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APPENDICES

Appendix A-1 Case Study 4.1.1 GAMS Code

Set

i Source stream /i1*i3/

j Sink stream /j1*j3/

;

Parameter

SA Source concentration A (ppm)

/i1 15

i2 120

i3 220/

SB Source concentration B (ppm)

/i1 400

i2 12500

i3 45/

SC Source concentration C (ppm)

/i1 35

i2 180

i3 9500/

FS Source flowrate (ton per hour)

/i1 45

i2 34

i3 56/

DMA Sink Maximum concentration A (ppm)

/j1 0

j2 20

j3 120/

DMB Sink Maximum concentration B (ppm)

/j1 0

j2 300

j3 20/

• DMC Sink Maximum concentration C (ppm)

/j1 0

j2 45

j3 200/

FD Sink flowrate (ton per hour)

/j1 45

j2 34

j3 56/

Variable OBJ Objective function

Positive variable $x(i,j)$ Source split fraction i to j

FW(j) Freshwater flowrate (ton per hour)

WW(i) Waste of each source (ton per hour)

F(i,j) Splitting flowrate i to j (ton per hour)

DA(j) Sink stream concentration A (ppm)

DB(j) Sink stream concentration B (ppm)

DC(j) Sink stream concentration C (ppm)

OFW Overall freshwater (ton per hour)

OWW Overall waste (ton per hour)

Binary variable $y(i,j)$

$z(j)$

Scalar OMEGA /10000/

Equation

| | |
|---------------|-----------------------------|
| MB1(j) | Mass balance (flowrate A) |
| MB2(j) | Mass balance (flowrate B) |
| MB3(j) | Mass balance (flowrate C) |
| MB4(j) | Mass balance (contaminant) |
| Cons1(i) | Constraint for x |
| Cons2(j) | Concentration constraint A |
| Cons3(j) | Concentration constraint B |
| Cons4(j) | Concentration constraint C |
| Flow(i,j) | Flowrate source i to sink j |
| Waste(i) | Waste of each source |
| OFresh | Overall freshwater |
| OWaste | Overall waste |
| Logical1(i,j) | Logical constraint1 |
| Logical2(j) | Logical constraint2 |
| Object | Objective |

$$\begin{aligned}
 & \text{MB1(j)} \dots \sum(i, SA(i) * FS(i) * x(i,j)) = e = DA(j) * FD(j); \\
 & \text{MB2(j)} \dots \sum(i, SB(i) * FS(i) * x(i,j)) = e = DB(j) * FD(j); \\
 & \text{MB3(j)} \dots \sum(i, SC(i) * FS(i) * x(i,j)) = e = DC(j) * FD(j); \\
 & \text{MB4(j)} \dots \sum(i, FS(i) * x(i,j)) + FW(j) = e = FD(j); \\
 & \text{Cons1(i)} \dots \sum(j, x(i,j)) = l = 1; \\
 & \text{Cons2(j)} \dots DA(j) = l = DMA(j); \\
 & \text{Cons3(j)} \dots DB(j) = l = DMB(j); \\
 & \text{Cons4(j)} \dots DC(j) = l = DMC(j); \\
 & \text{Flow(i,j)} \dots F(i,j) = e = FS(i) * x(i,j); \\
 & \text{Waste(i)} \dots WW(i) = e = (1 - \sum(j, x(i,j))) * FS(i); \\
 & \text{OFresh} \dots OFW = e = \sum(j, FW(j)); \\
 & \text{OWaste} \dots OWW = e = \sum(i, WW(i)); \\
 & \text{Logical1(i,j)} \dots F(i,j) - y(i,j) * OMEGA = l = 0; \\
 & \text{Logical2(j)} \dots FW(j) - z(j) * OMEGA = l = 0; \\
 & \text{Object} \dots OBJ = e = OFW + \sum((i,j), y(i,j)) + \sum(j, z(j));
 \end{aligned}$$

Model CASE11/ALL/;
 Solve CASE11 Using MINLP Minimizing OBJ;
 Display OBJ.L, OFW.L, OWW.L, FW.L, WW.L, x.L, F.L, y.L, DA.L, DB.L, DC.L;

**** REPORT SUMMARY : 0 : NONOPT

0 INFEASIBLE

0 UNBOUNDED

0 ERRORS

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows
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General Algebraic Modeling System

Execution

---- 108 VARIABLE OBJ.L = 111.662 Objective function
 VARIABLE OFW.L = 105.662 Overall freshwater (ton per
 hour)
 VARIABLE OWW.L = 105.662 Overall waste (ton per hour)

---- 108 VARIABLE FW.L Freshwater flowrate (ton per hour)
 j1 45.000, j2 8.500, j3 52.162

---- 108 VARIABLE WW.L Waste of each source (ton per hour)
 i1 16.832, i2 34.000, i3 54.831

---- 108 VARIABLE x.L Source split fraction i to j
 j2 j3
 i1 0.567 0.059
 i3 0.021

---- 108 VARIABLE F.L Splitting flowrate i to j (ton per hour)
 j2 j3
 i1 25.500 2.668
 i3 1.169

---- 108 VARIABLE y.L

 j2 j3

i1 1.000 1.000

i3 1.000

---- 108 VARIABLE DA.L Sink stream concentration A (ppm)

j2 11.250, j3 5.308

---- 108 VARIABLE DB.L Sink stream concentration B (ppm)

j2 300.000, j3 20.000

---- 108 VARIABLE DC.L Sink stream concentration C (ppm)

j2 26.250, j3 200.000

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-
WEI

USER: The Petroleum and Petrochemical College G131219:2228AS-WIN

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**** FILE SUMMARY

Appendix B-1 Case Study 4.2.1 GAMS Code

The first model: Non-linear programming (NLP)

Set

i Source stream /i1*i3/

j Sink stream /j1*j3/

;

Parameter

SMA Source concentration of Salts (ppm)

/i1 15

i2 120

i3 220/

SMB Source concentration of Organics (ppm)

/i1 400

i2 12500

i3 45/

SMC Source concentration of H₂S (ppm)

/i1 35

i2 180

i3 9500/

FS Maximun flowrate of fresh water

/i1 45

i2 33.184

i3 54.821/

LA Load of Salts contaminant (kg per hour)

/j1 0.675

j2 3.40

j3 5.60/

LB Load of Organics contaminant (kg per hour)

/j1 18.0

j2 414.80

j3 1.4/

LC Load of H₂S contaminant (kg per hour)

/j1 1.575

j2 4.590

j3 520.8/

DMA Sink Maximum concentration of Salts (ppm)

/j1 0

j2 20

j3 120/

DMB Sink Maximum concentration of Organics (ppm)

/j1 0

j2 300

j3 20/

DMC Sink Maximum concentration of H₂S (ppm)

/j1 0

j2 45

j3 200/

;

Variable OBJ Objective function

;

Positive variable

x(i,j) Source split fraction i to j

FW(j) Freshwater flowrate (ton per hour)

WW(i) Waste of each source (ton per hour)

F(i,j) Splitting flowrate i to j (ton per hour)

DA(j) Sink stream concentration of Salts (ppm)

DB(j) Sink stream concentration of Organics (ppm)

DC(j) Sink stream concentration of H₂S (ppm)

SA(i) Source stream concentration of Salts (ppm)

| | |
|--------------|--|
| SB(i) | Source stream concentration of Organics (ppm) |
| SC(i) | Source stream concentration of H ₂ S (ppm) |
| OFW | Overall freshwater (ton per hour) |
| OWW | Overall waste (ton per hour) |
| LoadA(i,j) | Contaminant load of Salts of Process i to j (gram per hour) |
| LoadB(i,j) | Contaminant load of Organics of Process i to j (gram per hour) |
| LoadC(i,j) | Contaminantload of H ₂ S of Process i to j (gram per hour) |
| Flowin(j) | Total flowrate inlet of Salts contaminant of each process (ton per hour) |
| DeltaCA(i,j) | Outlet concentration - Inlet concentration of Salts contaminant (ppm) |
| DeltaCB(i,j) | Outlet concentration - Inlet concentration of Organics contaminant (ppm) |
| DeltaCC(i,j) | Outlet concentration - Inlet concentration of H ₂ S contaminant (ppm) |

Equation

ConloadA1(i,j) Contaminantload of Salts of Process 1

ConloadA2(i,j) Contaminantload of Salts of Process 2

ConloadA3(i,j) Contaminantload of Salts of Process 3

ConloadB1(i,j) Contaminantload of Organics of Process 1

ConloadB2(i,j) Contaminantload of Organics of Process 2

ConloadB3(i,j) Contaminantload of Organics of Process 3

ConloadC1(i,j) Contaminantload of H₂S of Process 1

ConloadC2(i,j) Contaminantload of H₂S of Process 2

ConloadC3(i,j) Contaminantload of H₂S of Process 3

| | |
|--------------|---|
| MLoadA1(i,j) | Contaminantload balance of Salts of Process 1 |
| MLoadA2(i,j) | Contaminantload balance of Salts of Process 2 |
| MLoadA3(i,j) | Contaminantload balance of Salts of Process 3 |
| MLoadB1(i,j) | Contaminantload balance of Organics of Process 1 |
| MLoadB2(i,j) | Contaminantload balance of Organics of Process 2 |
| MLoadB3(i,j) | Contaminantload balance of Organics of Process 3 |
| MLoadC1(i,j) | Contaminantload balance of H2S of Process 1 |
| MLoadC2(i,j) | Contaminantload balance of H2S of Process 2 |
| MLoadC3(i,j) | Contaminantload balance of H2S of Process 3 |
| TFlowin1(j) | Total flowrate inlet of process 1 |
| TFlowin2(j) | Total flowrate inlet of process 2 |
| TFlowin3(j) | Total flowrate inlet of process 3 |
| FF1 | Constraint for flowrate inlet of process 1 |
| FF2 | Constraint for flowrate inlet of process 2 |
| FF3 | Constraint for flowrate inlet of process 3 |
| MconSA1(i) | Outlet concentration balance of Salts of process 1 |
| MconSA2(i) | Outlet concentration balance of Salts of process 2 |
| MconSA3(i) | Outlet concentration balance of Salts of process 3 |
| MconSB1(i) | Outlet concentration balance of Organics of process 1 |
| MconSB2(i) | Outlet concentration balance of Organics of process 2 |
| MconSB3(i) | Outlet concentration balance of Organics of process 3 |
| MconSC1(i) | Outlet concentration balance of H2S of process 1 |
| MconSC2(i) | Outlet concentration balance of H2S of process 2 |
| MconSC3(i) | Outlet concentration balance of H2S of process 3 |

| | | |
|-----------|------------|--|
| | DCA1(i,j) | Delta concentration of Salts of process 1 |
| | DCA2(i,j) | Delta concentration of Salts of process 2 |
| | DCA3(i,j) | Delta concentration of Salts of process 3 |
| | DCB1(i,j) | Delta concentration of Organics of process 1 |
| | DCB2(i,j) | Delta concentration of Organics of process 2 |
| | DCB3(i,j) | Delta concentration of Organics of process 3 |
| | DCC1(i,j) | Delta concentration of H2S of process 1 |
| | DCC2(i,j) | Delta concentration of H2S of process 2 |
| | DCC3(i,j) | Delta concentration of H2S of process 3 |
| | InconA1(j) | New concentration of water inlet of Salts of process 1 |
| | InconA2(j) | New concentration of water inlet of Salts of process 2 |
| | InconA3(j) | New concentration of water inlet of Salts of process 3 |
| process 1 | InconB1(j) | New concentration of water inlet of Organics of |
| process 2 | InconB2(j) | New concentration of water inlet of Organics of |
| process 3 | InconB3(j) | New concentration of water inlet of Organics of |
| | InconC1(j) | New concentration of water inlet of H2S of process 1 |
| | InconC2(j) | New concentration of water inlet of H2S of process 2 |
| | InconC3(j) | New concentration of water inlet of H2S of process 3 |
| | CBA1(j) | Concentration balance of Salts of process 1 |
| | CBA2(j) | Concentration balance of Salts of process 2 |
| | CBA3(j) | Concentration balance of Salts of process 3 |

| | |
|----------------|--|
| CBB1(j) | Concentration balance of Organics of process 1 |
| CBB2(j) | Concentration balance of Organics of process 2 |
| CBB3(j) | Concentration balance of Organics of process 3 |
| | |
| CBC1(j) | Concentration balance of H2S of process 1 |
| CBC2(j) | Concentration balance of H2S of process 2 |
| CBC3(j) | Concentration balance of H2S of process 3 |
| | |
| Cons1(i) | Constraint for x |
| Flowsplit(i,j) | Splited flowrate source i to sink j |
| OFresh | Overall freshwater |
| Object | Objective |

