

#### In Partial Fulfillment for the Degree of Bachelor of Science

Department of Chemistry, Faculty of Science

Chulalongkorn University

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การศึกษาการดูดซับก๊าซและปฏิกิริยาที่เกิดขึ้นบนอนุภาคนาโนซีเรีย



โครงการนี้เป็นส่วนหนึ่งของการศึกษาตามหลักสูตรปริญญาวิทยาศาสตรบัณฑิต

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ปีการศึกษา 2557



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**Project Title:** 

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**Project Advisor:** 

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**ชื่อโครงการ** การศึกษาการดูดซับก๊าซและปฏิกิริยาที่เกิดขึ้นบนอนุภาคนาโนซีเรีย

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# บทคัดย่อ

ทึกษาการดูดซับโมเลกุลก๊าซได้แก่ ไฮโดรเจน, ในโตรเจน, ออกซิเจน, การ์บอนมอนออกไซด์, ในโตรเจนมอนออกไซด์, การ์บอนไดออกไซด์, ไดไนโตรเจนมอนอกไซด์, ไนโตรเจนไดออกไซด์, น้ำ, ใดไฮโดรเจนซัลไฟด์, ซัลเฟอร์ไดออกไซด์, อีไทน์, อีทีน, มีเทน และแอมโมเนีย ที่ถูกดูดซับบนอนุภาคนา โนซีเรียได้แก่ ซีเรียมไดออกไซด์ (CeO<sub>2</sub>) และไดซีเรียมเตเตระออกไซด์ (Ce<sub>2</sub>O<sub>4</sub>) โดยการกำนวณด้วยวิธี DFT/B3LYP/GEN พบว่าการดูดซับของน้ำบน CeO<sub>2</sub> และCe<sub>2</sub>O<sub>4</sub> ดูดซับได้ดีที่สุด ซึ่งก่าการดูดซับบน CeO<sub>2</sub> และ Ce<sub>2</sub>O<sub>4</sub> เป็น -51.45 และ -52.45 กิโลแกลอรี่ต่อโมล ตามลำคับ ก่าช่องว่างพลังงานของ CeO<sub>2</sub> และ Ce<sub>2</sub>O<sub>4</sub> มีก่าลดลงมากหลังจากดูดซับโมเลกุลออกซิเจน และในโตรเจนมอนอกไซด์ ดังนั้น CeO<sub>2</sub> และ Ce<sub>2</sub>O<sub>4</sub> สามารถนำไปเป็นวัสดุรับรู้ก๊าซออกซิเจนและก๊าซไนโตรเจนมอนอกไซด์ได้ และยังพบว่าปฏิกิริยารี ดักชั่นของ CeO<sub>2</sub> ไปเป็น CeO โดยก๊าซไฮโดรเจนนั้นไม่สามารถเกิดขึ้นเองได้ที่อุณหภูมิ 298 เกลวิน ซึ่งก่า พลังงานอิสระมีก่า 234.1 กิโลแกลอรี่ต่อโมล

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# ABSTRACT

Adsorptions of diatomic (H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, CO, NO), triatomic (CO<sub>2</sub>, N<sub>2</sub>O, NO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub>S, SO<sub>2</sub>) and polyatomic (C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CH<sub>4</sub>, NH<sub>3</sub>) gases on CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> clusters were studied using the DFT/B3LYP/GEN method. Water adsorptions on Ce atom of CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> clusters were found to be the most favorable process. The adsorption enthalpies for water adsorbed on the CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> clusters are -51.45 and -52.45 kcal/mol, respectively. Energy gaps of CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> clusters largely decreased after adsorptions of O<sub>2</sub> and NO gases. The CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> clusters can therefore be used as the sensing materials for O<sub>2</sub> and NO detections. It was found that the CeO<sub>2</sub> reduced to the CeO cluster by H<sub>2</sub> gas is non-spontaneous reaction at 298 K; the Gibbs free energy of the reaction is 234.1 kcal/mol.

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#### CHAPTER I

#### **INTRODUCTION**

#### 1.1 Background and literature review

In petrochemical industry, Ceria or Ceriumdioxide (CeO<sub>2</sub>) is popularly used because of many specific chemical charateristics. For example: UV-visible adsorption capability [1], high level of heat stabilization [2], electrolyte and diffusion [3], solid, specific chemical reaction [4], oxygen storage and oxygen transmittance capability [5]. Therefore, nanoceriumdioxide particle is one of the significant substances in the industry of petrochemical. This substance is used as a catalyst in some kinds of reaction such as hydrocarbon transformtion, changing CO and NO<sub>x</sub> into H<sub>2</sub>O, CO<sub>2</sub> and N<sub>2</sub> in vehical system [6-10], solar cell, fuel cell, phosphorescent, luminescent, sensor gas etc. [11-14]. The information from the research of gas adsorption and ceriumdioxide surfaced reaction is a good source for estimating the reaction of ceriumdioxide surface. The special character on the surface consists of two features: crystal and nanoparticle.

In the year of 2009, Chen H. et al [15] analyzed the electronic properties of nanoparticle through the density functional theory. Fire algorithm binding with simulation of annealing process obtains all structures with global minimal energies and then DMOL3 program further re-optimized with double numerical atomic basis sets. Two helpful investigating methods are computed to describe the chemical reaction of different sites for nanoparticle.

In the year of 2010, Syzgantseva O. et al [16] analyzed the interaction between  $ZrO_2$  molecule and H<sub>2</sub> within the DFT and CCSD approached. H<sub>2</sub> is firstly activated and then the cleavage of H-H bond effecting OZrH-OH species with hydride and hydroxyl groups. Both direct transfer and two step process via Zr intermediate leads to the formation of water generating ZrO into H<sub>2</sub>O. The hybrid B3LYP or PBE0 functional with SDD basis set on Zr and 6-311 basis sets for O and H, representing the cooperation between accuracy and computational cost.

#### **1.2 Theoretical background**

Quantum Chemistry is categorized into semi-empirical, Hartree-Fock (HF) and density functional theory (DFT) methods to describe the behaviors of molecules. Quantum chemical studies relate to the ground state of individual atoms and molecules, to excited states, and to the transition states that occur throughout chemical reaction.

#### 1.2.1 Quantum chemical calculations

According to quantum mechanics research (QM), this study describes a unit that quantum theory allocates into certain physical quantities; for example, the energy of an atom at ground state. The synopsis of QM were introduced by Max Planck, Niels Bohr, Louise de Broglie, Erwin Schrödinger, Werner Heisenberg and others. The significant features of hypothesis of QM is called wave function, exist for any chemical system, and that appropriate function which react upon  $\Psi$  return the noticeable properties of the system. The equivalent formulation of QM was invented by Schrödinger [17-21],

$$\widehat{H}\Psi = E\Psi, \tag{1.1}$$

where  $\hat{H}$  is Hamiltonian operator, E is the total energy of the system and  $\Psi$  is the n-electron wave function, respectively.

