



- (๑) Lester Lipsky, and J.D. Church; "Application of a queueing network model for a computer system" in Computing Surveys, Vol.9, No.3, Sept. 1977.
- (๒) Peter J. Denning and Jeffrey P. Buzen "The operational Analysis of queueing network model" in Computing Surveys, Vol.10, No.3, Sept. 1978.
- (๓) Chiu, W.; Dumont, D.; and Woods, R., "Performance Analysis of a multiprogrammed Computer system" in IBM J.R. & D. 19(1975)
- (๔) Bhandiwad, R.A., and Williams, A.C., "Queueing network model of Computer System," in Proc. Third Annual Symp. Computer system, Univ. Tesax, Austin 1974.
- (๕) Giammo, T., "Validation of Computer performance Model of the exponential queueing network family" in Acta Informatica 7, 1976.
- (๖) Jackson., "Network of waiting lines," in Operations Research 5, (1957), 518-521.
- (๗) Jackson, J.r., "Jobshop-like queueing system," in Management Science 10, (1963), 131-142.
- (๘) Gordon, W.J., and Newell, G.F., "WClosed queueing system with exponential servers", in Operations Research 15, (1967), 254-265.
- (๙) Buzen, J.P., "Queueing network models of Multiprogramming," Ph.D. Thesis, Div. Engineering and applied Science, Harvard Univ., Cambridge, Mass, 1971.

- (90) Buzen, J.P., "Analysis of system Bottlenecks using a queueing Network Model," in Proc. ACM. SIGOPS Workshop system performance Evaluation, ACM, N.Y., 1971, p. 82-103.
- (91) Scherr, A.L., "An analysis of time shared computer system", MIT Press, Cambridge, Mass, 1967.
- (92) Buzen, J.P. "Analysis of system bottlenecks using a queueing network model" in Proc. ACM. SIGOPS Workshop System Performance Evaluation, 1971, ACM; N.Y. pp. 82-103.
- (93) Buzen, J.P., "Queueing network models of multiprogramming," Ph.D. Thesis, Div. Eng. and Applied Physics, Harvard Univ., Cambridge, Mass, May, 1971.
- (94) Buzen, J.P. "Computational algorithms for closed queueing networks with exponential servers," Commun. ACM 16, 9(1973) pp. 527-531.
- (95) W. Chiu;, D. Dumont; and R. Wood. "Performance Analysis of a multiprogrammed computer System" in IBM. J. Res. Develop., May 1975
- (96) IBM System/370 Ssystem Summary.
- (97) IBM Sytem/370 Principles of Operation.
- (98) A guide to the IBM System/370 Model 138.
- (99) IBM'S Data processing Division Reference Manual for IBM 3420 Models 3 and 5 Magnetictape Subsystem.
- (100) IBM Student text Introduction to IBM Direct-Access Storage Devices and Organization Methods.
- (101) John W. Boyse and David R. Warn" A Straight forward Model for Computer Performance Prediction" in Computing Surveys Vol. 7, No. 2, June 1975.

- 62
- (1010) Rose, C.A. "Measurement procedure for Queueing Network models of computer systems," in Computing surveys 10, 3 (Sept. 1978)
- (1011) Morse, P.M., Queues Inventories, and Maintenance. John Wiley & Sons, N.Y., 1958
- (1012) Sauer, C; and Chandy, K.M. "Approximate methods for Analyzing Queueing Network Models of Computing Systems in Computing Survey Vol. 10, No. 3, Sep. 1978.
- (1013) Billey E. Gillett. Introduction to operation Research: A Comp Oriented Algorithmic Approach. McGraw-Hill Ltd, N.Y.
- (1014) James Martin. System analysis for data Transmission. Englewood Chifts, N.J., prentice-Hall, 1972.
- (1015) Herbert Heller man and Thomas F. Conroy, Computer system Performance. McGraw-Hill Kogakusha Ltd, TOKYO
- (1016) Stuart E. Madnick and John J. Donovan. Operating System. McGraw-Hill Kogakusha Ltd. TOKYO
- (1017) G.F. Newell. Applications of queueing theory. Chapman and Hall Ltd. London.