;

*Contaminantload of each process

ConloadA1('i1','j1') .. LoadA('i1','j1') =e= 1000*LA('j1');

ConloadA2('i2','j2') .. LoadA('i2','j2') =e= 1000*LA('j2');

ConloadA3('i3','j3') .. LoadA('i3','j3') =e= 1000*LA('j3');

ConloadB1('i1','j1') .. LoadB('i1','j1') =e= 1000*LB('j1');

ConloadB2('i2','j2') .. LoadB('i2','j2') =e= 1000*LB('j2');

ConloadB3('i3','j3') .. LoadB('i3','j3') =e= 1000*LB('j3');

ConloadC1('i1','j1') .. LoadC('i1','j1') =e= 1000*LC('j1');

ConloadC2('i2','j2') .. LoadC('i2','j2') =e= 1000*LC('j2');

ConloadC3('i3','j3') .. LoadC('i3','j3') =e= 1000*LC('j3');

*Contaminantload balance of each process

MLoadA1('i1','j1')..LoadA('i1','j1')=e=Flowin('j1')*DeltaCA('i1','j1');

MLoadA2('i2','j2')..LoadA('i2','j2')=e=Flowin('j2')*DeltaCA('i2','j2');

MLoadA3('i3','j3')..LoadA('i3','j3')=e=Flowin('j3')*DeltaCA('i3','j3');

$M\text{LoadB1}(i1',j1')..LoadB(i1',j1')=e=Flowin(j1')*\Delta CB(i1',j1')$;
 $M\text{LoadB2}(i2',j2')..LoadB(i2',j2')=e=Flowin(j2')*\Delta CB(i2',j2')$;
 $M\text{LoadB3}(i2',j3')..LoadB(i3',j3')=e=Flowin(j3')*\Delta CB(i3',j3')$;

$M\text{LoadC1}(i1',j1')..LoadC(i1',j1')=e=Flowin(j1')*\Delta CC(i1',j1')$;
 $M\text{LoadC2}(i2',j2')..LoadC(i2',j2')=e=Flowin(j2')*\Delta CC(i2',j2')$;
 $M\text{LoadC3}(i2',j3')..LoadC(i3',j3')=e=Flowin(j3')*\Delta CC(i3',j3')$;

*Total inlet flowrate of each process

$T\text{Flowin1}(j1')..Flowin(j1')=e=\sum(i,FS(i)*x(i,j1'))+FW(j1')$;
 $T\text{Flowin2}(j2')..Flowin(j2')=e=\sum(i,FS(i)*x(i,j2'))+FW(j2')$;
 $T\text{Flowin3}(j3')..Flowin(j3')=e=\sum(i,FS(i)*x(i,j3'))+FW(j3')$;

*Constraint for flowrate inlet of each process

$FF1..Flowin(j1')=g=FS(i1')$;
 $FF2..Flowin(j2')=g=FS(i2')$;
 $FF3..Flowin(j3')=g=FS(i3')$;

*Outlet concentration of each process

$M\text{conSA1}(i1')..LA(j1')*1000=e=FS(i1')*SA(i1')$;
 $M\text{conSA2}(i2')..LA(j2')*1000=e=FS(i2')*SA(i2')$;
 $M\text{conSA3}(i3')..LA(j3')*1000=e=FS(i3')*SA(i3')$;

$M\text{conSB1}(i1')..LB(j1')*1000=e=FS(i1')*SB(i1')$;
 $M\text{conSB2}(i2')..LB(j2')*1000=e=FS(i2')*SB(i2')$;
 $M\text{conSB3}(i3')..LB(j3')*1000=e=FS(i3')*SB(i3')$;

$M\text{conSC1}(i1')..LC(j1')*1000=e=FS(i1')*SC(i1')$;
 $M\text{conSC2}(i2')..LC(j2')*1000=e=FS(i2')*SC(i2')$;
 $M\text{conSC3}(i3')..LC(j3')*1000=e=FS(i3')*SC(i3')$;

*Delta concentration of each process

$$DCA1('i1','j1') \dots \Delta CA('i1','j1') = e = (SA('i1') - DA('j1'));$$

$$DCA2('i2','j2') \dots \Delta CA('i2','j2') = e = (SA('i2') - DA('j2'));$$

$$DCA3('i3','j3') \dots \Delta CA('i3','j3') = e = (SA('i3') - DA('j3'));$$

$$DCB1('i1','j1') \dots \Delta CB('i1','j1') = e = (SB('i1') - DB('j1'));$$

$$DCB2('i2','j2') \dots \Delta CB('i2','j2') = e = (SB('i2') - DB('j2'));$$

$$DCB3('i3','j3') \dots \Delta CB('i3','j3') = e = (SB('i3') - DB('j3'));$$

$$DCC1('i1','j1') \dots \Delta CC('i1','j1') = e = (SC('i1') - DC('j1'));$$

$$DCC2('i2','j2') \dots \Delta CC('i2','j2') = e = (SC('i2') - DC('j2'));$$

$$DCC3('i3','j3') \dots \Delta CC('i3','j3') = e = (SC('i3') - DC('j3'));$$

*New concentration of water inlet

$$\text{InconA1}('j1') \dots DA('j1') * \text{Flowin}('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SA(i));$$

$$CBA1('j1') \dots DA('j1') = l = DMA('j1');$$

$$\text{InconA2}('j2') \dots DA('j2') * \text{Flowin}('j2') = e = \sum(i, FS(i) * x(i, 'j2') * SA(i));$$

$$CBA2('j2') \dots DA('j2') = l = DMA('j2');$$

$$\text{InconA3}('j3') \dots DA('j3') * \text{Flowin}('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SA(i));$$

$$CBA3('j3') \dots DA('j3') = l = DMA('j3');$$

$$\text{InconB1}('j1') \dots DB('j1') * \text{Flowin}('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SB(i));$$

$$CBB1('j1') \dots DB('j1') = l = DMB('j1');$$

$$\text{InconB2}('j2') \dots DB('j2') * \text{Flowin}('j2') = e = \sum(i, FS(i) * x(i, 'j2') * SB(i));$$

$$CBB2('j2') \dots DB('j2') = l = DMB('j2');$$

$$\text{InconB3}('j3') \dots DB('j3') * \text{Flowin}('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SB(i));$$

$$CBB3('j3') \dots DB('j3') = l = DMB('j3');$$

$$\text{InconC1}('j1') \dots DC('j1') * \text{Flowin}('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SC(i));$$

$$CBC1('j1') \dots DC('j1') = l = DMC('j1');$$

$$\text{InconC2}('j2') \dots DC('j2') * \text{Flowin}('j2') = e = \sum(i, FS(i) * x(i, 'j2') * SC(i));$$

$$CBC2('j2') \dots DC('j2') = l = DMC('j2');$$

$$\text{InconC3}('j3') \dots DC('j3') * \text{Flowin}('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SC(i));$$

```

CBC3('j3')..DC('j3')=1=DMC('j3');
Cons1(i)..sum(j,x(i,j))=1=1;
Flowsplit(i,j)..F(i,j)=e=FS(i)*x(i,j);
OFresh..OFW=e=sum(j,FW(j));
Object..OBJ=e=OFW;
DB.lo('j2')=300;
DC.lo('j3')=200;

```

```

Model CASE11/ALL/;
Solve CASE11 Using NLP Minimizing OBJ;
Display LoadA.l, LoadB.l, LoadC.l, Flowin.l, SA.l, SB.l, SC.l, DeltaCA.l,
DeltaCB.l, DeltaCC.l, DA.l, DB.l, DC.l, FW.l, OBJ.l, OFW.l, x.l, F.l;

```

```

**** REPORT SUMMARY :    0  NONOPT
                        1  INFEASIBLE (INFES)
                        SUM 10200.000
                        MAX 10200.000
                        MEAN 10200.000
                        0  UNBOUNDED
                        0  ERRORS

```

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows

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General Algebraic Modeling System

Execution

```

---- 275 VARIABLE LoadA.L Contaminantload of Salts of Process i to j (gram p
           er hour)
           j1    j2    j3
i1  675.000
i2      3400.000
i3      5600.000

```


---- 275 VARIABLE LoadB.L Contaminantload of Organics of Process i to j

j1 j2 j3

i1 18000.000

i2 414800.000

i3 1400.000

---- 275 VARIABLE LoadC.L Contaminantload of H2S of Process i to j (gram per
hour)

j1 j2 j3

i1 1575.000

i2 4590.000

i3 520800.000

---- 275 VARIABLE Flowin.L Total flowrate inlet of Salts contaminant of each
process (ton per hour)

j1 45.000, j2 34.000, j3 56.000

---- 275 VARIABLE SA.L Source stream concentration of Salts (ppm)

i1 15.000, i2 102.459, i3 102.151

---- 275 VARIABLE SB.L Source stream concentration of Organics (ppm)

i1 400.000, i2 12500.000, i3 25.538

---- 275 VARIABLE SC.L Source stream concentration of H2S (ppm)

i1 35.000, i2 138.320, i3 9500.009

---- 275 VARIABLE DeltaCA.L Outlet concentration - Inlet concentration of Sa
Its contaminant (ppm)

j1 j2 j3

i1 15.000

i2 100.000

i3 100.000

---- 275 VARIABLE DeltaCB.L Outlet concentration - Inlet concentration of Organics contaminant (ppm)

| | j1 | j2 | j3 |
|----|---------|-----------|--------|
| i1 | 400.000 | | |
| i2 | | 12200.000 | |
| i3 | | | 25.000 |

---- 275 VARIABLE DeltaCC.L Outlet concentration - Inlet concentration of H2S contaminant (ppm)

| | j1 | j2 | j3 |
|----|--------|---------|----------|
| i1 | 35.000 | | |
| i2 | | 135.000 | |
| i3 | | | 9300.009 |