The kinetic and potential energies within each molecule were indicated by the  $\hat{H}$  as illustrated in the equation. (1.2)

$$\hat{H} = -\frac{\hbar^2}{2m_e} \sum_{i}^{\text{electrons}} \nabla_i^2 - \frac{\hbar^2}{2} \sum_{A}^{\text{nuclei}} \frac{1}{M_A} \nabla_A^2 - \frac{e^2}{4} \sum_{0}^{\text{electron}} \sum_{A}^{\text{nuclei}} \frac{A}{r_{iA}} + \frac{e^2}{4} \sum_{0}^{\text{electrons}} \sum_{i}^{\text{electrons}} \frac{1}{r_{ij}} + \frac{e^2}{4} \sum_{0}^{\text{nuclei}} \sum_{B}^{\text{nuclei}} \frac{A}{R_{AB}}$$
(1.2)

where Z is the nuclear charge,  $M_A$  is the mass of electron,  $R_{AB}$  is the distance between nuclei A and B,  $r_{ij}$  is the distance between electrons i and j,  $r_{iA}$  is the distance between electron *i* and nucleus, and  $\varepsilon_0$  is the permittivity of vacaum.

#### 1.2.2 DFT method

The idea of DFT [21-24] is the investigation of ground-state electronic energy by an electron density that was later confirmed by Hohenberg and Kohn in 1964. Therefore, this experiment is the pertinence between two factors: the electronic energy and electron density.

#### 1.2.2.1 The Kohn-Sham formalism

The main problem of DFT concept is to describe how kinetic energy reacts in the system. The idea of kinetic energy function can be calculated into two terms; Firstly the electron itself was considered as non-interacting particles could be precisely estimated and secondly the energy function is a small correction term accounted for electron-electron interactions.

$$E[] = -\frac{1}{2}\sum_{i=1}^{n}\int \Psi_{i}^{*}(r_{1})\nabla_{i}^{2}\Psi_{i}(r_{1})dr_{1} - \sum_{i=1}^{N}\int \frac{1}{r_{i}}(r_{1})dr_{1} + \frac{1}{2}\iint \frac{p(r_{1})(r_{2})}{r_{12}}dr_{1}dr_{2} + E^{C}[], \qquad (1.3)$$

where  $\Psi_i$  (*i* = 1,2,3,...,n) are the Kohn-Sham orbitals, n is the number of electrons, N is the number of nuclei. The first term of the equation (1.3) accounts for the kinetic energy of the noninteracting electrons, the second term represents the nuclear-electron interactions, the third term known as the Coulombic repulsions between the total charge distributions and the fourth term corresponds to the exchange correlation which represents the correction of kinetic energy from the interacting repulsion between electron-electron.

As set of one-electron orbitals, the ground state electron density (r) can be written

$$\rho(\mathbf{r}) = \sum_{i=1}^{n} |\Psi_i(\mathbf{r})|^2.$$
(1.4)

The Kohn-Sham orbitals are identified by solving the Kohn-Sham equations, given by

$$(\Psi_i)(r_1) = {}_i \Psi_i(r_1),$$
 (1.5)

where  $\varepsilon_i$  is the Kohn-Sham orbital energy, and  $\hat{h}_i$  is the Kohn-Sham Hamiltonian, given by

$$\hat{} = -\frac{1}{2} \nabla_1^2 - \sum_{i=1}^{N} \frac{1}{r_i} + \int \frac{(r_2)}{r_{12}} dr_2 + C(r_1).$$
(1.6)

In equation (1.6) <sup>C</sup> is the functional derivertive of the exchange-correlation energy that can be written as

$$^{C} [] = \frac{E^{C} [}{ . }$$
(1.7)

The exchange-correlation energy (E  $^{\rm C}$  ) is split into two terms that are shown in Equation (1.8)

$${}^{C}[] = [] + {}^{C}[].$$
(1.8)

The first term is exchange term  $(E^X)$  that generally associated with interactions between the same spin electrons and the second term is correlation term  $(E^{C})$  that associated with interactions between opposite spin electrons.

as

#### **1.2.2.2 Hybrid methods**

The most widespread hybrid functional is referred from an exchange-energy functional invented by Becke and Steven that is the introduction of LYP correlation energy. Accordingly this correlation functional called B3LYP functional is as below.

$${}^{B3LYP}_{C} = (1 - a_0 - a_x) {}^{LSDA} + a_0 {}^{HF} + a {}^{B} + (1 - a_0) {}^{N} + a_C {}^{LYP}_{C}.$$
(1.9)

Here <sup>LSDA</sup> is the kind accurate pure DFT the local spin-density approximation (LSDA) non-gradient-corrected exchange functional, <sup>HF</sup> is the Kohn-Sham orbitals based HF exchange energy functional, <sup>B</sup> is the Becke 88 exchange functional

$${}^{B} = {}^{LDA} + {}^{B} ;$$

$${}^{B} = {}^{1/3} \frac{x^{2}}{1+6 \text{ x sinh}^{-1} \text{x}^{2}}$$
(1.10)

The parameter is determined by fitting to known atomic data and x is a dimension gradient variable. The  $^{N}$  is the Vosko, Wilk, Nusair function (VWN) is given by

$$\sum_{n=1}^{LDA} \frac{(1+ax^{2}+bx^{4}+cx^{6})^{1/5}}{x=\left|\frac{\nabla}{4/3}\right|}.$$
 (1.11)

#### 1.2.3 Gaussian basis sets

The basis sets are the mathematical function which used the DFT calculation to describe the electron allocation and model the shape of molecular orbitals and electron density [25]. These orbitals are estimated as linear combinations of the basic functions that

are named linear combination of atomic orbitals approach (LCAO). Nevertheless, the function was not popularly effective in terms of over-cost issue and early numerical calculations were forwarded using Slater-type orbitals (STOs).

$$(\mathbf{r}, \, ) = \frac{(2\zeta/a_0)^{n+1/2}}{[(2n)^{1/2}} \mathbf{r}^{n-1} e^{-\zeta \mathbf{r}/a_0} \mathbf{Y}_1^{\mathbf{m}}(\,, \, ).$$
(1.12)

Further work showed that the cost of calculations can be further reduced if the AOs are expanded in terms of Gaussian functions, which have the form

$$g_{ijk}(r) = Nx^i y^j z^k e^{-r^2}$$
 (1.13)

#### 1.2.3.1 Minimal basis sets

Minimal basis sets carry the minimum number of basis functions needed for each atom that required permanent size atomic type orbitals. The minimal basis sets is based on STO-3G.

$$(2s) = d_{1s}e^{-1sr^{2}} + d_{1s}e^{-1sr^{2}} + d_{1s}e^{-1sr^{2}}$$

$$(2p_{x}) = d_{1p_{x}}e^{-1pr^{2}} + d_{2p_{x}}e^{-2pr^{2}} + d_{3p_{x}}e^{-3pr^{2}}$$

$$(2p_{y}) = d_{1p_{y}}e^{-1pr^{2}} + d_{2p_{y}}e^{-2pr^{2}} + d_{3p_{y}}e^{-3pr^{2}}$$

$$(2p_{z}) = d_{1p_{z}}e^{-1pr^{2}} + d_{2p_{z}}e^{-2pr^{2}} + d_{3p_{z}}e^{-3pr^{2}}$$

## 1.2.3.2 Split-valence basis sets

The problem is treating all electrons as equal, therefore split valence basis sets are designed to explain valence orbitals and core orbitals. In split-valence basis sets, the core electrons can be illustrated with a single STO but in fact the valence electron are used more than one contact GTO. The good example of split-valence basis sets is 6-31G basis set, which comprises of 6 gaussians for inner-shell orbital, 3 gaussians for the first STO of valence orbital and 1 gaussian for the second STO.