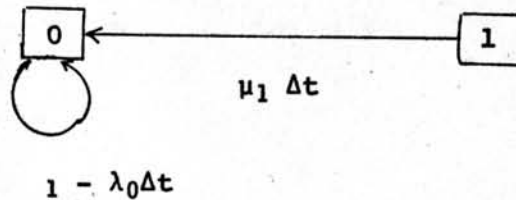
การพิมพ์

ภาคผนวก

พิสูจน์สมการ 3.18 และ 3.19

เขียน detailed balance เมื่อระบบเข้าสู่ steady-state โดยให้  
 n แทน state ของระบบ ( $n = 0, 1, \dots, n, \dots, M$ )

เมื่อระบบอยู่ใน state 0



$$P_0(t + \Delta t) = P_0(t)(1 - \lambda_0 \Delta t) + P_1(t)\mu_1 \Delta t$$

$$\frac{P_0(t + \Delta t) - P_0(t)}{\Delta t} = \mu_1 P_1(t) - \lambda_0 P_0(t)$$

เมื่อ  $\Delta t \rightarrow 0$  จะได้

$$\frac{d}{dt} P_0(t) = \mu_1 P_1(t) - \lambda_0 P_0(t)$$

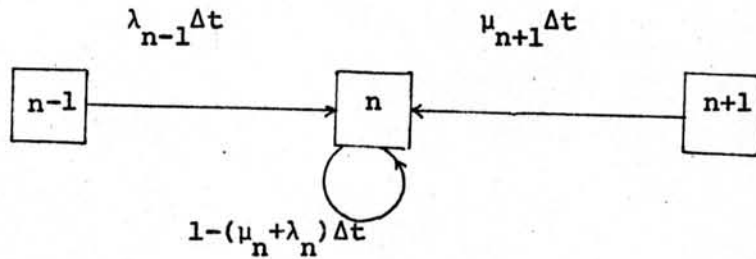
เมื่อระบบเข้าสู่ steady state  $\frac{d}{dt} P_0(t) = 0$

$$\therefore \mu_1 P_1(t) - \lambda_0 P_0(t) = 0 \quad \longrightarrow 1$$

และโอกาสที่จะมีงานในระบบ = n ไม่ขึ้นกับเวลา t เมื่อระบบเข้าสู่ steady state ดังนั้น ถ้าเราแทนค่า  $P_n(t)$  ด้วย  $\pi(n)$  จะได้

$$\lambda_0 \pi_0 - \mu_1 \pi_1 = 0 \quad \longrightarrow \quad 2$$

เมื่อระบบอยู่ใน state n



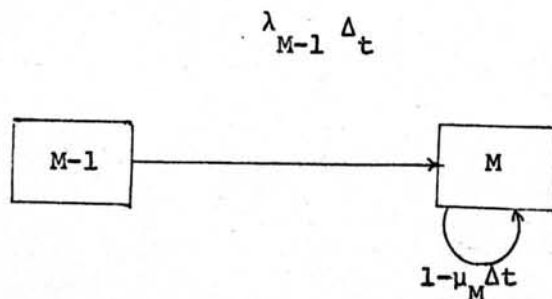
$$P_n(t+\Delta t) = P_{n-1}(t) (\lambda_{n-1} \Delta t) + P_n(t) [1 - (\lambda_n + \mu_n) \Delta t] + P_{n+1}(t) (\mu_{n+1} \Delta t)$$

$$\frac{P_n(t+\Delta t) - P_n(t)}{\Delta t} = P_{n-1}(t) \lambda_{n-1} - P_n(t) (\lambda_n + \mu_n) + P_{n+1}(t) \mu_{n+1}$$

$$\frac{d}{dt} P_n(t) = 0 = P_{n-1}(t) \lambda_{n-1} - P_n(t) (\lambda_n + \mu_n) + P_{n+1}(t) \mu_{n+1}$$

$$\pi_{n+1} \cdot \mu_{n+1} + \pi_{n-1} - \pi_n (\mu_n + \lambda_n) + \pi_{n-1} \lambda_{n-1} = 0 \quad \longrightarrow \quad 3$$