---- 275 VARIABLE DA.L Sink stream concentration of Salts (ppm)

j2 2.459, j3 2.151

---- 275 VARIABLE DB.L Sink stream concentration of Organics (ppm)

j2 300.000, j3 0.538

---- 275 VARIABLE DC.L Sink stream concentration of H2S (ppm)

j2 3.320, j3 200.000

---- 275 VARIABLE FW.L Freshwater flowrate (ton per hour)

j1 45.000, j2 33.184, j3 54.821

---- 275 VARIABLE OBJ.L = 133.005 Objective function

VARIABLE OFW.L = 133.005 Overall freshwater (

ton per hour)

---- 275 VARIABLE x.L Source split fraction i to j

| | j2 | j3 |
|----|-------|-------|
| i2 | 0.025 | |
| i3 | | 0.022 |

---- 275 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j2 | j3 |
|----|-------|-------|
| i2 | 0.816 | |
| i3 | | 1.179 |

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-WEI

USER: The Petroleum and Petrochemical College G131219:2228AS-WIN
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**** FILE SUMMARY

Input C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 1 - Initialization step for Water Network.gms

Output C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 1 - Initialization step for Water Network.lst

The second model: Mixed-integer non-linear programming (MINLP)

Set

i Source stream /i1*i3/

j Sink stream /j1*j3/

;

Parameter

SA Source concentration A (ppm)

/i1 15

i2 120

i3 220/

SB Source concentration B (ppm)

/i1 400

i2 12500

i3 45/

SC Source concentration C (ppm)

/i1 35

i2 180

i3 9500/

DMA Sink Maximum concentration A (ppm)

/j1 0

j2 20

j3 120/

DMB Sink Maximum concentration B (ppm)

/j1 0

j2 300

j3 20/

DMC Sink Maximum concentration C (ppm)

/j1 0

j2 45

j3 200/

;

Variable OBJ Objective function

;

Positive variable $x(i,j)$ Source split fraction i to j
 FW(j) Freshwater flowrate (ton per hour)
 WW(i) Waste of each source (ton per hour)
 FS(i) Flowrate outlet (ton per hour)
 FD(j) Flowrate inlet (ton per hour)
 F(i,j) Splitting flowrate i to j (ton per hour)
 DA(j) Sink stream concentration A (ppm)
 DB(j) Sink stream concentration B (ppm)
 DC(j) Sink stream concentration C (ppm)
 OFW Overall freshwater (ton per hour)
 OWW Overall waste (ton per hour)
 FWCost Total cost of freshwater (\$ per y)
 nXCost Total cost of water splitting units (\$)
 nFCost Total cost of water feeding units (\$)
 OCost Total operating cost (\$ per year)

;

Binary variable $y(i,j)$
 $z(j)$

;

Scalar OMEGA /10000/
 HY /8400/
 CostFW /2.00/
 CostnX /10000/
 CostnF /10000/

;

Equation

***** Water Network

MB1(j) Mass balance (flowrate A)

MB2(j) Mass balance (flowrate B)
 MB3(j) Mass balance (flowrate C)
 MB4(j) Mass balance (contaminant)
 Cons1(i) Constraint for x
 Cons2(j) Concentration constraint A
 Cons3(j) Concentration constraint B
 Cons4(j) Concentration constraint C
 Cons5(i,j) Constraint for water flowrate
 Flow(i,j) Flowrate source i to sink j
 Waste(i) Waste of each source
 OFresh Overall freshwater
 OWaste Overall waste

***** Number of units

Logical1(i,j) Logical constraint1
 Logical2(j) Logical constraint2

***** Cost

CostofFW Total cost of Fresh water
 CostofnX Total cost of water splitting units
 CostofnF Total cost of water feeding units
 CostofO Total cost of operation

***** Minimizing

Object Objective

;

***** Water Network

MB1(j)..sum(i,SA(i)*FS(i)*x(i,j))=e=DA(j)*FD(j);

MB2(j)..sum(i,SB(i)*FS(i)*x(i,j))=e=DB(j)*FD(j);

MB3(j)..sum(i,SC(i)*FS(i)*x(i,j))=e=DC(j)*FD(j);

$MB4(j) \cdot \sum(i, FS(i) \cdot x(i,j)) + FW(j) = e = FD(j);$
 $Cons1(i) \cdot \sum(j, x(i,j)) = l = 1;$
 $Cons2(j) \cdot DA(j) = l = DMA(j);$
 $Cons3(j) \cdot DB(j) = l = DMB(j);$
 $Cons4(j) \cdot DC(j) = l = DMC(j);$
 $Cons5(i,j) \$ (ord(i) \text{ eq } ord(j)) \cdot FS(i) = e = FD(j);$
 $Flow(i,j) \cdot F(i,j) = e = FS(i) \cdot x(i,j);$
 $Waste(i) \cdot WW(i) = e = (1 - \sum(j, x(i,j))) \cdot FS(i);$
 $OFresh \cdot OFW = e = \sum(j, FW(j));$
 $OWaste \cdot OWW = e = \sum(i, WW(i));$

***** Number of units

$Logical1(i,j) \cdot F(i,j) - y(i,j) \cdot OMEGA = l = 0;$
 $Logical2(j) \cdot FW(j) - z(j) \cdot OMEGA = l = 0;$

***** Cost

$CostofFW \cdot FWCost = e = OFW \cdot CostFW \cdot HY;$
 $CostofnX \cdot nXCost = e = \sum((i,j), y(i,j)) \cdot CostnX;$
 $CostofnF \cdot nFCost = e = \sum(j, z(j)) \cdot CostnF;$
 $CostofO \cdot OCost = e = FWCost;$

***** Minimizing

$Object \cdot OBJ = e = FWCost + nXCost + nFCost;$
 $FS.lo('i1') = 45;$
 $FS.lo('i2') = 34;$
 $FS.lo('i3') = 56;$

Model CASE11/ALL/;

Solve CASE11 Using MINLP Minimizing OBJ;

Display OBJ.l, OCost.l, OFW.l, OWW.l, FW.l, WW.l, FS.l, FD.l, x.l, F.l, y.l,
DA.l, DB.l, DC.l, FWCost.l, nXCost.l, nFCost.l;

**** REPORT SUMMARY : 0 NONOPT

0 INFEASIBLE

0 UNBOUNDED

0 ERRORS

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows

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General Algebraic Modeling System

Execution

---- 137 VARIABLE OBJ.L = 1835128.478 Objective function

VARIABLE OCost.L = 1775128.478 Total operating cost
(\$ per year)

VARIABLE OFW.L = 105.662 Overall freshwater (
ton per hour)

VARIABLE OWW.L = 105.662 Overall waste (ton pe
r hour)

---- 137 VARIABLE FW.L Freshwater flowrate (ton per hour)

j1 45.000, j2 8.500, j3 52.162

---- 137 VARIABLE WW.L Waste of each source (ton per hour)

i1 16.832, i2 34.000, i3 54.831

---- 137 VARIABLE FS.L Flowrate outlet (ton per hour)

i1 45.000, i2 34.000, i3 56.000

---- 137 VARIABLE FD.L Flowrate inlet (ton per hour)

j1 45.000, j2 34.000, j3 56.000

---- 137 VARIABLE x.L Source split fraction i to j

j2 j3

i1 0.567 0.059

i3 0.021

---- 137 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j2 | j3 |
|----|--------|-------|
| i1 | 25.500 | 2.668 |
| i3 | | 1.169 |

---- 137 VARIABLE y.L

| | j2 | j3 |
|----|-------|-------|
| i1 | 1.000 | 1.000 |
| i3 | | 1.000 |

---- 137 VARIABLE DA.L Sink stream concentration A (ppm)

j2 11.250, j3 5.308

---- 137 VARIABLE DB.L Sink stream concentration B (ppm)

j2 300.000, j3 20.000

---- 137 VARIABLE DC.L Sink stream concentration C (ppm)

j2 26.250, j3 200.000

---- 137 VARIABLE FWCost.L = 1775128.478 Total cost of freshwater (\$ per y)

VARIABLE nXCost.L = 30000.000 Total cost of water splitting units (\$)

VARIABLE nFCost.L = 30000.000 Total cost of water feeding units (\$)

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-WEI

USER: The Petroleum and Petrochemical College G131219:2228AS-WIN

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**** FILE SUMMARY

Input C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 2 - Water Network with out treatment.gms

Output C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 2 - Water Network with out treatment.lst

Appendix B-2 Case Study 4.2.2 GAMS Code**The second model: Mixed-integer non-linear programming (MINLP)**

Set

i Source stream /i1*i6/

j Sink stream /j1*j6/

;

Parameter

SA Source concentration A (ppm)

/i1 367.5

i2 154.4

i3 80

i4 293.34

i5 220.1111

i6 2375.043/

SB Source concentration B (ppm)

/i1 500

i2 4000

i3 3500

i4 6000

i5 1800

i6 6500/

SC Source concentration C (ppm)

/i1 5655.5

i2 10

i3 175

i4 127.5

i5 340

i6 167.2/

SD Source concentration C (ppm)

i1 1537.5
i2 32
i3 116.65
i4 1096.67
i5 271.2
i6 400/

DMA Sink Maximum concentration A (ppm)

j1 300
j2 10
j3 10
j4 100
j5 85
j6 1000/

DMB Sink Maximum concentration B (ppm)

j1 50
j2 1
j3 1
j4 200
j5 200
j6 1000/

DMC Sink Maximum concentration C (ppm)

j1 5000
j2 0
j3 0
j4 50
j5 300
j6 150/

DMD Sink Maximum concentration D (ppm)

/j1 1500

j2 0

j3 0

j4 1000

j5 200

j6 200/

;

Variable OBJ Objective function

;

Positive variable

$x(i,j)$ Source split fraction i to j

FS(i) Flowrate outlet (ton per hour)

FD(j) Flowrate inlet (ton per hour)

FW(j) Freshwater flowrate (ton per hour)

WW(i) Waste of each source (ton per hour)

F(i,j) Splitting flowrate i to j (ton per hour)

DA(j) Sink stream concentration A (ppm)

DB(j) Sink stream concentration B (ppm)

DC(j) Sink stream concentration C_c (ppm)

DD(j) Sink stream concentration D (ppm)

OFW Overall freshwater (ton per hour)

OWW Overall waste (ton per hour)

FWCost Total cost of freshwater (\$ per y)

nXCost Total cost of water splitting units (\$)

nFCost Total cost of water feeding units (\$)

OCost Total operating cost (\$ per year)

;

Binary variable $y(i,j)$

$z(j)$

;

Scalar OMEGA /10000/

HY /8400/

CostFW /2.00/

CostnX /10000/

CostnF /10000/

;

Equation

***** Water Network

| | |
|------------|-------------------------------|
| MB1(j) | Mass balance (flowrate A) |
| MB2(j) | Mass balance (flowrate B) |
| MB3(j) | Mass balance (flowrate C) |
| MB4(j) | Mass balance (flowrate D) |
| MB5(j) | Mass balance (contaminant) |
| Cons1(i) | Constraint for x |
| Cons2(j) | Concentration constraint A |
| Cons3(j) | Concentration constraint B |
| Cons4(j) | Concentration constraint C |
| Cons5(j) | Concentration constraint D |
| Cons6(i,j) | Constraint for water flowrate |
| Flow(i,j) | Flowrate source i to sink j |
| Waste(i) | Waste of each source |
| OFresh | Overall freshwater |
| OWaste | Overall waste |