#### **1.2.3.3 Polarized functions**

Polarization functions are extra included in basis sets in trying to simulate the polarization effects model as the atom is closely brought together. Therefore this is a reason of electron cloud shape distortion in the neighborhood atom. The polarized basis sets add D function to carbon atoms and P function to hydrogen atoms to calculate the polarization effect. The polarized basis sets for these function has been detailed in to basic set such as 6-31G(d,p).

#### 1.2.3.4 Effective core potentials

Effective core potential (ECP) has been used for the highly performance in the molecular orbital computing that is appropriate for transition metals. ECP is a category of potential function that could be replaced the inner electrons of atomic and molecular systems and calculate only the valence electrons obviously in quantum molecular computing. The concept was approved the precision of data calculating compared with experimental results and those from an expensive all electron basis sets.

#### 1.2.4 The chemical indices

The chemical indices are obtained by the density calculation. These indices show the specific properties of a chemical species [26].

#### 1.2.4.1 Electronic chemical potential

The chemical potential of the DFT [27], which is variational the principle of equation (1.15), is a very small one-electron energy that is smaller than the total electronic energy. It gets into the variational principle of traditional quantum chemistry.

$$\delta\left\{E\left[\eta\left(r\right)\right]-\mu\left[N[n(r)]\right]\right\}=0,$$
(1.15)

where  $\mu$  is a electronic chemical potential,  $\eta$  is a chemical hardness and N is a electron number in molecular system.

It has to solve this equation for every  $\mu$ , then taking the  $\mu$  value that makes the correct number of electrons for the system of interest. According to the Lagrangian multipliers,  $\mu$  determines how sensitive the extreme *E* is to change in *N*.



Approximate of  $\mu$  can be computed by the equation (1.17) which ionization potential is *IP* and electron affinity is *EA*.

$$\mu \approx -\frac{1}{2}(IP + EA) \tag{1.17}$$

#### 1.2.4.2 Mulliken electronegativity

The Milliken electronegativity  $(\chi)$  [26] is a negative of chemical potential in DFT, shown by equation as:



#### 1.2.4.3 Chemical hardness

The hardness  $(\eta)$  [28-30] can be described as a resistance to charge transfer. *E* versus *N* plot is not straight lines, but is generally convex upward. Their curvatures define another property of substantial importance.

$$\eta = \left(\frac{\partial^2 E}{\partial N^2}\right)_{V(\bar{r})}$$
(1.19)

The finite-difference approximation is expressed in equation (1.20). It can be written as

$$\eta \approx -\frac{1}{2} (IP - EA). \tag{1.20}$$

#### **1.2.4.4 Electrophilicity**

The electrophilicity  $(\omega)$  index [31] is used to describe a reliable property of a chemical system and may be used as quantum chemical descriptor. The operational definition is expressed by term of electrophilicity index may be written as

$$\omega = \frac{\mu^2}{2\eta}.$$
(1.21)

#### **1.2.4.5 Dipole moment**

The asymmetry of a charge distribution is determined by the physical property which is the dipole moment. The dipole moment is shown as the product of the total amount of positive or negative charge and the distance between their centroids. The unit for dipole moments is called a Debye.

#### 1.2.5 Thermodynamic properties

The basic equations used to describe thermochemical quantities [32] such as enthalpy, free energy and rate of reaction.

#### 1.2.5.1 Enthalpies and Gibbs free energies of reaction

The different of the sums of heats of formation is taken to calculate the enthalpies of reaction using this equation

$$\Delta_r H^{\circ}(298K) = \sum_{prod} \Delta_f H^{\circ}_{prod}(298K) - \sum_{react} \Delta_f H^{\circ}_{react}(298K).$$
(1.22)

However, there is the way to simply take different of the sums of heats of formation for reactant and the products. Gaussian program provides the short cut to calculate the enthalpy of reaction is defined as

$$\Delta_r H^{\circ}(298K) = \sum_{prod} (\varepsilon_0 + H_{corr})_{prod} - \sum_{react} (\varepsilon_0 + H_{corr})_{react}, \qquad (1.23)$$

where  $\varepsilon_0$  for the total electronic energy.  $H_{corr}$  is correction to the enthalpy due to internal energy which can be calculated by

$$H_{corr} = E_{tot} + k_B T , \qquad (1.24)$$

where  $E_{tot}$  (total internal energy) is the sum of  $E_t, E_r, E_v, E_e$  (internal energy due to translation, rotational, vibrational and electronic motion, respectively).

$$E_{tot} = E_t + E_r + E_v + E_e.$$
(1.25)

Likewise, Gibbs free energies of reaction can be calculated by the same short cut:

$$\Delta_r G^{\circ}(298K) = \sum_{prod} (\varepsilon_0 + G_{corr})_{prod} - \sum_{react} (\varepsilon_0 + G_{corr})_{react}, \qquad (1.26)$$

where the correction to the Gibbs free energy due to internal energy  $(G_{corr})$  can be calculated by

$$G_{corr} = H_{corr} - TS_{tot}, \qquad (1.27)$$

$$S_{tot} = S_t + S_r + S_v + S_e, (1.28)$$

where  $S_{tot}$  (total internal entropy) is the sum of  $S_t, S_r, S_v, S_e$  (entropy due to translation, rotational, vibrational and electronic motion, respectively).

#### 1.2.5.2 Rate of reaction

The rate of reaction (k(T)) is defined by equation:

$$k(T) = \frac{k_B T}{hc^{\circ}} e^{-\Delta G^{\circ}/RT}, \qquad (1.29)$$

where  $k_B$  is the Boltzmann's constant, h is Plank's constant, T is the absolute temperature, R is the gas constant,  $c^\circ = 1$  for the concentration.