เมื่อระบบอยู่ใน state M



$$P_M(t+\Delta t) = P_{M-1}(t)\lambda_{M-1}\Delta t + P_M(t)[1-\mu_M\Delta t]$$

$$\frac{P_M(t+\Delta t) - P_M(t)}{\Delta t} = P_{M-1}(t)\lambda_{M-1} - P_M(t)\mu_M$$

$$\frac{d}{dt} P_M(t) = 0 = P_{M-1}(t)\lambda_{M-1} - P_M(t)\mu_M$$

$$\pi_{M-1}\lambda_{M-1} - \pi_M\mu_M = 0 \quad \longrightarrow 4$$

จาก (2)  $\pi_1 = \frac{\pi_0\lambda_0}{\mu_1} \quad \longrightarrow 5$

จาก (3) แทนค่า  $n = 1$  จะได้

$$\pi_2\mu_2 + \pi_0\lambda_0 - (\mu_1 + \lambda_1)\pi_1 = 0 \quad \longrightarrow 6$$

แทนค่า 5 ใน 6 จะได้

$$\pi_2 = \frac{\lambda_0\lambda_1\pi_0}{\mu_1\mu_2} \quad \longrightarrow 7$$

จาก 3 แทนค่า  $n = 2$  จะได้

$$\pi_3\mu_3 + \pi_1\lambda_1 - (\mu_2 + \lambda_2)\pi_2 = 0 \quad \longrightarrow 8$$

แทนค่า  $\pi_1$  และ  $\pi_2$  ใน 8

$$\therefore \pi_3 = \frac{\lambda_0\lambda_1\lambda_2\pi_0}{\mu_1\mu_2\mu_3} \quad \longrightarrow 9$$

จาก 9 แทนค่า  $\pi_0$  ในเทอมของ  $\pi_2$  จากสมการ 7

$$\therefore \pi_3 = \frac{\lambda_2 \pi_2}{\mu_3}$$

$$\therefore \pi_n = \frac{\lambda_{n-1} \cdot \pi_{n-1}}{\mu_n} \longrightarrow 10$$

จาก 9

$$\pi_m = \frac{\lambda_0 \lambda_1 \lambda_2 \dots \lambda_{m-1}}{\mu_1 \mu_2 \dots \mu_m} \cdot (\pi_0)$$

$$\pi_m = \prod_{j=1}^m \frac{\lambda_{j-1}}{\mu_j} \cdot \pi_0$$

$$\sum_{m=0}^M \pi_m = \sum_{m=0}^M \prod_{j=1}^m \frac{\lambda_{j-1}}{\mu_j} \cdot \pi_0$$

$$1 = \sum_{m=0}^M \prod_{j=1}^m (M-j+1) \cdot (c/i) \cdot (\pi_0)$$

$$\therefore \pi_0 = \frac{1}{\sum_{m=0}^M \frac{M!}{(M-m)!} \cdot (c/i)^m} \longrightarrow 11$$

แทนค่า (3.21) และ (3.22) ใน (11) จะได้

$$\pi_0 = \frac{1}{1 + \sum_{m=1}^M \prod_{j=1}^m \frac{\lambda_{j-1}}{\mu_j}} \longrightarrow 12$$



## ประวัติผู้ทำการวิจัย

นายศรีสุข เทียนสันติสุข ได้รับปริญญาวิศวกรรมศาสตรบัณฑิต สาขาวิศวกรรมไฟฟ้า  
จากคณะวิศวกรรมศาสตร์ สถาบันเทคโนโลยีพระจอมเกล้า วิทยาเขตธนบุรี เมื่อปีการศึกษา ๒๕๑๔

