of the results between the proposed method and the simple bending theory are presented and the accuracy of the effective width criteria in conventional flexural analysis is evaluated.

#### ACKNOWLEDGEMENTS

The author wishes to express his deep gratitute to his advisor, Mr. Mana Vongpivat, for his helpful guidance and assistance thoughout this study. He also wishes to express his appreciation to Prof. Dr. Niwat Daranandana, Prof. Arun Chaiseri and Asst. Prof. Dr. Suthum Suriyamongkol for serving as members of the thesis committee.

Grateful acknowledgements are extended to Mr. Arthorn Sinsawasdi and Mr. Sukij Kiatboonsri for their generous help in the computer work. Thanks are also due to Miss Sukuman Satitanun for typing the manuscript.



### TABLE OF CONTENTS

	Pag
Title Page in Thai	ſi
Title Page in English	ii
Thesis Approval	iii
Abstract in Thai	iv
Abstract in English	٧
Acknowledgements	vi
Table of Contents	vii
List of Figures	viii
List of Symbols	x
CHAPTER	
I INTRODUCTION	1
II METHOD OF ANALYSIS	3
Assumptions	3
Rectangular Plates in Bending	4
Rectangular Plates in Plane Stress	8
Applied Load and Load Factors	12
Boundary Conditions	13
Solution	14
III NUMERICAL EXAMPLES AND RESULTS	19
IV DISCUSSION AND CONCLUSION	22
REFERENCES	24
APPENDIX	47
VITA	63

## LIST OF FIGURES

Figure	Title	Page
1.	Simply Supported Inverted Channel Floor Unit.	25
2.	Orientation of Coordinate Axes.	25
3.	Positive Directions of Stress Resultants and Load	
	Components.	26
4.	Positive Directions of the Stress Resultants and	
	Displacements at the Joint.	26
5.	Stress Resultants and Displacements: 2a = 30 cm.,	
	$2c = 15 \text{ cm.}, t_d = t_w = 4 \text{ cm.}, b = 400 \text{ cm.}$	27
6.	Comparison of Stress Resultants and Displacements	
	Between Various Thickness: 2a = 30 cm., 2c = 15 cm.,	
	$b = 400 \text{ cm.}, t_d = t_w = 3, 4 \text{ and } 5 \text{ cm.}$	30
7.	Comparison of Stress Resultants and Displacements	
	Between Various Depths: 2a = 30 cm., td = t = 4 cm.,	
	b = 400  cm., 2c = 10, 15  and  20  cm.	33
8.	Comparison of Stress Resultant and Displacements	
	Between the Proposed Method and Simple Bending Theory:	
1 y 1	$2a = 40 \text{ cm.}, 2c = 30 \text{ cm.}, t_d = t_w = 4 \text{ cm.}, b = 400 \text{ cm.}$	36
9.	Comparison of Stress Resultant and Displacements	
	Between the Proposed Method and Simple Bending Theory:	
	$2a = 60$ cm., $2c = 30$ cm., $t_d = t_w = 4$ cm., $b = 400$ cm.	38
10.	Comparison of Stress Resultant and Displacements	
	Between the Proposed Method and Simple Bending Theory:	
	$2a = 80 \text{ cm.}$ , $2c = 30 \text{ cm.}$ , $t_d = t_w = 4 \text{ cm.}$ , $b = 400 \text{ cm.}$	40

.

## LIST OF FIGURE (Continued)

Figure	Title	Page
11.	Stress Resultants and Displacements: 2a = 80 cm.,	
	$2c = 30 \text{ cm.}, t_d = t_w = 4 \text{ cm.}, b = 400 \text{ cm.}$	42



#### LIST OF SYMBOLS

- A = constant of integration for horizontal plate
- a = distant from mid-width of horizontal plate to mid-plane of vertical plate
- B = constant of integration for vertical plate
- b = span length
- C = constant of integration for horizontal plate
- c = distant from mid-width of vertical plate to mid-plane of horizontal plate
- D = flexural rigidity of plate
- E = modulus of elasticity
- K == load factor in bending analysis
- L = load factor in membrane analysis
- $M_{_{\mathrm{X}}}$  = bending moment per unit length of section of a plate perpendecular to x-axis
- M = bending moment per unit length of section of a plate perpendicular to y-axis
- M = twisting moment per unit length of section of a plate perpendicular to x-axis
- m = summation index
- $N_{_{
  m X}}$  = normal force per unit length of section of a plate perpendicular to x-axis
- N<sub>y</sub> = normal force per unit length of section of a plate perpendicular to y-axis
- N = membrane shearing force per unit length of section of a plate perme pendicular to x-axis

- n = summation index
- Q = shearing force perallel to z-axis per unit length of section of a plate perpendicular to x-axis
- Qy = shearing force parallel to z-axis per unit length of section of a plate perpendicular to y-axis
- t = thickness of a plate
- u = component of displacement in x-direction
- $V_{x}$  = supplemented shearing force parallel to z-axis per unit length of section of a plate perpendicular to x-axis
- V<sub>y</sub> = supplemented shearing force parallel to z-axis per unit length of section of a plate perpendicular to y-axis
- v = component of displacement in y-direction
- w = component of displacement in z-direction
- x,y,z,= rectangular coordinates
- $\nabla^4$  = biharmonic operator
- v = Poisson's ratio
- φ = Airy's stress function

The subscripts d and w refer to horizontal and vertical plates respectively.