#### 1.3 Objective

The adsorptions of diatomic gases (H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, CO, NO), triatomic gases (CO<sub>2</sub>, N<sub>2</sub>O, NO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub>S, SO<sub>2</sub>), polyatomic gases (C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CH<sub>4</sub>, NH<sub>3</sub>) on CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> have been studied. The reduction process of CeO<sub>2</sub> to CeO by H<sub>2</sub> gas have been investigated. Electronic properties and thermodynamic properties of all reactions have been obtained and reported.

#### **CHAPTER II**

#### **COMPUTATIONAL DETAILS**

#### 2.1 Computational methods

The quantum chemical calculations have been performed with B3LYP method, the Becke's three-parameter hybrid functional [33] combined with the Lee-Yang-Parr correlation functional [34], using Stuttgart RSC ANO/ECP basis set for cerium atom and 6-31G(d) for other atoms. All calculations were performed with the Gaussian 09 program [35].

#### 2.2 Definitions of reaction terms

#### 2.2.1 Adsorption of small gases on cerium oxide

The adsorption energy ( $\Delta E_{ads}$ ) for gas molecules adsorbed on the cerium oxide has been computed by the equation (2.1)

$$\Delta E_{\rm ads} = E_{\rm gas/cerium \, oxide} - \left( E_{\rm cerium \, oxide} + E_{\rm gas} \right), \tag{2.1}$$

where  $E_{\text{gas/cerium oxide}}$ ,  $E_{\text{cerium oxide}}$  and  $E_{\text{gas}}$  are total energies of gas adsorption structure on

cerium oxide and gas molecule, respectively.

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#### 2.2.2 Thermodynamic quantities

The standard enthalpy  $\Delta H_{298}$  and Gibbs free energy changes  $\Delta G_{298}$  of adsorption of hydrogen molecule onto CeO<sub>2</sub> have been derived from the frequency calculations at the same level of theory. The equilibrium constant (*K*) was computed using formula,  $\exp(-\Delta G_{298}/RT)$ 

#### **CHAPTER III**

#### **RESULTS AND DISCUSSIONS**

In the present study, adsorptions of diatomic gases (H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, CO, NO), triatomic gases (CO<sub>2</sub>, N<sub>2</sub>O, NO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub>S, SO<sub>2</sub>) and polyatomic gases (C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CH<sub>4</sub>, NH<sub>3</sub>) on the CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> cluster and the reduction reaction of CeO<sub>2</sub> by H<sub>2</sub> gas, were mainly investigated. Therefore, three sections of results are presented.

#### 3.1 The optimized structures

The B3LYP/GEN-optimized structures of  $CeO_2$  and  $Ce_2O_4$  obtained by full geometry optimizations are shown in Figure 3.1.



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Figure 3.1 The B3LYP/GEN-optimized structures of (a) CeO<sub>2</sub> and (b) trans-Ce<sub>2</sub>O<sub>4</sub>.

#### 3.2 Adsorption of single molecule of gases on the CeO2 and Ce2O4 clusters

#### 3.2.1 Adsorption of gases on the CeO<sub>2</sub>

The B3LYP/GEN-optimized structures of adsorption configurations of diatomic gases (H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, CO, NO), triatomic gases (CO<sub>2</sub>, N<sub>2</sub>O, NO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub>S, SO<sub>2</sub>), polyatomic gases (C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CH<sub>4</sub>, NH<sub>3</sub>) on CeO<sub>2</sub> are shown in Figure 3.2. It shows that diatomic gases adsorption structure pointing their atom-end toward Ce atom except H<sub>2</sub> whose H-H bond is

perpendicular to Ce atom of CeO<sub>2</sub>. The CO<sub>2</sub>/CeO<sub>2</sub> adsorption structure, suggests that CO<sub>2</sub> point its oxygen atom toward Ce atom of CeO<sub>2</sub> molecule. The N<sub>2</sub>O/CeO<sub>2</sub> adsorption structure has two configurations. One is of pointing its N-end toward Ce atom of CeO<sub>2</sub>. O-N bond parallel to Ce-O bond of CeO<sub>2</sub> molecule. Another one is of the pointing its oxygen atom toward Ce atom and nitrogen atom toward oxygen atom. The adsorption structure of NO<sub>2</sub> suggests that N-O bond is approximately perpendicular to Ce atom of CeO<sub>2</sub> structure. The H<sub>2</sub>O/CeO<sub>2</sub> adsorption structure suggests that O-H bond of water parallel to Ce-O bond of CeO<sub>2</sub> molecule. The adsorption atom toward Ce atom and hydrogen atom toward O atom of CeO<sub>2</sub> molecule. The adsorption structure of H<sub>2</sub>S suggests that their molecular planes are parallel. The adsorption structure of SO<sub>2</sub> suggests that C=C bond of C<sub>2</sub>H<sub>4</sub> are perpendicular to Ce atom, CH<sub>4</sub> suggests that its two hydrogen atoms point toward Ce atom and NH<sub>3</sub> sugests that its nitrogen atom point toward Ce atom of CeO<sub>2</sub> molecule.

The energy gaps and chemical indices of  $CeO_2$  and its gas adsorption configurations are shown in Table 3.1. The energy gaps of  $CeO_2$  cluster largely decreased after adsorptions of  $O_2$  and NO gases. The energy gaps of other gases adsorptions with  $CeO_2$  were also not much different from its corresponding bare cluster.

Adsorption abilities of CeO<sub>2</sub> with diatomic, triatomic and polyatomic gases are in orders :  $O_2(\Delta E_{ads} = -17.83 \text{ kcal/mol}) > NO$  its N-end toward ( $\Delta E_{ads} = -7.39 \text{ kcal/mol}) > CO$  its C-end toward ( $\Delta E_{ads} = -7.04 \text{ kcal/mol}) > CO$  its O-end toward ( $\Delta E_{ads} = -3.77 \text{ kcal/mol}) > NO$  its O-end toward ( $\Delta E_{ads} = -3.50 \text{ kcal/mol}) > N_2$  ( $\Delta E_{ads} = -3.30 \text{ kcal/mol}) > H_2$  ( $\Delta E_{ads} = -1.66 \text{ kcal/mol}$ ), H<sub>2</sub>O ( $\Delta E_{ads} = -51.45 \text{ kcal/mol}) > NO_2$  ( $\Delta E_{ads} = -47.91 \text{ kcal/mol}) > SO_2$  ( $\Delta E_{ads} = -15.85 \text{ kcal/mol}) > H_2S$  ( $\Delta E_{ads} = -7.52 \text{ kcal/mol}) > CO_2$  ( $\Delta E_{ads} = -5.16 \text{ kcal/mol}) > N_2O$  its O-end toward ( $\Delta E_{ads} = -4.87 \text{ kcal/mol}) > N_2O$  its N-end toward ( $\Delta E_{ads} = -4.26 \text{ kcal/mol})$ ) and NH<sub>3</sub> ( $\Delta E_{ads} = -19.62 \text{ kcal/mol}) > C_2H_2$  ( $\Delta E_{ads} = -10.31 \text{ kcal/mol}) > C_2H_4$  ( $\Delta E_{ads} = -8.50 \text{ kcal/mol}) > CH_4$  ( $\Delta E_{ads} = -2.43 \text{ kcal/mol})$ ) respectively. Their adsorption energies are shown in Table 3.2.