***** Number of units

| | |
|---------------|---------------------|
| Logical1(i,j) | Logical constraint1 |
| Logical2(j) | Logical constraint2 |

***** Cost

| | |
|----------|---------------------------|
| CostofFW | Total cost of Fresh water |
|----------|---------------------------|

CostofnX Total cost of water splitting units

CostofnF Total cost of water feeding units

CostofO Total cost of operation

***** Minimizing

Object Objective

;

***** Water Network

MB1(j)..sum(i,SA(i)*FS(i)*x(i,j))=e=DA(j)*FD(j);

MB2(j)..sum(i,SB(i)*FS(i)*x(i,j))=e=DB(j)*FD(j);

MB3(j)..sum(i,SC(i)*FS(i)*x(i,j))=e=DC(j)*FD(j);

MB4(j)..sum(i,SD(i)*FS(i)*x(i,j))=e=DD(j)*FD(j);

MB5(j)..sum(i,FS(i)*x(i,j))+FW(j)=e=FD(j);

Cons1(i)..sum(j,x(i,j))=l=1;

Cons2(j)..DA(j)=l=DMA(j);

Cons3(j)..DB(j)=l=DMB(j);

Cons4(j)..DC(j)=l=DMC(j);

Cons5(j)..DD(j)=l=DMD(j);

Cons6(i,j)\$\text{(ord(i) eq ord(j))}..FS(i)=e=FD(j);

Flow(i,j)..F(i,j)=e=FS(i)*x(i,j);

Waste(i)..WW(i)=e=(1-sum(j,x(i,j)))*FS(i);

OFresh..OFW=e=sum(j,FW(j));

OWaste..OWW=e=sum(i,WW(i));

***** Number of units

Logical1(i,j)..F(i,j)-y(i,j)*OMEGA=l=0;

Logical2(j)..FW(j)-z(j)*OMEGA=l=0;

***** Cost

CostofFW..FWCost=e=OFW*CostFW*HY;

CostofnX..nXCost=e=sum((i,j),y(i,j))*CostnX;

```

CostofnF..nFCost=e=sum(j,z(j))*CostnF;
CostofO..OCost=e=FWCost+nXCost+nFCost;
***** Minimizing
*****

Object..OBJ=e=OCost;
FS.lo('i1')=2.67;
FS.lo('i2')=25;
FS.lo('i3')=8.574;
FS.lo('i4')=10.3448;
FS.lo('i5')=28.125;
FS.lo('i6')=87.27;

Model CASE11/ALL/;
Solve CASE11 Using MINLP Minimizing OBJ;
Display OBJ.l, OCost.l, OFW.l, OWW.l, FW.l, WW.l, FS.l, x.l, F.l, DA.l,
DB.l, DC.l, DD.l, FWCost.l, nXCost.l, nFCost.l;

```

```

**** REPORT SUMMARY :    0  NONOPT
                        0  INFEASIBLE
                        0  UNBOUNDED
                        0  ERRORS

```

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows

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General Algebraic Modeling System

Execution

```

---- 180 VARIABLE OBJ.L          = 2141389.067 Objective function
      VARIABLE OCost.L          = 2141389.067 Total operating cost
                                   ($ per year)
      VARIABLE OFW.L            = 120.916 Overall freshwater (
                                   ton per hour)
      VARIABLE OWW.L            = 120.916 Overall waste

```

---- 180 VARIABLE FW.L Freshwater flowrate (ton per hour)

j1 2.670, j2 25.000, j3 8.574, j4 10.345, j5 25.415, j6 48.912

---- 180 VARIABLE WW.L Waste of each source (ton per hour)

i1 1.180, i2 22.121, i4 10.345, i6 87.270

---- 180 VARIABLE FS.L Flowrate outlet (ton per hour)

i1 2.670, i2 25.000, i3 8.574, i4 10.345, i5 28.125, i6 87.270

---- 180 VARIABLE x.L Source split fraction i to j

| | j5 | j6 |
|----|-------|-------|
| i1 | 0.558 | |
| i2 | 0.049 | 0.066 |
| i3 | | 1.000 |
| i5 | | 1.000 |

---- 180 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j5 | j6 |
|----|-------|--------|
| i1 | 1.490 | |
| i2 | 1.220 | 1.659 |
| i3 | | 8.574 |
| i5 | | 28.125 |

---- 180 VARIABLE DA.L Sink stream concentration A (ppm)

j5 26.164, j6 81.731

---- 180 VARIABLE DB.L Sink stream concentration B (ppm)

j5 200.000, j6 1000.000

---- 180 VARIABLE DC.L Sink stream concentration C (ppm)

j5 300.000, j6 126.957

---- 180 VARIABLE DD.L Sink stream concentration D (ppm)

j5 82.828, j6 99.470

---- 180 VARIABLE FWCost.L = 2031389.067 Total cost of freshwater (\$ per y)

VARIABLE nXCost.L = 50000.000 Total cost of water splitting units (\$)

VARIABLE nFCost.L = 60000.000 Total cost of water feeding units (\$)

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-WEI

USER: The Petroleum and Petrochemical College G131219:2228AS-WIN

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**** FILE SUMMARY

Input C:\Users\deepd_000\Documents\gamsdir\projdir\Data 2 Case 2 - Water Network with out treatment.gms

Output C:\Users\deepd_000\Documents\gamsdir\projdir\Data 2 Case 2 - Water Network with out treatment.lst

Appendix C-1 Case Study 4.3.1 GAMS Code**The second model: Mixed-integer non-linear programming (MINLP)**

Set

i Source stream /i1*i7/

j Sink stream /j1*j6/

;

Parameter

SA Source concentration A (ppm)

/i1 367.5

i2 154.4

i3 80

i4 293.34

i5 220.1111

i6 2375.043

i7 20/

SB Source concentration B (ppm)

/i1 500

i2 4000

i3 3500

i4 6000

i5 1800

i6 6500

i7 50/

SC Source concentration C (ppm)

/i1 5655.5

i2 10

i3 175

i4 127.5

i5 340

i6 167.2

i7 5/

SD Source concentration C (ppm)

/i1 1537.5

i2 32

i3 116.65

i4 1096.67

i5 271.2

i6 400

i7 30/

DMA Sink Maximum concentration A (ppm)

/j1 300

j2 10

j3 10

j4 100

j5 85

j6 1000/

DMB Sink Maximum concentration B (ppm)

/j1 50

j2 1

j3 1

j4 200

j5 200

j6 1000/

DMC Sink Maximum concentration C (ppm)

/j1 5000

j2 0

j3 0

j4 50

j5 300

j6 150/

DMD Sink Maximum concentration D (ppm)

/j1 1500

j2 0

j3 0

j4 1000

j5 200

j6 200/

Variable OBJ Objective function

Positive variable $x(i,j)$ Source split fraction i to j

FW(j) Freshwater flowrate (ton per hour)

WW(i) Waste of each source (ton per hour)

FS(i) Flowrate outlet (ton per hour)

FD(j) Flowrate inlet (ton per hour)

F(i,j) Splitting flowrate i to j (ton per hour)

DA(j) Sink stream concentration A (ppm)

DB(j) Sink stream concentration B (ppm)

DC(j) Sink stream concentration C (ppm)

DD(j) Sink stream concentration D (ppm)

OFW Overall freshwater (ton per hour)

OWW Overall waste (ton per hour)

OWD Overall waste water disposal (ton per hour)

CWA(i) waste concentration A (ppm)

CWB(i) waste concentration B (ppm)

CWC(i) waste concentration C (ppm)

CWD(i) waste concentration D (ppm)

OCWA Overall waste concentration A (ppm)

OCWB Overall waste concentration B (ppm)

OCWC Overall waste concentration C (ppm)

OCWD Overall waste concentration D (ppm)

WTA Concentration of waste treatment A (ppm)

WTB Concentration of waste treatment B (ppm)
 WTC Concentration of waste treatment C (ppm)
 WTD Concentration of waste treatment D (ppm)
 t treatment fraction
 FT Overall treatment flowrate
 FWCost Total cost of freshwater (\$ per y)
 TCost Total cost of Treatment (\$ per y)
 nXCost Total cost of water splitting units (\$)
 nFCost Total cost of water feeding units (\$)
 OCost Total operating cost (\$ per year)
 OCostPAPER Total operating cost PAPER (\$ per year)

;
 Binary variable y(i,j)
 z(j)

;
 Scalar OMEGA /10000/
 HY /8400/
 CostFW /2.00/
 CostT /1.68/
 CostnX /10000/
 CostnF /10000/
 ECostFW /0.32/

;
 Equation

***** Water Network

MB1(j) Mass balance (Contaminant A)
 MB2(j) Mass balance (Contaminant B)
 MB3(j) Mass balance (Contaminant C)
 MB4(j) Mass balance (Contaminant D)
 MB5(j) Mass balance (Flowrate)
 Cons1(i) Constraint for x

| | |
|------------|-----------------------------|
| Cons2(j) | Concentration constraint A |
| Cons3(j) | Concentration constraint B |
| Cons4(j) | Concentration constraint C |
| Cons5(j) | Concentration constraint D |
| Cons6(i,j) | Flowrate constraint |
| Flow(i,j) | Flowrate source i to sink j |
| OFresh | Overall freshwater |

***** Waste Water

| | |
|----------|--|
| Waste(i) | Waste of each source |
| MBW1(i) | Mass balance for waste concentration A |
| MBW2(i) | Mass balance for waste concentration B |
| MBW3(i) | Mass balance for waste concentration C |
| MBW4(i) | Mass balance for waste concentration D |
| MBW5 | Mass balance for overall waste concentration A |
| MBW6 | Mass balance for overall waste concentration B |
| MBW7 | Mass balance for overall waste concentration C |
| MBW8 | Mass balance for overall waste concentration D |
| OWaste | Overall waste |
| OWasteD | Overall waste disposal |

***** Treatment

| | |
|------|--------------------------------------|
| MBT1 | Mass balance for waste treatment A |
| MBT2 | Mass balance for waste treatment B |
| MBT3 | Mass balance for waste treatment C |
| MBT4 | Mass balance for waste treatment D |
| MBT5 | Constraint for waste treatment A |
| MBT6 | Constraint for waste treatment B |
| MBT7 | Constraint for waste treatment C |
| MBT8 | Constraint for waste treatment D |
| MBT9 | Mass balance for treatment treatment |

```

***** Number of units
*****

Logical1(i,j) Logical constraint1
Logical2(j) Logical constraint2

***** Cost
*****

CostofFW Total cost of Fresh water
CostofT Total cost of Treatment
CostofnX Total cost of water splitting units
CostofnF Total cost of water feeding units
CostofO Total cost of operation
CostofPAPER Total cost of operation with PAPER

***** Minimizing
*****

Object Objective function
;

***** Water Network
*****

MB1(j)..sum(i,SA(i)*FS(i)*x(i,j))=e=DA(j)*FD(j);
MB2(j)..sum(i,SB(i)*FS(i)*x(i,j))=e=DB(j)*FD(j);
MB3(j)..sum(i,SC(i)*FS(i)*x(i,j))=e=DC(j)*FD(j);
MB4(j)..sum(i,SD(i)*FS(i)*x(i,j))=e=DD(j)*FD(j);
MB5(j)..sum(i,FS(i)*x(i,j))+FW(j)=e=FD(j);
Cons1(i)..sum(j,x(i,j))=l=1;
Cons2(j)..DA(j)=l=DMA(j);
Cons3(j)..DB(j)=l=DMB(j);
Cons4(j)..DC(j)=l=DMC(j);
Cons5(j)..DD(j)=l=DMD(j);
Cons6(i,j)$ (ord(i) eq ord(j))..FS(i)=e=FD(j);
Flow(i,j)..F(i,j)=e=FS(i)*x(i,j);
OFresh..OFW=e=sum(j,FW(j));