Figure 3.2. The adsorption configurations of (a)  $H_2$ , (b)  $N_2$ , (c)  $O_2$ , (d) CO (its C-end toward), (e) CO (its O-end toward), (f) NO (its N-end toward), (g) NO (its O-end toward), (h) CO<sub>2</sub>, (i)  $N_2O$  (its N-end toward), (j)  $N_2O$  (its O-end toward), (k)  $NO_2$ , (l)  $H_2O$ , (m)  $H_2S$ , (n) SO<sub>2</sub>, (o)  $C_2H_2$ , (p)  $C_2H_4$ , (q) CH<sub>4</sub>, (r) NH<sub>3</sub> on CeO<sub>2</sub> cluster, computed at the B3LYP/GEN method. Their bond distances are in Å.

Compound	$E_{\rm HOMO}{}^{\rm a}$	$E_{\text{LUMO}}^{a}$	$\Delta E_{\rm gap}{}^{\rm a}$	$\mu^{ m b}$	$\chi^{c}$	$\eta^{ ext{d}}$	ω <sup>e</sup>
CeO <sub>2</sub>	-6.006	-1.604	4.402	-3.805	3.805	2.201	3.289
Diatomic							
$H_2/CeO_2$	-5.962	-1.274	4.688	-3.618	3.618	2.344	2.792
$N_2/CeO_2$	-5.838	-2.184	3.654	-4.011	4.011	1.827	4.403
$O_2/CeO_2$	-7.083	-5.121	1.962	-6.102	6.102	0.981	18.976
<u>C</u> O/CeO <sub>2</sub>	-5.806	-2.338	3.468	-4.072	4.072	1.734	4.780
CO/CeO <sub>2</sub>	-5.805	-1.921	3.884	-3.863	3.863	1.942	3.841
<u>N</u> O/CeO <sub>2</sub>	-6.261	-4.178	2.083	-5.220	5.220	1.042	13.079
NO/CeO2	-5.968	-4.195	1.773	-5.082	5.082	0.886	14.568
Triatomic	L				24		
$CO_2/CeO_2$	-5.673	-1.216	<mark>4.4</mark> 58	-3.444	3.444	2.229	2.661
$ON_2/CeO_2$	-5.711	-1.978	3.733	-3.845	3.845	1.867	3.959
N2O/CeO2	-5.818	-1.362	4.456	-3.590	3.590	2.228	2.893
$O_2 N/CeO_2$	-7.419	-2.699	4.720	-5.059	5.059	2.360	5.423
H <sub>2</sub> O/CeO <sub>2</sub>	-5.697	-1.177	4.521	-3.437	3.437	2.260	2.613
H <sub>2</sub> S/CeO <sub>2</sub>	-5.621	-1.142	4.479	-3.382	3.382	2.240	2.553
SO <sub>2</sub> /CeO <sub>2</sub>	-6.723	-2.799	3.923	-4.761	4.761	1.962	5.777
Polyatomic		W CAR		1			
$C_2H_2/CeO_2$	-5.654	-0.998	4.657	-3.326	3.326	2.328	2.376
$C_2H_4/CeO_2$	-5.667	-1.177	4.490	-3.422	3.422	2.245	2.608
CH <sub>4</sub> /CeO <sub>2</sub>	-5.843	-1.284	4.560	-3.563	3.563	2.280	2.785
H <sub>3</sub> N/CeO <sub>2</sub>	-5.187	-0.956	4.231	-3.072	3.072	2.116	2.230

**Table 3.1.** Energy gap and chemical indices of CeO<sub>2</sub> cluster and its gas adsorptions, computed at the DFT/B3LYP/GEN method.

compound	ЕНОМОа	ELUMOa	ΔΕγαπα	μβ	XX	$\eta\delta$	Œ
CeO2	-6.006	-1.604	4.402	-3.805	3.805	2.201	3.289
Diatomic							
H2/CeO2	-5.962	-1.274	4.688	-3.618	3.618	2.344	2.792
N2/CeO2	-5.838	-2.184	3.654	-4.011	4.011	1.827	4.403
O2/CeO2	-7.083	-5.121	1.962	-6.102	6.102	0.981	18.976
CO/CeO2	-5.806	-2.338	3.468	-4.072	4.072	1.734	4.780
CO/CeO2	-5.805	-1.921	3.884	-3.863	3.863	1.942	3.841
<u>NO</u> /CeO2	-6.261	-4.178	2.083	-5.220	5.220	1.042	13.079
NO/CeO2	-5.968	-4.195	1.773	-5.082	5.082	0.886	14.568
Triatomic							
CO2/CeO2	-5.673	-1.216	4.458	-3.444	3.444	2.229	2.661
ON2/CeO2	-5.711	-1.978	3.733	-3.845	3.845	1.867	3.959

N2O/CeO2	-5.818	-1.362	4.456	-3.590	3.590	2.228	2.893
O2N/CeO2	-7.419	-2.699	4.720	-5.059	5.059	2.360	5.423
H2O/CeO2	-5.697	-1.177	4.521	-3.437	3.437	2.260	2.613
H2S/CeO2	-5.621	-1.142	4.479	-3.382	3.382	2.240	2.553
SO2/CeO2	-6.723	-2.799	3.923	-4.761	4.761	1.962	5.777
Polyatomic							
C2H2/CeO2	-5.654	-0.998	4.657	-3.326	3.326	2.328	2.376
<sup>a</sup> In eV.							

<sup>b</sup> Electronic chemical potential,  $\mu = (E_{HOMO} + E_{LUMO})/2$ 

<sup>c</sup> The Mulliken electronegativity index,  $\chi = -(E_{HOMO} + E_{LUMO})/2$ 

<sup>d</sup> Chemical hardness,  $\eta = (E_{\text{LUMO}} - E_{\text{HOMO}})/2$ ,  $\eta = E_{\text{gap}}/2$ 