```

***** Waste Water

Waste(i)..WW(i)=e=FS(i)-sum(j,F(i,j));

MBW1(i)..CWA(i)=e=WW(i)*SA(i);

MBW2(i)..CWB(i)=e=WW(i)*SB(i);

MBW3(i)..CWC(i)=e=WW(i)*SC(i);

MBW4(i)..CWD(i)=e=WW(i)*SD(i);

MBW5..OCWA*125.285=e=sum(i,CWA(i))-CWA('i7');

MBW6..OCWB*125.285=e=sum(i,CWB(i))-CWB('i7');

MBW7..OCWC*125.285=e=sum(i,CWC(i))-CWC('i7');

MBW8..OCWD*125.285=e=sum(i,CWD(i))-CWD('i7');

OWaste..OWW=e=sum(i,WW(i))-WW('i7');

OWasteD..OWD=e=OWW-(sum(j,x('i7',j))*FS('i7'));

***** Treatment

MBT1..WTA*33.574=e=(OCWA*(33.574-t))+(SA('i7')*t);

MBT2..WTB*33.574=e=(OCWB*(33.574-t))+(SB('i7')*t);

MBT3..WTC*33.574=e=(OCWC*(33.574-t))+(SC('i7')*t);

MBT4..WTD*33.574=e=(OCWD*(33.574-t))+(SD('i7')*t);

MBT5..WTA=l=100;

MBT6..WTB=l=100;

MBT7..WTC=l=100;

MBT8..WTD=l=100;

MBT9..FT=e=(sum(j,x('i7',j))*FS('i7'))+t;

***** Number of units

Logical1(i,j)..F(i,j)-y(i,j)*OMEGA=l=0;

Logical2(j)..FW(j)-z(j)*OMEGA=l=0;

***** Cost

CostofFW..FWCost=e=OFW*CostFW*HY;


```

CostofT..TCost=e=FT*HY*CostT;
CostofnX..nXCost=e=sum((i,j),y(i,j))*CostnX;
CostofnF..nFCost=e=sum(j,z(j))*CostnF;
CostofO..OCost=e=FWCost+TCost;
CostofPAPER..OCostPAPER=e=(OWW*CostT*HY)+(OFW*ECostFW*HY
);

```

```

***** Minimizing

```

```

*****

```

```

Object..OBJ=e=FWCost+TCost+nXCost+nFCost;

```

```

FS.lo('i1')=2.67;

```

```

FS.lo('i2')=25;

```

```

FS.lo('i3')=8.574;

```

```

FS.lo('i4')=10.3448;

```

```

FS.lo('i5')=28.125;

```

```

FS.lo('i6')=87.27;

```

```

FS.fx('i7')=1000;

```

```

Model CASE11/ALL/;

```

```

Solve CASE11 Using MINLP Minimizing OBJ;

```

```

Display OBJ.l, OCost.l, OCostPAPER.l, OFW.l, OWD.l, FT.l, OWW.l, FW.l,
WW.l, FS.l, FD.l, x.l, F.l, y.l, DA.l, DB.l, DC.l, DD.l,
CWA.l, CWB.l, CWC.l, CWD.l, OCWA.l, OCWB.l, OCWC.l, OCWD.l,
WTA.l, WTB.l, WTC.l, WTD.l, t.l, FWCost.l, TCost.l, nXCost.l, nFCost.l;

```

**** REPORT SUMMARY : 0 NONOPT

0 INFEASIBLE

0 UNBOUNDED

0 ERRORS

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows

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General Algebraic Modeling System

Execution

---- 252 VARIABLE OBJ.L = 2407965.113 Objective function

VARIABLE OCost.L = 2327965.113 Total operating cost
(\$ per year)

VARIABLE OCostPAPER.L = 1858266.010 Total operating cost
PAPER (\$ per year)

VARIABLE OFW.L = 33.574 Overall freashwater (
ton per hour)

VARIABLE OWD.L = 33.574 Overall waste water d
isposal (ton per hour
)

VARIABLE FT.L = 124.994 Overall treatment flo
wrate

VARIABLE OWW.L = 125.285 Overall waste (ton pe
r hour)

---- 252 VARIABLE FW.L Freshwater flowrate (ton per hour)

j2 25.000, j3 8.574

---- 252 VARIABLE WW.L Waste of each source (ton per hour)

i1 2.670, i2 25.000, i4 10.345, i6 87.270, i7 908.289

---- 252 VARIABLE FS.L Flowrate outlet (ton per hour)

i1 2.670, i2 25.000, i3 8.574, i4 10.345, i5 28.125

i6 87.270, i7 1000.000

---- 252 VARIABLE FD.L Flowrate inlet (ton per hour)

j1 2.670, j2 25.000, j3 8.574, j4 10.345, j5 28.125, j6 87.270

---- 252 VARIABLE x.L Source split fraction i to j

| | j1 | j4 | j5 | j6 |
|----|-------|-------|-------|-------|
| i3 | | | | 1.000 |
| i5 | | | | 1.000 |
| i7 | 0.003 | 0.010 | 0.028 | 0.051 |

---- 252 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j1 | j4 | j5 | j6 |
|----|-------|--------|--------|--------|
| i3 | | | | 8.574 |
| i5 | | | | 28.125 |
| i7 | 2.670 | 10.345 | 28.125 | 50.571 |

---- 252 VARIABLE y.L

| | j1 | j4 | j5 | j6 |
|----|-------|-------|-------|-------|
| i3 | | | | 1.000 |
| i5 | | | | 1.000 |
| i7 | 1.000 | 1.000 | 1.000 | 1.000 |

---- 252 VARIABLE DA.L Sink stream concentration A (ppm)

j1 20.000, j4 20.000, j5 20.000, j6 90.386

---- 252 VARIABLE DB.L Sink stream concentration B (ppm)

j1 50.000, j4 50.000, j5 50.000, j6 952.934

---- 252 VARIABLE DC.L Sink stream concentration C (ppm)

j1 5.000, j4 5.000, j5 5.000, j6 129.664

---- 252 VARIABLE DD.L Sink stream concentration D (ppm)

j1 30.000, j4 30.000, j5 30.000, j6 116.246

---- 252 VARIABLE CWA.L waste concentration A (ppm)

i1 981.225, i2 3860.000, i4 3034.544, i6 207270.003

i7 18165.784

---- 252 VARIABLE CWB.L waste concentration B (ppm)

i1 1335.000, i2 100000.000, i4 62068.800, i6 567255.000

i7 45414.460

---- 252 VARIABLE CWC.L waste concentration C (ppm)

i1 15100.185, i2 250.000, i4 1318.962, i6 14591.544, i7 4541.446

---- 252 VARIABLE CWD.L waste concentration D (ppm)

i1 4105.125, i2 800.000, i4 11344.832, i6 34908.000, i7 27248.676

---- 252 VARIABLE OCWA.L = 1717.251 Overall waste concentration A (ppm)

VARIABLE OCWB.L = 5831.974 Overall waste concentration B (ppm)

VARIABLE OCWC.L = 249.517 Overall waste concentration C (ppm)

VARIABLE OCWD.L = 408.333 Overall waste concentration D (ppm)

VARIABLE WTA.L = 34.677 Concentration of waste treatment A (ppm)

VARIABLE WTB.L = 100.000 Concentration of waste treatment B (ppm)

VARIABLE WTC.L = 7.114 Concentration of waste treatment C (ppm)

VARIABLE WTD.L = 33.272 Concentration of waste treatment D (ppm)

VARIABLE t.L = 33.284 treatment fraction

VARIABLE FWCost.L = 564043.200 Total cost of freshwater (\$ per y)

VARIABLE TCost.L = 1763921.913 Total cost of Treatment (\$ per y)
VARIABLE nXCost.L = 60000.000 Total cost of water splitting units (\$)
VARIABLE nFCost.L = 20000.000 Total cost of water feeding units (\$)

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-WEI

USER: The Petroleum and Petrochemical College G131219:2228AS-WIN
Chulalongkorn University DC4365

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**** FILE SUMMARY

Input C:\Users\deepd_000\Documents\gamssdir\projdir\Data 2 Case 3 - Water Network with end of pipe.gms

Output C:\Users\deepd_000\Documents\gamssdir\projdir\Data 2 Case 3 - Water Network with end of pipe.lst

Appendix D-1 Case Study 4.4.1 GAMS Code**The model: Liner programming (LP)**

Set

i Source stream /i1*i4/

u Sink stream /u1*u1/

;

Parameter

CSA Source concentration A (ppm)

/i1 15

i2 120

i3 220

i4 50/

CSB Source concentration B (ppm)

/i1 400

i2 12500

i3 45

i4 5/

CSC Source concentration C (ppm)

/i1 35

i2 180

i3 9500

i4 20/

FS Source flowrate (ton per hour)

/i1 16.832

i2 34

i3 54.831

i4 200/

CKLA Sink concentration A (ppm)

/u1 100/

CKLB Sink concentration B (ppm)

/u1 100/

CKLC Sink concentration C (ppm)

/u1 100/

FK Sink flowrate (ton per hour)

/u1 105.662/

;

Variable OBJ Objective function

;

Positive variable $x(i,u)$ Source split fraction i to j
 $F(i,u)$ Splitting flowrate i to j (ton per hour)
 $CKA(u)$ Sink stream concentration A (ppm)
 $CKB(u)$ Sink stream concentration B (ppm)
 $CKC(u)$ Sink stream concentration C (ppm)

;

Equation

MB1(u) Mass balance (flowrate A)
 MB2(u) Mass balance (flowrate B)
 MB3(u) Mass balance (flowrate C)
 MB4(u) Mass balance (contaminant)
 Cons1(i) Constraint for x
 Cons2(u) Concentration constraint A
 Cons3(u) Concentration constraint B
 Cons4(u) Concentration constraint C

Flow(i,u) Flowrate source i to sink j
 Object Objective

```

MB1(u)..sum(i,CSA(i)*FS(i)*x(i,u))=e=CKA(u)*FK(u);
MB2(u)..sum(i,CSB(i)*FS(i)*x(i,u))=e=CKB(u)*FK(u);
MB3(u)..sum(i,CSC(i)*FS(i)*x(i,u))=e=CKC(u)*FK(u);
MB4(u)..sum(i,FS(i)*x(i,u))=e=FK(u);
Cons1(i)..sum(u,x(i,u))=l=1;
Cons2(u)..CKA(u)=l=CKLA(u);
Cons3(u)..CKB(u)=l=CKLB(u);
Cons4(u)..CKC(u)=l=CKLC(u);
Flow(i,u)..F(i,u)=e=FS(i)*x(i,u);
Object..OBJ =e= F('i4','u1');

```

```
x.fx('i2','u1')=0;
```

```
x.fx('i3','u1')=0;
```

```
Model CASE11/ALL/;
```

```
Solve CASE11 Using LP Minimizing OBJ;
```

```
Display OBJ.l, x.l, F.l, CKA.l, CKB.l, CKC.l;
```

```
**** REPORT SUMMARY :    0    NOOPT
```

```
                  0 INFEASIBLE
```

```
                  0 UNBOUNDED
```

```
GAMS 24.2.1 r43572 Released Dec 9, 2013 WIN-VS8 x86/MS Windows
```

```
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```

```
General Algebraic Modeling System
```

```
Execution
```

```
---- 85 VARIABLE OBJ.L            =    88.830 Objective function
```


---- 85 VARIABLE x.L Source split fraction i to j

u1

i1 1.000

i4 0.444

---- 85 VARIABLE F.L Splitting flowrate i to j (ton per hour)

u1

i1 16.832

i4 88.830

---- 85 VARIABLE CK.A.L Sink stream concentration A (ppm)

u1 44.424

---- 85 VARIABLE CK.B.L Sink stream concentration B (ppm)

u1 67.924

---- 85 VARIABLE CK.C.L Sink stream concentration C (ppm)

u1 22.390

EXECUTION TIME = 0.015 SECONDS 3 MB 24.2.1 r43572
WIN-VS8

USER: The Petroleum and Petrochemical College G131219:2228AS-
WIN

Chulalongkorn University

DC4365

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**** FILE SUMMARY

Input C:\Users\DoNuT\Documents\gamsdir\projdir\Data 1 Case 5 -
Treatment part of case 2.gms

Output C:\Users\DoNuT\Documents\gamsdir\projdir\Data 1 Case 5 -
Treatment part of case 2.lst

Appendix E-1 Case Study 4.5.1 GAMS Code

The first model: Non-linear programming (NLP)

Set

i Source stream /i1*i3/

j Sink stream /j1*j3/

;

Parameter

SMA Source concentration of Salts (ppm)

/i1 15

i2 120

i3 220/

SMB Source concentration of Organics (ppm)

/i1 400

i2 12500

i3 45/

SMC Source concentration of H₂S (ppm)

/i1 35

i2 180

i3 9500/

FS Maximun flowrate of fresh water

/i1 45

i2 33.184

i3 54.821/

LA Load of Salts contaminant (kg per hour)

/j1 0.675

j2 3.40

j3 5.60/

LB Load of Organics contaminant (kg per hour)

/j1 18.0

j2 414.80

j3 1.4/

LC Load of H₂S contaminant (kg per hour)

/j1 1.575

j2 4.590

j3 520.8/

DMA Sink Maximum concentration of Salts (ppm)

/j1 0

j2 20

j3 120/

DMB Sink Maximum concentration of Organics (ppm)

/j1 0

j2 300

j3 20/

DMC Sink Maximum concentration of H₂S (ppm)

/j1 0

j2 45

j3 200/

Variable OBJ Objective function

Positive variable

| | |
|--------|---|
| x(i,j) | Source split fraction i to j |
| FW(j) | Freshwater flowrate (ton per hour) |
| WW(i) | Waste of each source (ton per hour) |
| F(i,j) | Splitting flowrate i to j (ton per hour) |
| DA(j) | Sink stream concentration of Salts (ppm) |
| DB(j) | Sink stream concentration of Organics (ppm) |
| DC(j) | Sink stream concentration of H ₂ S (ppm) |
| SA(i) | Source stream concentration of Salts (ppm) |
| SB(i) | Source stream concentration of Organics (ppm) |
| SC(i) | Source stream concentration of H ₂ S (ppm) |
| OFW | Overall freshwater (ton per hour) |
| OWW | Overall waste (ton per hour) |

- $LoadA(i,j)$ Contaminant load of Salts of Process i to j (gram per hour)
 $LoadB(i,j)$ Contaminant load of Organics of Process i to j (gram per hour)
 $LoadC(i,j)$ Contaminantload of H₂S of Process i to j (gram per hour)
 $Flowin(j)$ Total flowrate inlet of Salts contaminant of each process (ton per hour)
 $DeltaCA(i,j)$ Outlet concentration - Inlet concentration of Salts contaminant (ppm)
 $DeltaCB(i,j)$ Outlet concentration - Inlet concentration of Organics contaminant (ppm)
 $DeltaCC(i,j)$ Outlet concentration - Inlet concentration of H₂S contaminant (ppm)

;

Equation

$ConloadA1(i,j)$ Contaminantload of Salts of Process 1

$ConloadA2(i,j)$ Contaminantload of Salts of Process 2

$ConloadA3(i,j)$ Contaminantload of Salts of Process 3

$ConloadB1(i,j)$ Contaminantload of Organics of Process 1

$ConloadB2(i,j)$ Contaminantload of Organics of Process 2

$ConloadB3(i,j)$ Contaminantload of Organics of Process 3

$ConloadC1(i,j)$ Contaminantload of H₂S of Process 1

$ConloadC2(i,j)$ Contaminantload of H₂S of Process 2

$ConloadC3(i,j)$ Contaminantload of H₂S of Process 3

$MLoadA1(i,j)$ Contaminantload balance of Salts of Process 1

$MLoadA2(i,j)$ Contaminantload balance of Salts of Process 2

$MLoadA3(i,j)$ Contaminantload balance of Salts of Process 3

$MLoadB1(i,j)$ Contaminantload balance of Organics of Process 1

$MLoadB2(i,j)$ Contaminantload balance of Organics of Process 2

$MLoadB3(i,j)$ Contaminantload balance of Organics of Process 3

MLoadC1(i,j) Contaminantload balance of H2S of Process 1
 MLoadC2(i,j) Contaminantload balance of H2S of Process 2
 MLoadC3(i,j) Contaminantload balance of H2S of Process 3

TFlowin1(j) Total flowrate inlet of process 1
 TFlowin2(j) Total flowrate inlet of process 2
 TFlowin3(j) Total flowrate inlet of process 3

FF1 Constraint for flowrate inlet of process 1
 FF2 Constraint for flowrate inlet of process 2
 FF3 Constraint for flowrate inlet of process 3

MconSA1(i) Outlet concentration balance of Salts of process 1
 MconSA2(i) Outlet concentration balance of Salts of process 2
 MconSA3(i) Outlet concentration balance of Salts of process 3

MconSB1(i) Outlet concentration balance of Organics of process1
 MconSB2(i) Outlet concentration balance of Organics of process2
 MconSB3(i) Outlet concentration balance of Organics of process3

MconSC1(i) Outlet concentration balance of H2S of process 1
 MconSC2(i) Outlet concentration balance of H2S of process 2
 MconSC3(i) Outlet concentration balance of H2S of process 3

DCA1(i,j) Delta concentration of Salts of process 1
 DCA2(i,j) Delta concentration of Salts of process 2
 DCA3(i,j) Delta concentration of Salts of process 3

DCB1(i,j) Delta concentration of Organics of process 1
 DCB2(i,j) Delta concentration of Organics of process 2
 DCB3(i,j) Delta concentration of Organics of process 3

| | | |
|-----------|------------|--|
| | DCC1(i,j) | Delta concentration of H2S of process 1 |
| | DCC2(i,j) | Delta concentration of H2S of process 2 |
| | DCC3(i,j) | Delta concentration of H2S of process 3 |
| | InconA1(j) | New concentration of water inlet of Salts of process 1 |
| | InconA2(j) | New concentration of water inlet of Salts of process 2 |
| | InconA3(j) | New concentration of water inlet of Salts of process 3 |
| process 1 | InconB1(j) | New concentration of water inlet of Organics of |
| process 2 | InconB2(j) | New concentration of water inlet of Organics of |
| process 3 | InconB3(j) | New concentration of water inlet of Organics of |
| | InconC1(j) | New concentration of water inlet of H2S of process 1 |
| | InconC2(j) | New concentration of water inlet of H2S of process 2 |
| | InconC3(j) | New concentration of water inlet of H2S of process 3 |
| | CBA1(j) | Concentration balance of Salts of process 1 |
| | CBA2(j) | Concentration balance of Salts of process 2 |
| | CBA3(j) | Concentration balance of Salts of process 3 |
| | CBB1(j) | Concentration balance of Organics of process 1 |
| | CBB2(j) | Concentration balance of Organics of process 2 |
| | CBB3(j) | Concentration balance of Organics of process 3 |
| | CBC1(j) | Concentration balance of H2S of process 1 |
| | CBC2(j) | Concentration balance of H2S of process 2 |
| | CBC3(j) | Concentration balance of H2S of process 3 |

Cons1(i) Constraint for x
 Flowsplit(i,j) Splited flowrate source i to sink j
 OFresh Overall freshwater
 Object Objective

;

*Contaminantload of each process

ConloadA1('i1','j1') .. LoadA('i1','j1') =e= 1000*LA('j1');

ConloadA2('i2','j2') .. LoadA('i2','j2') =e= 1000*LA('j2');

ConloadA3('i3','j3') .. LoadA('i3','j3') =e= 1000*LA('j3');

ConloadB1('i1','j1') .. LoadB('i1','j1') =e= 1000*LB('j1');

ConloadB2('i2','j2') .. LoadB('i2','j2') =e= 1000*LB('j2');

ConloadB3('i3','j3') .. LoadB('i3','j3') =e= 1000*LB('j3');

ConloadC1('i1','j1') .. LoadC('i1','j1') =e= 1000*LC('j1');

ConloadC2('i2','j2') .. LoadC('i2','j2') =e= 1000*LC('j2');

ConloadC3('i3','j3') .. LoadC('i3','j3') =e= 1000*LC('j3');

*Contaminantload balance of each process

MLoadA1('i1','j1')..LoadA('i1','j1')=e=Flowin('j1')*DeltaCA('i1','j1');

MLoadA2('i2','j2')..LoadA('i2','j2')=e=Flowin('j2')*DeltaCA('i2','j2');

MLoadA3('i2','j3')..LoadA('i3','j3')=e=Flowin('j3')*DeltaCA('i3','j3');

MLoadB1('i1','j1')..LoadB('i1','j1')=e=Flowin('j1')*DeltaCB('i1','j1');

MLoadB2('i2','j2')..LoadB('i2','j2')=e=Flowin('j2')*DeltaCB('i2','j2');

MLoadB3('i2','j3')..LoadB('i3','j3')=e=Flowin('j3')*DeltaCB('i3','j3');

MLoadC1('i1','j1')..LoadC('i1','j1')=e=Flowin('j1')*DeltaCC('i1','j1');