<sup>e</sup> The electrophilicity index,  $\omega = \mu^2/2\eta$ 



	Gases adsorption					
Diaton	nic					
CeO <sub>2</sub>	+	$H_2$	$\rightarrow$	$H_2/CeO_2$	-1.66	
$CeO_2$	+	$N_2$	$\rightarrow$	$N_2/CeO_2$	-3.30	
$CeO_2$	+	$O_2$	$\rightarrow$	O <sub>2</sub> /CeO <sub>2</sub>	-17.83	
$CeO_2$	+	CO	$\rightarrow$	<u>C</u> O/CeO <sub>2</sub>	-7.04	
$CeO_2$	+	CO	$\rightarrow$	CO/CeO <sub>2</sub>	-3.77	
$CeO_2$	+	NO	$\rightarrow$	<u>N</u> O/CeO <sub>2</sub>	-7.39	
$CeO_2$	+	NO	$\rightarrow$	NO/CeO <sub>2</sub>	-3.50	
Triator	nic			- Min		
$CeO_2$	+	$CO_2$	$\rightarrow$	$CO_2/CeO_2$	-5.16	
$CeO_2$	+	$N_2O$	$\rightarrow$	ON <sub>2</sub> /CeO <sub>2</sub>	-4.26	
$CeO_2$	+	$N_2O$	$\rightarrow$	N <sub>2</sub> O/CeO <sub>2</sub>	-4.87	
$CeO_2$	+	$NO_2$	$\rightarrow$	O <sub>2</sub> <u>N</u> /CeO <sub>2</sub>	-47.91	
$CeO_2$	+	$H_2O$	$\rightarrow$	H <sub>2</sub> O/CeO <sub>2</sub>	-51.45	
$CeO_2$	+	$H_2S$	$\rightarrow$	H <sub>2</sub> S/CeO <sub>2</sub>	-7.52	
$CeO_2$	+	$SO_2$	$\rightarrow$	$SO_2/CeO_2$	-15.85	
Polyate	omic	,		() Surreaction	M Research	
$CeO_2$	+	$C_2H_2$	$\rightarrow$	$C_2H_2/CeO_2$	-10.31	
CeO <sub>2</sub>	+	$C_2H_4$	$\rightarrow$	C <sub>2</sub> H <sub>4</sub> /CeO <sub>2</sub>	-8.50	
CeO <sub>2</sub>	+	$\mathrm{CH}_4$	$\rightarrow$	CH <sub>4</sub> /CeO <sub>2</sub>	-2.43	
CeO <sub>2</sub>	+	$NH_3$	$\rightarrow$	H <sub>3</sub> N/CeO <sub>2</sub>	-19.62	
				TT I	(find	

**Table 3.2** Adsorption energies of diatomic, triatomic and polyatomic gases on the  $CeO_2$ cluster, computed at the B3LYP/GEN method.

<sup>a</sup> In kcal/mol.

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#### 3.2.2 Adsorption of gases on Ce<sub>2</sub>O<sub>4</sub>

The B3LYP/GEN-optimized structures of adsorption configurations of diatomic gases (H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, CO, NO), triatomic gases (CO<sub>2</sub>, N<sub>2</sub>O, NO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub>S, SO<sub>2</sub>), polyatomic gases (C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CH<sub>4</sub>, NH<sub>3</sub>) on Ce<sub>2</sub>O<sub>4</sub> are shown in Figure 3.3. The H<sub>2</sub>/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that H-H bond is perpendicular to Ce atom of Ce<sub>2</sub>O<sub>4</sub>. The adsorption structure of N<sub>2</sub> suggests that its nitrogen atom point toward Ce atom of Ce<sub>2</sub>O<sub>4</sub>. The O<sub>2</sub>/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that O-O bond is perpendicular to Ce atom of Ce<sub>2</sub>O<sub>4</sub>. The  $CO/Ce_2O_4$  adsorption structure suggests that pointing atom-end toward Ce atom of  $Ce_2O_4$ . The NO/Ce<sub>2</sub>O<sub>4</sub> adsorption structure has two configurations. One is of the pointing its N-end toward Ce atom of Ce<sub>2</sub>O<sub>4</sub>. Another one is of the N-O bond is perpendicular to Ce atom of  $Ce_2O_4$ . The adsorption structure of  $CO_2$  suggests that pointing oxygen atom toward Ce atom of Ce<sub>2</sub>O<sub>4</sub>. The N<sub>2</sub>O/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that has two configurations. One is of the pointing its N-end toward Ce atom of Ce<sub>2</sub>O<sub>4</sub>. Another one is of the O-N bond parallel to Ce-O bond of Ce<sub>2</sub>O<sub>4</sub> molecule by pointing its oxygen atom toward Ce atom and nitrogen atom toward oxygen atom. The NO<sub>2</sub>/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that N-O bond is approximately parallel to Ce-O bond of Ce<sub>2</sub>O<sub>4</sub> molecule by pointing its oxygen atom toward Ce atom and nitrogen atom toward Ce atom. The adsorption structure of water suggests that its oxygen atom point toward Ce atom. The H<sub>2</sub>S/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that its hydrogen atom point toward oxygen atom of Ce<sub>2</sub>O<sub>4</sub>. The SO<sub>2</sub>/Ce<sub>2</sub>O<sub>4</sub> adsorption structure suggests that S=O bond is parallel to Ce-O bond of Ce<sub>2</sub>O<sub>4</sub> by pointing its oxygen atom toward Ce atom and sulfer atom toward oxygen atom. The adsorption structure of triatomic gases suggest that C=C bond of  $C_2H_2$  and C=C bond of  $C_2H_4$  are perpendicular to Ce atom, CH<sub>4</sub> suggests that its two hydrogen atoms point toward Ce atom and NH<sub>3</sub> suggests that its nitrogen atom point toward Ce atom of Ce<sub>2</sub>O<sub>4</sub> molecule.

The energy gaps and chemical indices of  $Ce_2O_4$  and its gas adsorption configurations are shown in Table 3.3. The energy gaps of  $Ce_2O_4$  cluster largely decreased after adsorptions of  $O_2$  and NO gases. The energy gaps of other gases adsorptions with  $Ce_2O_4$  were also not much different from its corresponding bare cluster.

Adsorption abilities of Ce<sub>2</sub>O<sub>4</sub> with diatomic, triatomic and polyatomic gases are in orders:  $O_2(\Delta E_{ads} = -8.52 \text{ kcal/mol}) > CO$  its C-end toward ( $\Delta E_{ads} = -6.19 \text{ kcal/mol}) > NO$  its N-end toward ( $\Delta E_{ads} = -3.93 \text{ kcal/mol}) > CO$  its O-end toward ( $\Delta E_{ads} = -3.40 \text{ kcal/mol}) > N_2$ ( $\Delta E_{ads} = -2.67 \text{ kcal/mol}) > NO$  its O-end toward ( $\Delta E_{ads} = -2.29 \text{ kcal/mol}) > H_2$  ( $\Delta E_{ads} = -1.13$  kcal/mol), H<sub>2</sub>O ( $\Delta E_{ads} = -52.45$  kcal/mol) > NO<sub>2</sub> ( $\Delta E_{ads} = -42.02$  kcal/mol) > SO<sub>2</sub> ( $\Delta E_{ads} = -13.87$  kcal/mol) > H<sub>2</sub>S ( $\Delta E_{ads} = -7.14$  kcal/mol) > CO<sub>2</sub> ( $\Delta E_{ads} = -4.85$  kcal/mol) > N<sub>2</sub>O its O-end toward ( $\Delta E_{ads} = -4.32$  kcal/mol) > N<sub>2</sub>O its N-end toward ( $\Delta E_{ads} = -3.71$  kcal/mol) and NH<sub>3</sub> ( $\Delta E_{ads} = -19.65$  kcal/mol) > C<sub>2</sub>H<sub>2</sub> ( $\Delta E_{ads} = -8.66$  kcal/mol) > C<sub>2</sub>H<sub>4</sub> ( $\Delta E_{ads} = -7.94$  kcal/mol) > CH<sub>4</sub> ( $\Delta E_{ads} = -2.13$  kcal/mol) respectively. Their adsorption energies are shown in Table 3.4.