MLoadC2('i2','j2')..LoadC('i2','j2')=e=Flowin('j2')*DeltaCC('i2','j2');

MLoadC3('i2','j3')..LoadC('i3','j3')=e=Flowin('j3')*DeltaCC('i3','j3');

*Total inlet flowrate of each process

$$TFlowin1('j1')..Flowin('j1')=e=sum(i,FS(i)*x(i,'j1'))+FW('j1');$$

$$TFlowin2('j2')..Flowin('j2')=e=sum(i,FS(i)*x(i,'j2'))+FW('j2');$$

$$TFlowin3('j3')..Flowin('j3')=e=sum(i,FS(i)*x(i,'j3'))+FW('j3');$$

*Constraint for flowrate inlet of each process

$$FF1..Flowin('j1')=g=FS('i1');$$

$$FF2..Flowin('j2')=g=FS('i2');$$

$$FF3..Flowin('j3')=g=FS('i3');$$

*Outlet concentration of each process

$$MconSA1('i1')..LA('j1')*1000=e=FS('i1')*SA('i1');$$

$$MconSA2('i2')..LA('j2')*1000=e=FS('i2')*SA('i2');$$

$$MconSA3('i3')..LA('j3')*1000=e=FS('i3')*SA('i3');$$

$$MconSB1('i1')..LB('j1')*1000=e=FS('i1')*SB('i1');$$

$$MconSB2('i2')..LB('j2')*1000=e=FS('i2')*SB('i2');$$

$$MconSB3('i3')..LB('j3')*1000=e=FS('i3')*SB('i3');$$

$$MconSC1('i1')..LC('j1')*1000=e=FS('i1')*SC('i1');$$

$$MconSC2('i2')..LC('j2')*1000=e=FS('i2')*SC('i2');$$

$$MconSC3('i3')..LC('j3')*1000=e=FS('i3')*SC('i3');$$

*Delta concentration of each process

$$DCA1('i1','j1') .. DeltaCA('i1','j1') =e= (SA('i1')-DA('j1'));$$

$$DCA2('i2','j2') .. DeltaCA('i2','j2') =e= (SA('i2')-DA('j2'));$$

$$DCA3('i3','j3') .. DeltaCA('i3','j3') =e= (SA('i3')-DA('j3'));$$

$$DCB1('i1','j1') .. DeltaCB('i1','j1') =e= (SB('i1')-DB('j1'));$$

$$DCB2('i2','j2') .. DeltaCB('i2','j2') =e= (SB('i2')-DB('j2'));$$

$$DCB3('i3','j3') .. DeltaCB('i3','j3') =e= (SB('i3')-DB('j3'));$$

$DCC1('i1','j1') .. \Delta CC('i1','j1') = e = (SC('i1') - DC('j1'));$
 $DCC2('i2','j2') .. \Delta CC('i2','j2') = e = (SC('i2') - DC('j2'));$
 $DCC3('i3','j3') .. \Delta CC('i3','j3') = e = (SC('i3') - DC('j3'));$

*New concentration of water inlet

$InconA1('j1') .. DA('j1') * Flowin('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SA(i));$
 $CBA1('j1') .. DA('j1') = l = DMA('j1');$
 $InconA2('j2') .. DA('j2') * Flowin('j2') = e = \sum(i, FS(i) * x(i, 'j2') * SA(i));$
 $CBA2('j2') .. DA('j2') = l = DMA('j2');$
 $InconA3('j3') .. DA('j3') * Flowin('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SA(i));$
 $CBA3('j3') .. DA('j3') = l = DMA('j3');$

$InconB1('j1') .. DB('j1') * Flowin('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SB(i));$
 $CBB1('j1') .. DB('j1') = l = DMB('j1');$
 $InconB2('j2') .. DB('j2') * Flowin('j2') = e = \sum(i, FS(i) * x(i, 'j1') * SB(i));$
 $CBB2('j2') .. DB('j2') = l = DMB('j2');$
 $InconB3('j3') .. DB('j3') * Flowin('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SB(i));$
 $CBB3('j3') .. DB('j3') = l = DMB('j3');$

$InconC1('j1') .. DC('j1') * Flowin('j1') = e = \sum(i, FS(i) * x(i, 'j1') * SC(i));$
 $CBC1('j1') .. DC('j1') = l = DMC('j1');$
 $InconC2('j2') .. DC('j2') * Flowin('j2') = e = \sum(i, FS(i) * x(i, 'j2') * SC(i));$
 $CBC2('j2') .. DC('j2') = l = DMC('j2');$
 $InconC3('j3') .. DC('j3') * Flowin('j3') = e = \sum(i, FS(i) * x(i, 'j3') * SC(i));$
 $CBC3('j3') .. DC('j3') = l = DMC('j3');$

$Cons1(i) .. \sum(j, x(i, j)) = l = 1;$

$Flowsplit(i, j) .. F(i, j) = e = FS(i) * x(i, j);$

$OFresh .. OFW = e = \sum(j, FW(j));$

$Object .. OBJ = e = OFW;$

$DB.lo('j2') = 300;$

$DC.lo('j3') = 200;$

Model CASE11/ALL/;

Solve CASE11 Using NLP Minimizing OBJ;

Display LoadA.l, LoadB.l, LoadC.l, Flowin.l, SA.l, SB.l, SC.l, DeltaCA.l,

DeltaCB.l, DeltaCC.l, DA.l, DB.l, DC.l, FW.l, OBJ.l, OFW.l, x.l, F.l;

**** REPORT SUMMARY : 0 NONOPT

1 INFEASIBLE (INFES)

SUM 10200.000

MAX 10200.000

MEAN 10200.000

0 UNBOUNDED

0 ERRORS

GAMS 24.2.1 r43572 Released Dec 9, 2013 WEX-WEI x86_64/MS Windows

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General Algebraic Modeling System

Execution

---- 275 VARIABLE LoadA.L Contaminantload of Salts of Process i to j (gram per hour)

| | j1 | j2 | j3 |
|----|---------|----------|----------|
| i1 | 675.000 | | |
| i2 | | 3400.000 | |
| i3 | | | 5600.000 |

---- 275 VARIABLE LoadB.L Contaminantload of Organics of Process i to j (gram per hour)

| | j1 | j2 | j3 |
|----|-----------|------------|----------|
| i1 | 18000.000 | | |
| i2 | | 414800.000 | |
| i3 | | | 1400.000 |

---- 275 VARIABLE LoadC.L Contaminantload of H2S of Process i to j (gram per hour)

| | j1 | j2 | j3 |
|----|----------|----------|------------|
| i1 | 1575.000 | | |
| i2 | | 4590.000 | |
| i3 | | | 520800.000 |

---- 275 VARIABLE Flowin.L Total flowrate inlet of Salts contaminant of each process (ton per hour)

j1 45.000, j2 34.000, j3 56.000

---- 275 VARIABLE SA.L Source stream concentration of Salts (ppm)

i1 15.000, i2 102.459, i3 102.151

---- 275 VARIABLE SB.L Source stream concentration of Organics (ppm)

i1 400.000, i2 12500.000, i3 25.538

---- 275 VARIABLE SC.L Source stream concentration of H2S (ppm)

i1 35.000, i2 138.320, i3 9500.009

---- 275 VARIABLE DeltaCA.L Outlet concentration - Inlet concentration of Salts contaminant (ppm)

| | j1 | j2 | j3 |
|----|--------|---------|---------|
| i1 | 15.000 | | |
| i2 | | 100.000 | |
| i3 | | | 100.000 |

---- 275 VARIABLE DeltaCB.L Outlet concentration - Inlet concentration of Organics contaminant (ppm)

| | j1 | j2 | j3 |
|----|---------|-----------|--------|
| i1 | 400.000 | | |
| i2 | | 12200.000 | |
| i3 | | | 25.000 |

---- 275 VARIABLE DeltaCC.L Outlet concentration - Inlet concentration of H2S contaminant (ppm)

| | j1 | j2 | j3 |
|----|--------|---------|----------|
| i1 | 35.000 | | |
| i2 | | 135.000 | |
| i3 | | | 9300.009 |

---- 275 VARIABLE DA.L Sink stream concentration of Salts (ppm)
j2 2.459, j3 2.151

---- 275 VARIABLE DB.L Sink stream concentration of Organics (ppm)
j2 300.000, j3 0.538

---- 275 VARIABLE DC.L Sink stream concentration of H2S (ppm)
j2 3.320, j3 200.000

---- 275 VARIABLE FW.L Freshwater flowrate (ton per hour)
j1 45.000, j2 33.184, j3 54.821

---- 275 VARIABLE OBJ.L = 133.005 Objective function
VARIABLE OFW.L = 133.005 Overall freshwater (ton per hour)

---- 275 VARIABLE x.L Source split fraction i to j

| | j2 | j3 |
|----|-------|-------|
| i2 | 0.025 | |
| i3 | | 0.022 |

---- 275 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j2 | j3 |
|----|-------|-------|
| i2 | 0.816 | |
| i3 | | 1.179 |

EXECUTION TIME = 0.000 SECONDS 3 MB 24.2.1 r43572 WEX-WEI

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**** FILE SUMMARY

Input C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 1 - Initialization step for Water Network.gms

Output C:\Users\deepd_000\Documents\gamsdir\projdir\Data 1 Case 1 - Initialization step for Water Network.lst

The second model: Mixed-integer non-linear programming (MINLP)

Set

i Source stream /i1*i4/

j Sink stream /j1*j3/

Parameter

SA Source concentration A (ppm)

/i1 15

i2 120

i3 220

i4 50/

SB Source concentration B (ppm)

/i1 400

i2 12500

i3 45

i4 5/

SC Source concentration C (ppm)

/i1 35

i2 180

i3 9500

i4 20/

DMA Sink Maximum concentration A (ppm)

/j1 0

j2 20

j3 120/

DMB Sink Maximum concentration B (ppm)

/j1 0
 j2 300
 j3 20/

DMC Sink Maximum concentration C (ppm)

/j1 0
 j2 45
 j3 200/

;

Variable OBJ Objective function

;

Positive variable $x(i,j)$ Source split fraction i to j
 FW(j) Freshwater flowrate (ton per hour)
 WW(i) Waste of each source (ton per hour)
 FS(i) Flowrate outlet (ton per hour)
 FD(j) Flowrate inlet (ton per hour)
 F(i,j) Splitting flowrate i to j (ton per hour)
 DA(j) Sink stream concentration A (ppm)
 DB(j) Sink stream concentration B (ppm)
 DC(j) Sink stream concentration C (ppm)
 OFW Overall freshwater (ton per hour)
 OWW Overall waste (ton per hour)
 OWD Overall waste water disposal (ton per hour)
 CWA(i) waste concentration A (ppm)
 CWB(i) waste concentration B (ppm)
 CWC(i) waste concentration C (ppm)
 OCWA Overall waste concentration A (ppm)
 OCWB Overall waste concentration B (ppm)
 OCWC Overall waste concentration C (ppm)

WTA Concentration of waste treatment A (ppm)
 WTB Concentration of waste treatment B (ppm)
 WTC Concentration of waste treatment C (ppm)
 t treatment fraction
 FT Overall treatment flowrate
 FWCost Total cost of freshwater (\$ per y)
 TCost Total cost of Treatment (\$ per y)
 nXCost Total cost of water splitting units (\$)
 nFCost Total cost of water feeding units (\$)
 OCost Total operating cost (\$ per year)
 SCost Saving Cost (\$ per y)

Binary variable $y(i,j)$
 $z(j)$

Scalar OMEGA /10000/
 HY /8400/
 CostFW /2.00/
 CostnX /10000/
 CostnF /10000/
 CostT /1.68/

Equation

***** Water Network

MB1(j) Mass balance (flowrate A)