Figure 3.3. The adsorption configurations of (a)  $H_2$ , (b)  $N_2$ , (c)  $O_2$ , (d) CO (its C-end toward), (e) CO (its O-end toward), (f) NO (its N-end toward), (g) NO (its O-end toward), (h) CO<sub>2</sub>, (i)  $N_2O$  (its N-end toward), (j)  $N_2O$  (its O-end toward), (k)  $NO_2$ , (l)  $H_2O$ , (m)  $H_2S$ , (n) SO<sub>2</sub>, (o)  $C_2H_2$ , (p)  $C_2H_4$ , (q) CH<sub>4</sub>, (r) NH<sub>3</sub> on Ce<sub>2</sub>O<sub>4</sub> cluster, computed at the B3LYP/GEN method. Their bond distances are in Å.

compound	$E_{\rm HOMO}{}^{\rm a}$	$E_{\rm LUMO}^{a}$	$\Delta E_{ m gap}{}^{ m a}$	$\mu^{ m b}$	$\chi^{c}$	$\eta^{ ext{d}}$	$\omega^{e}$
$Ce_2O_4$	-6.744	-2.032	4.713	-4.388	4.388	2.356	4.086
Diatomic							
$H_2/Ce_2O_4$	-6.706	-1.992	4.715	-4.349	4.349	2.357	4.012
$N_2/Ce_2O_4$	-6.604	-2.338	4.267	-4.471	4.471	2.133	4.685
$O_2/Ce_2O_4$	-7.001	-5.938	1.063	-6.470	6.470	0.531	39.379
$\underline{C}O/Ce_2O_4$	-6.573	-2.488	4.085	-4.530	4.530	2.043	5.024
$CO/Ce_2O_4$	-6.594	-2.101	4.493	-4.347	4.347	2.247	4.206
<u>N</u> O/Ce <sub>2</sub> O <sub>4</sub>	-6.643	-4.490	2.152	-5.566	5.566	1.076	14.395
NO/Ce <sub>2</sub> O <sub>4</sub>	-6.634	-4.261	2.373	-5.448	5.448	1.187	12.503
Triatomic			MA W				
$CO_2/Ce_2O_4$	-6.509	-1.832	<mark>4.6</mark> 77	-4.170	4.170	2.338	3.719
$ON_2/Ce_2O_4$	-6.514	-2.131	4.383	-4.322	4.322	2.192	4.262
$N_2 O/Ce_2 O_4$	-6.625	-1.913	4.712	-4.269	4.269	2.356	3.867
$O_2 \underline{N}/Ce_2 O_4$	-6.777	-3.020	3.757	-4.899	4.899	1.878	6.388
$H_2O/Ce_2O_4$	-6.292	-1.656	4.635	-3.974	3.974	2.318	3.407
H <sub>2</sub> S/Ce <sub>2</sub> O <sub>4</sub>	-6.646	-1.969	4.677	-4.307	4.307	2.339	3.966
$SO_2/Ce_2O_4$	-7.060	-3.066	3.994	-5.063	5.063	1.997	6.417
Polyatomic		1 5	acca())2222	The state of the s			
$C_2H_2/Ce_2O_4$	-6.482	-1.782	4.700	-4.132	4.132	2.350	3.633
$C_2H_4/Ce_2O_4$	-6.478	-1.826	4.652	-4.152	4.152	2.326	3.706
$CH_4/Ce_2O_4$	-6.644	-1.935	4.709	-4.289	4.289	2.355	3.906
H <sub>3</sub> N/Ce <sub>2</sub> O <sub>4</sub>	-6.14 <mark>6</mark>	-1.550	4.596	-3.848	9.848	2.298	3.221

**Table 3.3**. Energy gap and chemical indices of  $Ce_2O_4$  cluster and its gas adsorption on the  $Ce_2O_4$  cluster, computed at the DFT/B3LYP/GEN method.

<sup>a</sup> In eV.

<sup>b</sup> Electronic chemical potential,  $\mu = (E_{\text{HOMO}} + E_{\text{LUMO}})/2$ 

<sup>c</sup> The Mulliken electronegativity index,  $\chi = -(E_{HOMO} + E_{LUMO})/2$ 

<sup>d</sup> Chemical hardness,  $\eta = (E_{\text{LUMO}} - E_{\text{HOMO}})/2$ ,  $\eta = E_{\text{gap}}/2$ 

<sup>e</sup> The electrophilicity index,  $\omega = \mu^2/2\eta$ 

Gases adsorption							
Diatom	ic						
$Ce_2O_4$	+	$H_2$	$\rightarrow$	$H_2/Ce_2O_4$	-1.13		
$Ce_2O_4$	+	$N_2$	$\rightarrow$	$N_2/Ce_2O_4$	-2.67		
$Ce_2O_4$	+	$O_2$	$\rightarrow$	$O_2/Ce_2O_4$	-8.52		
$Ce_2O_4$	+	CO	$\rightarrow$	$\underline{C}O/Ce_2O_4$	-6.19		
$Ce_2O_4$	+	CO	$\rightarrow$	$CO/Ce_2O_4$	-3.40		
$Ce_2O_4$	+	NO	$\rightarrow$	$\underline{N}O/Ce_2O_4$	-3.93		
$Ce_2O_4$	+	NO	$\rightarrow$	NO/Ce <sub>2</sub> O <sub>4</sub>	-2.29		
Triatom	nic						
$Ce_2O_4$	+	$CO_2$	$\rightarrow$	$CO_2/Ce_2O_4$	-4.85		
$Ce_2O_4$	+	$N_2O$	$\rightarrow$	$ON_2/Ce_2O_4$	-3.71		
$Ce_2O_4$	+	$N_2O$	$\rightarrow$	$N_2 O/Ce_2 O_4$	-4.32		
$Ce_2O_4$	+	$NO_2$	$\rightarrow$	$O_2 N/Ce_2 O_4$	-42.02		
$Ce_2O_4$	+	$H_2O$	$\rightarrow$	$H_2O/Ce_2O_4$	-52.45		
$Ce_2O_4$	+	$H_2S$	$\rightarrow$	H <sub>2</sub> S/Ce <sub>2</sub> O <sub>4</sub>	-7.14		
$Ce_2O_4$	+	$SO_2$	$\rightarrow$	$SO_2/Ce_2O_4$	-13.87		
Polyato	mic			Disconstance (o) page ()			
$Ce_2O_4$	+	$C_2H_2$	$\rightarrow$	$C_2H_2/Ce_2O_4$	-8.66		
$Ce_2O_4$	+	$C_2H_4$	$\rightarrow$	$C_2H_4/Ce_2O_4$	-7.94		
$Ce_2O_4$	+	$\mathrm{CH}_4$	$\rightarrow$	CH <sub>4</sub> /Ce <sub>2</sub> O <sub>4</sub>	-2.13		
$Ce_2O_4$	+	$\mathrm{NH}_3$	$\rightarrow$	H <sub>3</sub> N/Ce <sub>2</sub> O <sub>4</sub>	-19.65		
				TT .	(and		

**Table 3.4.** Adsorption energies of diatomic, triatomic and polyatomic gases on the  $Ce_2O_4$  cluster, computed at the B3LYP/GEN method.

<sup>a</sup> In kcal/mol.

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#### 3.3 The reduction of CeO<sub>2</sub> to CeO by H<sub>2</sub> gas.

The reaction considered for H<sub>2</sub> interacting with CeO<sub>2</sub> is the water elimination:

$$CeO_2 + H_2 \rightarrow CeO + H_2O.$$
 (3.1)

This reaction is accompanied by the reduction of the cerium site from formal oxidation state Ce<sup>+4</sup> (f<sup>0</sup>) to Ce<sup>+2</sup> (f<sup>2</sup>). The B3LYP/GEN-optimized structures of CeO<sub>2</sub>, CeO and the related intermediates and transition states are displayed in Figure 3.4. The first step in the reaction is the formation of a  $H_2/CeO_2$  compound 1, followed by the addition of  $H_2$  to the Ce–O bond forming a OCe(H)OH intermediate 2. Next, two paths for the formation of a H<sub>2</sub>O/CeO compound 4 are considered: the concerted pathway of water from OCe(H)OH, or the stepwise pathway by the migration of one hydrogen forming the Ce(OH)<sub>2</sub> intermediate 3. The final step is the elimination of water in the H<sub>2</sub>O/CeO compound 4. Potential energy profile for reduction of CeO<sub>2</sub> to CeO by H<sub>2</sub> gas is also shown in Figure 3.5. It obviously shows that CeO<sub>2</sub> is more energetic preferred than CeO. Energies, thermodynamic properties, rate constants, and equilibrium constants of reduction reaction are shown in Table 3.5. The rate determining steps for the Stepwise pathway and Concerted pathway are 1.02×10<sup>-18</sup> and  $2.73 \times 10^{-23}$  s<sup>-1</sup>, respectively. The overall equilibrium constants for the Stepwise pathway and Concerted pathway are  $3.30 \times 10^{-163}$  are  $2.66 \times 10^{-31}$ , respectively. The overall reaction enthalpies of both pathways are endothermic process. The Gibbs free energy of the reaction is 234.1 kcal/mol. It was found that the CeO<sub>2</sub> reduced to the CeO cluster by H<sub>2</sub> gas is nonspontaneous reaction at 298 K.



Figure 3.4 B3LYP/GEN-optimized structures of CeO<sub>2</sub>, CeO and the related intermediates

and transition states.

**Table 3.5** Energetics, thermodynamic properties, rate constants, and equilibrium constants of reduction reaction of CeO<sub>2</sub> to CeO, computed at the DFT/B3LYP/GEN method.

Reaction	$\Delta E^{\ddagger a}$	$\Delta G^{\ddagger a}$	k <sub>298</sub> <sup>b</sup>	$\Delta E^{\mathrm{a}}$	$\Delta H_{298}{}^{\rm a}$	$\Delta G_{298}{}^{\rm a}$	<i>K</i> <sub>298</sub>
$CeO_2 + H_2 \longrightarrow H_2/CeO_2$	_	_	_	-0.23	-0.50	4.08	1.03×10 <sup>-3</sup>
$H_2/CeO_2 \rightarrow TS1 \rightarrow OCe(H)OH$	22.06	20.72	3.83×10 <sup>-5</sup>	6.60	5.80	8.36	7.43×10 <sup>-7</sup>
Stepwise pathway		(Mag	A Ma				
$OCe(H)OH \rightarrow TS2 \rightarrow Ce(OH)_2$	42.47	42.18	1.02×10 <sup>-18</sup>	16.73	16.61	16.84	4.55×10 <sup>-13</sup>
$Ce(OH)_2 \rightarrow TS3 \rightarrow H_2O/CeO$	35.81	36.46	3.19×10 <sup>-14</sup>	25.48	25.58	24.87	5.85×10 <sup>-19</sup>
$H_2O/CeO \rightarrow CeO + H_2O$	-			185.86	186.03	179.94	1.24×10 <sup>-132</sup>
Concerted pathway							
$OCe(H)$ -OH $\rightarrow$ TS4 $\rightarrow$ H <sub>2</sub> O/CeO	48.61	48.15	2.73×10 <sup>-23</sup>	42.20	42.19	41.71	2.66×10 <sup>-31</sup>
<sup>a</sup> In kcal/mol.		140	(A)	10			
<sup>b</sup> In s <sup>-1</sup> .				1			



Figure 3.5. Potential energy profile for reduction of  $CeO_2$  to CeO by hydrogen gas.

#### **CHAPTER IV**

#### CONCLUSIONS

A theoretical study on the adsorption of diatomic gases, triatomic gases and polyatomic gases on the  $CeO_2$  and  $Ce_2O_4$  clusters for all possible configurations were investigated at the B3LYP/GEN level of theory. All the results can be concluded as follows:

- 1. The adsorption of various gases on  $CeO_2$  and  $Ce_2O_4$  is physisorption.
- The energy gaps of CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> are largely reduced after the adsorptions of O<sub>2</sub> and NO on CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub>.
- 3. The CeO<sub>2</sub> and Ce<sub>2</sub>O<sub>4</sub> are sensitive material for  $O_2$  and NO. they could be developed as sensor based on electrical conductivity.

The reaction process of the CeO<sub>2</sub> reduced to the CeO cluster by H<sub>2</sub> gas was investigated at the B3LYP/GEN level of theory. It was found that the reduction reaction of CeO<sub>2</sub> to CeO by H<sub>2</sub> gas consist of two pathways. The first pathway is the conversion of OCe(H)OH to Ce(OH)<sub>2</sub> before to H<sub>2</sub>O/CeO and the second one is the conversion to H<sub>2</sub>O/CeO. The overall equilibrium constants for the Stepwise pathway and Concerted pathway are  $3.30 \times 10^{-163}$  are  $2.66 \times 10^{-31}$ , respectively. The overall reaction enthalpies of both pathways are endothermic process. It was found that the CeO<sub>2</sub> reduced to the CeO cluster by H<sub>2</sub> gas is non-spontaneous reaction at 298 K.

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