 MB2(j) Mass balance (flowrate B)
 MB3(j) Mass balance (flowrate C)

| | |
|------------|-----------------------------|
| MB4(j) | Mass balance (contaminant) |
| Cons1(i) | Constraint for x |
| Cons2(j) | Concentration constraint A |
| Cons3(j) | Concentration constraint B |
| Cons4(j) | Concentration constraint C |
| Cons5(i,j) | Flowrate constraint |
| Flow(i,j) | Flowrate source i to sink j |
| OFresh | Overall freshwater |

***** Waste Water

| | |
|----------|--|
| Waste(i) | Waste of each source |
| MBW1(i) | Mass balance for waste concentration A |
| MBW2(i) | Mass balance for waste concentration B |
| MBW3(i) | Mass balance for waste concentration C |
| MBW4 | Mass balance for overall waste concentration A |
| MBW5 | Mass balance for overall waste concentration B |
| MBW6 | Mass balance for overall waste concentration C |
| OWaste | Overall waste |
| OWasted | Overall waste disposal |

***** Treatment

| | |
|------|--------------------------------------|
| MBT1 | Mass balance for waste treatment A |
| MBT2 | Mass balance for waste treatment B |
| MBT3 | Mass balance for waste treatment C |
| MBT4 | Constraint for waste treatment A |
| MBT5 | Constraint for waste treatment B |
| MBT6 | Constraint for waste treatment C |
| MBT7 | Mass balance for treatment treatment |

***** Number of units

Logical1(i,j) Logical constraint1

Logical2(j) Logical constraint2

***** Cost

CostofFW Total cost of Fresh water

CostofT Total cost of Treatment

CostofnX Total cost of water splitting units

CostofnF Total cost of water feeding units

CostofO Total cost of operation

CostofS Total saving cost

***** Minimizing

Object Objective function

;

***** Water Network

MB1(j)..sum(i,SA(i)*FS(i)*x(i,j))=e=DA(j)*FD(j);

MB2(j)..sum(i,SB(i)*FS(i)*x(i,j))=e=DB(j)*FD(j);

MB3(j)..sum(i,SC(i)*FS(i)*x(i,j))=e=DC(j)*FD(j);

MB4(j)..sum(i,FS(i)*x(i,j))+FW(j)=e=FD(j);

Cons1(i)..sum(j,x(i,j))=l=1;

Cons2(j)..DA(j)=l=DMA(j);

Cons3(j)..DB(j)=l=DMB(j);

Cons4(j)..DC(j)=l=DMC(j);

Cons5(i,j)\$\text{(ord(i) eq ord(j))}..FS(i)=e=FD(j);

Flow(i,j)..F(i,j)=e=FS(i)*x(i,j);

OFresh..OFW=e=sum(j,FW(j));

***** Waste Water

Waste(i)..WW(i)=e=FS(i)-sum(j,F(i,j));

MBW1(i)..CWA(i)=e=WW(i)*SA(i);

MBW2(i)..CWB(i)=e=WW(i)*SB(i);

MBW3(i)..CWC(i)=e=WW(i)*SC(i);

MBW4..OCWA*106.495=e=sum(i,CWA(i))-CWA('i4');

MBW5..OCWB*106.495=e=sum(i,CWB(i))-CWB('i4');

MBW6..OCWC*106.495=e=sum(i,CWC(i))-CWC('i4');

OWaste..OWW=e=sum(i,WW(i))-WW('i4');

OWasteD..OWD=e=OWW-(sum(j,x('i4',j))*FS('i4'));

***** Treatment

MBT1..WTA*47.602=e=(OCWA*(47.602-t))+(SA('i4')*t);

MBT2..WTB*47.602=e=(OCWB*(47.602-t))+(SB('i4')*t);

MBT3..WTC*47.602=e=(OCWC*(47.602-t))+(SC('i4')*t);

MBT4..WTA=l=100;

MBT5..WTB=l=100;

MBT6..WTC=l=100;

MBT7..FT=e=(sum(j,x('i4',j))*FS('i4'))+36.153;

***** Number of units

Logical1(i,j)..F(i,j)-y(i,j)*OMEGA=l=0;

Logical2(j)..FW(j)-z(j)*OMEGA=l=0;

***** Cost

CostofFW..FWCost=e=OFW*CostFW*HY;

CostofT..TCost=e=CostT*FT*HY;

CostofnX..nXCost=e=sum((i,j),y(i,j))*CostnX;

CostofnF..nFCost=e=sum(j,z(j))*CostnF;

CostofO..OCost=e=FWCost+TCost;

CostofS..SCost=e=(133*3.68*HY)-OCost;

***** Minimizing

Object..OBJ=e=FWCost+TCost+nXCost+nFCost;

FS.lo('i1')=45;

FS.lo('i2')=34;

FS.lo('i3')=56;

FS.fx('i4')=200;

Model CASE11/ALL/;

Solve CASE11 Using MINLP Minimizing OBJ;

Display OBJ.l, OCost.l, SCost.l, OFW.l, OWD.l, FT.l, OWW.l, FW.l, WW.l,

FS.l, FD.l, x.l, F.l, y.l, DA.l, DB.l, DC.l,

CWA.l, CWB.l, CWC.l, OCWA.l, OCWB.l, OCWC.l, WTA.l, WTB.l,

WTC.l, t.l, FWCost.l, TCost.l, nXCost.l, nFCost.l;

**** REPORT SUMMARY : 0 NONOPT

0 INFEASIBLE

0 UNBOUNDED

0 ERRORS

GAMS 24.2.1 r43572 Released Dec 9, 2013 WIN-VS8 x86/MS Windows 03/15/15

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General Algebraic Modeling System

Execution

---- 197 VARIABLE OBJ.L = 2211008.076 Objective function
 VARIABLE OCost.L = 2141008.076 Total operating cost
 (\$ per year)
 VARIABLE SCost.L = 1970287.924 Saving Cost (\$ per y)
 VARIABLE OFW.L = 47.602 Overall freashwater (
 ton per hour)
 VARIABLE OWD.L = 47.602 Overall waste water d
 isposal (ton per hour)
 VARIABLE FT.L = 95.046 Overall treatment flowrate
 VARIABLE OWW.L = 106.495 Overall waste (ton per hour)

---- 197 VARIABLE FW.L Freshwater flowrate (ton per hour)
 j1 45.000, j2 2.602

---- 197 VARIABLE WW.L Waste of each source (ton per hour)
 i1 17.555, i2 34.000, i3 54.940, i4 141.107

---- 197 VARIABLE FS.L Flowrate outlet (ton per hour)
 i1 45.000, i2 34.000, i3 56.000, i4 200.000

---- 197 VARIABLE FD.L Flowrate inlet (ton per hour)
 j1 45.000, j2 34.000, j3 56.000

---- 197 VARIABLE x.L Source split fraction i to j

| | j2 | j3 |
|----|-------|-------|
| i1 | 0.565 | 0.045 |
| i3 | | 0.019 |
| i4 | 0.030 | 0.265 |

---- 197 VARIABLE F.L Splitting flowrate i to j (ton per hour)

| | j2 | j3 |
|----|--------|--------|
| i1 | 25.425 | 2.019 |
| i3 | | 1.060 |
| i4 | 5.972 | 52.921 |

---- 197 VARIABLE y.L

| | j2 | j3 |
|----|-------|-------|
| i1 | 1.000 | 1.000 |
| i3 | | 1.000 |
| i4 | 1.000 | 1.000 |

---- 197 VARIABLE DA.L Sink stream concentration A (ppm)

j2 20.000, j3 51.956

---- 197 VARIABLE DB.L Sink stream concentration B (ppm)

j2 300.000, j3 20.000

---- 197 VARIABLE DC.L Sink stream concentration C (ppm)

j2 29.686, j3 200.000

---- 197 VARIABLE CWA.L waste concentration A (ppm)

i1 263.331, i2 4080.000, i3 12086.779, i4 7055.347

---- 197 VARIABLE CWB.L waste concentration B (ppm)

i1 7022.170, i2 425000.000, i3 2472.296, i4 705.535

---- 197 VARIABLE CWC.L waste concentration C (ppm)

i1 614.440, i2 6120.000, i3 521929.087, i4 2822.139

---- 197 VARIABLE OCWA.L = 154.281 Overall waste concentration A (ppm)

VARIABLE OCWB.L = 4079.952 Overall waste concentration B (ppm)

VARIABLE OCWC.L = 4964.210 Overall waste concentration C (ppm)

VARIABLE WTA.L = 51.687 Concentration of waste treatment A (ppm)

VARIABLE WTB.L = 70.934 Concentration of waste treatment B (ppm)

VARIABLE WTC.L = 100.000 Concentration of waste treatment C (ppm)

VARIABLE t.L = 46.832 treatment fraction

VARIABLE FWCost.L = 799717.942 Total cost of freshwater (\$ per y)

VARIABLE TCost.L = 1341290.134 Total cost of Treatment (\$ per y)

VARIABLE nXCost.L = 50000.000 Total cost of water splitting units (\$)

VARIABLE nFCost.L = 20000.000 Total cost of water feeding units (\$)

EXECUTION TIME = 0.016 SECONDS 3 MB 24.2.1 r43572 WIN-VS8

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**** FILE SUMMARY

Input C:\Users\DoNuT\Documents\gamsdir\projdir\Data 1 Case 3 - Water Network with end of pipe.gms

Output C:\Users\DoNuT\Documents\gamsdir\projdir\Data 1 Case 3 - Water Network with end of pipe.lst

CURRICULUM VITAE

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| | | |
|----------------|---------------|------------------|
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Publications:

1. Pungthong, K; and Siemanond K. (2015) Multiple-contaminant Water Network Synthesis. Computer Aided Chemical Engineering, in press.
2. Pungthong, K; and Siemanond K. (2015) The Retrofit Design for Water Network with Multiple Contaminants of Industrial Process. Chemical Engineering Transactions, in press.

Proceedings:

1. Pungthong, K; and Siemanond K. (2015, April 21) Multiple-contaminant Water Network Synthesis. Proceedings of The 6th Research Symposium on Petroleum, Petrochemicals and Advanced Materials and The 21th PPC Symposium on Petroleum, Petrochemicals, and Polymers, Bangkok, Thailand.

Presentations:

1. Pungthong, K; and Siemanond K. (2015, April 21) Multiple-contaminant Water Network Synthesis. Poster presented at Proceedings of The 6th Research Symposium on Petroleum, Petrochemicals and Advanced Materials and The 21th PPC Symposium on Petroleum, Petrochemicals, and Polymers, Bangkok, Thailand.

2. Pungthong, K; and Siemanond K. (2015, May 31 – June 4) MINLP optimization model for water/wastewater networks with multiple contaminants. Poster presented at 12th International Symposium on Process Systems Engineering and 25th European Symposium on Computer Aided Process Engineering (PSE2015/ESCAPE25), Copenhagen, Denmark.
3. Pungthong, K; and Siemanond K. (2015, Aug 23 – 27) The Retrofit Design for Water Network with Multiple Contaminants of Industrial Process. Poster presented at Proceedings of The 18th International Conference on Process Integration, Modelling and Optimization for Energy Saving and Pollution (PRES' 15), Kuching, Sarawak, Malaysia.